# Enhanced Functional Potential of Nucleic Acid Aptamer Libraries Patterned to Increase Secondary Structure 

Karen M. Ruff, Thomas M. Snyder, and David R. Liu*

## Supporting Information

## Library Design

After choosing a pattern in which purine-rich positions pair with pyrimidine-rich positions (see the main text) we next considered possible arrangements of purines and pyrimidines in the library. One possibility would be a long stretch of purines that would find and base pair with a long stretch of pyrimidines $\left(\mathrm{R}_{\mathrm{n}} \mathrm{Y}_{\mathrm{n}}\right)$. A second possibility would be a track of alternating purines and pyrimidines that would find and base pair with another track of alternating purines and pyrimidines ((RY) $)_{\mathrm{n}}$ ). One thousand randomly chosen sequences matching these two possible patterns were generated and folded in silico using the Oligonucleotide Modeling Platform (OMP, DNA Software), and the average folding energies of the two patterns were compared (Figure S1). The (RY) ${ }_{\mathrm{n}}$ library members exhibited a significantly higher average predicted folding energy than $\mathrm{R}_{\mathrm{n}} \mathrm{Y}_{\mathrm{n}}$ library members, possibly because any RY track can pair with any other RY track, while in an $R_{n} Y_{n}$ sequence, purine stretches can only pair with pyrimidine stretches, and not other purine stretches. We therefore chose to use library patterns in which purines and pyrimidines alternate.


Figure S1. Predicted folding energies of two possible patterns. $(\mathrm{RY})_{\mathrm{n}}=$ $(\mathrm{RY})_{4} \mathrm{NNN}(\mathrm{RY})_{5} \mathrm{NNNN}(\mathrm{RY})_{5} \mathrm{NNN}(\mathrm{RY})_{5} \mathrm{NNNN}(\mathrm{RY})_{4} ; \mathrm{R}_{\mathrm{n}} \mathrm{Y}_{\mathrm{n}}=\mathrm{R}_{8} \mathrm{NNNY}_{10} \mathrm{NNNNR}_{10} \mathrm{NNNY}_{10} \mathrm{NNNNR}_{8}$

We focused on library designs that contain several alternating patterned and $\mathrm{N}_{\mathrm{m}}$ stretches to maximize the ways in which each patterned region can interact with multiple other patterned or random regions. Sixty-base variable regions were chosen to allow the inclusion of multiple pattern and $\mathrm{N}_{\mathrm{m}}$ regions while still maintaining the ability of the libraries to be synthesized as a single degenerate oligonucleotide without requiring enzymatic ligation. In addition, Knight, Yarus, and coworkers found that the optimal variable region length for selecting a simple, well-studied isoleucine aptamer was between 50 and 70 nucleotides. ${ }^{1}$

## Choice of Primer-Binding and Tag Sequences

Following the design of the variable regions of the $\mathrm{N}_{60}, \mathrm{R}^{*} \mathrm{Y}^{*}$, and RY libraries, we calculated the predicted average folding energy of 5,000 arbitrarily chosen members of each library, without any constant sequences. Next we identified a 6-base tag sequence for each library that did not perturb the relative folding energies of the libraries or their spreads (standard deviations). These tags were chosen to be cleavable by restriction endonucleases. Several possible tag sequences were screened computationally to identify tags that would not affect the predicted folding energy distribution of the libraries. Similarly, primer sequences were chosen that meet the usual requirements of similar and sufficiently high melting temperatures and no mutual or self-complementarity at their $3^{\prime}$ ends, and that also preserve the relative folding energies of the libraries (Figure 1 in the main text and Table S1). The final primer and tag sequences are given below. Note that the constant sequences increased the folding energy of all libraries because the extra sequences increase the opportunities to form internal base pairing, even though the predicted relative folding energies of the three libraries and the standard deviation of these energies remain similar to that of the libraries lacking these constant regions.

| library | average predicted $\Delta \mathrm{G}$ of folding $\pm$ standard deviation $(\mathrm{kcal} / \mathrm{mol})$ |  |  |
| :---: | :---: | :---: | :---: |
|  | no primer | streptavidin primer set | IgE/VEGF primer set |
| N | $-11.2 \pm 3.2$ | $-12.0 \pm 3.3$ | $-16.3 \pm 3.3$ |
| $\mathrm{R}^{*} \mathrm{Y}^{*}$ | $-13.6 \pm 3.5$ | $-14.3 \pm 3.6$ | $-20.2 \pm 3.8$ |
| RY | $-16.1 \pm 3.7$ | -- | $-22.6 \pm 4.0$ |

Table S1. Predicted folding energies of libraries with and without primers.
Streptavidin selection library sequences:
$\mathrm{N}_{60}$ ( $5^{\prime}$-CGGTGCTCCTTGCGGTC-GGATCC- $\mathrm{N}_{60}$-GCACCAGACCACACGG), where $\mathrm{N}=$ 25:25:25:25 A:C:G:T
$\mathrm{R}^{*} \mathrm{Y}^{*}\left(5^{\prime} \text {-CGGTGCTCCTTGCGGTC-CAGCTG-( } \mathrm{R} * \mathrm{Y}^{*}\right)_{4} \mathrm{~N}_{4}\left(\mathrm{R} * \mathrm{Y}^{*}\right)_{5} \mathrm{~N}_{3}\left(\mathrm{R}^{*} \mathrm{Y}^{*}\right)_{5} \mathrm{~N}_{4}\left(\mathrm{R} * \mathrm{Y}^{*}\right)_{5} \mathrm{~N}_{3}$ $\left(\mathrm{R} * \mathrm{Y}^{*}\right)_{4}$ GCACCAGACCACGACGG), where $\mathrm{N}=25: 25: 25: 25 \mathrm{~A}: \mathrm{C}: \mathrm{G}: \mathrm{T}, \mathrm{R} *=45: 5: 45: 5$, and $\mathrm{Y}^{*}=$ 5:45:5:45

IgE and VEGF selection library sequences:
$\mathrm{N}_{60}$ (5' TGTCGCTGCGTCGCCTG-GGATCC- $\mathrm{N}_{60}$ - CACCGGAAGACGCACGC), where N is a mixture that couples at 25:25:25:25 A:C:G:T
$\mathrm{R}^{*} \mathrm{Y}^{*}\left(5^{\prime}\right.$ TGTCGCTGCGTCGCCTG-CAGCTG- $\left(\mathrm{R} * \mathrm{Y}^{*}\right)_{4} \mathrm{~N}_{4}\left(\mathrm{R} * \mathrm{Y}^{*}\right)_{5} \mathrm{~N}_{3}\left(\mathrm{R} * \mathrm{Y}^{*}\right)_{5} \mathrm{~N}_{4}\left(\mathrm{R} * \mathrm{Y}^{*}\right)_{5} \mathrm{~N}_{3}$ $\left(\mathrm{R}^{*} \mathrm{Y}^{*}\right)_{4}$-CACCGGAAGACGCACGC), where $\mathrm{N}=25: 25: 25: 25 \mathrm{~A}: \mathrm{C}: \mathrm{G}: \mathrm{T} ; \mathrm{R}^{*}=45: 5: 45: 5 ; \mathrm{Y}^{*}=$ 5:45:5:45
RY ( $5^{\prime}$ TGTCGCTGCGTCGCCTG-GCTAGC-(RY) $)_{4} \mathrm{~N}_{4}(\mathrm{RY})_{5} \mathrm{~N}_{3}(\mathrm{RY})_{5} \mathrm{~N}_{4}(\mathrm{RY})_{5} \mathrm{~N}_{3}(\mathrm{RY})_{4}{ }^{-}$
CACCGGAAGACGCACGC), where $\mathrm{N}=25: 25: 25: 25 \mathrm{~A}: \mathrm{C}: \mathrm{G}: \mathrm{T} ; \mathrm{R}=50: 0: 50: 0$; and $\mathrm{Y}=0: 50: 0: 50$

## DNA Library Synthesis and Analysis

Libraries were synthesized using phosporamidite mixtures as described in the main text. Because different bases couple at different efficiencies, mixtures with molar ratios based on desired target ratios were not sufficient to achieve desired amounts of incorporation of the bases into the libraries. Instead, mixtures were optimized empirically using an HPLC assay that quantifies dimers of form [5'-mix-C]. After the mixtures were adjusted to achieve the desired coupling ratios, the $\mathrm{N}_{60}, \mathrm{R} * \mathrm{Y}^{*}$, and RY libraries were synthesized. Approximately 30 members of each library were cloned and sequenced. The target nucleotide ratios, the ratios observed by HPLC, and the ratios observed by DNA sequencing
at each type of position in all three libraries were in good agreement (Figure S2). The ratios observed by DNA sequencing were used to calculate binding motif probabilities and the folding energies of the libraries used in the selections.


Figure S2. Base ratios for IgE and VEGF starting libraries. Target (T), HPLC-determined (H), and sequencing-determined ( S ) nucleotide ratios for each type of position in all three libraries are shown. Error bars reflect the standard error from sequencing-determined ratios.

We generated 3,000 randomly chosen members from each library using the observed nucleotide ratios and determined their predicted energy of folding with the Oligonucleotide Modeling Platform (DNA Software) (Table S2). The $\mathrm{N}_{60}$ library base ratios and average energy were very close to the intended values. The $\mathrm{R} * \mathrm{Y}^{*}$ library had slightly lower incorporation of off-pattern bases than desired ( $3 \%$ instead of $5 \%$ each off-pattern base), but the A:G and C:T ratios were balanced and the average predicted folding energy was similar to the intended value. The experimental RY library had a significantly lower average predicted folding energy than a theoretical library with the intended ratios ( $\Delta \Delta \mathrm{G}=2 \mathrm{kcal} / \mathrm{mol}$ ), such that its average was the same as that of the $\mathrm{R}^{*} \mathrm{Y}^{*}$ library (standard deviation of the mean $=0.1 \mathrm{kcal} / \mathrm{mol}$ ). We believe that the slightly higher abundance of A and T lowered the overall average folding energy. Because the experimental RY library is predicted to have the same folding energy average and standard deviation as that of the $\mathrm{R} * \mathrm{Y} *$ library, they can be directly compared to determine the importance of incorporating a small fraction of off-pattern bases at each patterned position.

|  | energy of folding (kcal/mol) |  |
| :---: | :---: | :---: |
| library | average | standard deviation |
| $\mathrm{N}_{60}$ | -16.2 | 3.3 |
| $\mathrm{R}^{*} \mathrm{Y}^{*}$ | -20.6 | 3.6 |
| RY | -20.6 | 3.6 |

Table S2. Experimental folding energies of IgE and VEGF starting libraries.
The starting library for the streptavidin selection used different primer-binding sequences and was synthesized separately with different phosphoramidite mixes. The sequences of 25 clones from the
input library were aligned with the pattern and the experimental ratios of the bases at each position were determined (Table S3).

|  | A | C | G | T |
| :---: | :---: | :---: | :---: | :---: |
| N | 26 | 28 | 18 | 28 |
| $\mathrm{R}^{*}$ | 52 | 4 | 41 | 3 |
| $\mathrm{Y}^{*}$ | 2 | 40 | 2 | 56 |

Table S3. Observed base ratios (in percent) in the starting library for the streptavidin selection.
While some of these variations in composition were wider than desired, the patterning was successful with predominantly purines/pyrimidines at the appropriate positions in the structured library. We remodeled the folding energies of the $\mathrm{N}_{60}$ and $\mathrm{R}^{*} \mathrm{Y}^{*}$ libraries using our estimates of the compositions given above. The average energy of our synthesized $\mathrm{N}_{60}$ library is $-9.8 \pm 3.2 \mathrm{kcal} / \mathrm{mol}$, and the average energy of $\mathrm{R}^{*} \mathrm{Y}^{*}$ is $-13.0 \pm 3.3 \mathrm{kcal} / \mathrm{mol}$. Thus the average predicted folding energy difference between the libraries was $3.2 \mathrm{kcal} / \mathrm{mol}$, one standard deviation of the $\mathrm{N}_{60}$ library (comparable to the one standard deviation difference in average energy of the theoretical libraries).

## PCR Amplification Efficiency Tests

a)

b)


Figure S3. DNA libraries amplify with comparable efficiency when tested (a) separately under the same conditions with common primers, and (b) in one solution carried through ten successive cycles of 128 -fold dilution and PCR amplification. Error bars represent the standard error of three digestions. For (a), we generated standard curves for each library by $q P C R$, fit the $\mathrm{C}_{\mathrm{T}}$ values to a line based on the natural $\log$ of the known starting amount of DNA, and determined the amplification efficiencies according to the formula, efficiency $=\left[\mathrm{e}^{\wedge}(-1 /\right.$ slope $\left.)-1\right] * 100 \%$. The three libraries amplify with similar efficiencies.

## Restriction Digestion of Tag Sequences

We used tag digestions to determine the bulk library ratios in our selection pools. These digestions were performed under conditions that resulted in complete cleavage of the target library, but no offtarget cleavage of the other two libraries (Figure S4).


Figure S4. Library digestions by tag-specific endonucleases. For each library, the corresponding enzyme causes complete digestion, while a combination of the other two enzymes results in no digestion.

## Analysis of Selection Results

## Library Ratios by Restriction Enzyme Digestion

We digested the pool material from each round of the three selections under the same conditions used in Figure S4. The library ratios across each of the three selections are depicted in Figure S5. For both the streptavidin and VEGF selections, the presence of significant uncut DNA especially in later rounds (representing up to $\sim 30 \%$ of either selection's pool) obscured interpretation. We attribute the uncut DNA to mutations in tag sequences, as was explicitly observed in sequences of $\mathrm{R}^{*} \mathrm{Y}^{*}$-derived clones in both the streptavidin and VEGF selections, or to inefficient digestion of particularly wellfolded DNA sequences.
a)

b)
$\lg E$ selection

c)


Figure S5. Tag cleavage ratios for selections against (a) streptavidin, (b) IgE, and (c) VEGF. Error bars indicate the standard error of three replicate digestions; ** the striped bars indicate the normalized percentage of clone V9-103 (which was from the $\mathrm{R}^{*} \mathrm{Y}^{*}$ library but which contained a mutation in its tag sequence, preventing digestion), as determined by sequence-specific digestion in Figure S7. Due to the significant presence of uncut DNA in the streptavidin and VEGF selections, tag sequences were
used primarily to ascertain a library member's origins rather than to calculate library abundances by digestion.

Streptavidin Selection Sequences
For the streptavidin selection, the round 10 pool was sequenced, and 37 distinct sequences were determined (Table S4a). As described in the text, 27 of these 37 sequences contained a common hexaloop motif (bulge/loop in bold; stems underlined in Table S4a). Additionally, four sequences contained related motifs with expanded bulges or loops. Several clones, including the most frequent $\mathrm{R}^{*} \mathrm{Y}^{*}$ clone, contained mutations in the library tag that preclude digestion (mutated tags italicized in Table S4a). The standard motif occurred in the same frame in all of the $\mathrm{R}^{*} \mathrm{Y}^{*}$ clones $\left(\mathrm{R}^{*} \mathrm{Y}^{*}\right.$ pattern shown for comparison). The sequences' frequency and motif characteristics are described in Table S4b.

| ne | G) |
| :---: | :---: |
|  | RYRYRYRY NNNN RYRYRYRYRY NNN RYRYRYRYRY NNNN RYRYRYRYRY NNN RYRYRYRY |
| S10-317 | CAGCTG AGAAGCGC CAGG GTGTACATGC ACA ACGCGTACGC CGCA GTACTTGTGC TTA ACATGTGT |
| S10-134 | CAAGCTGACGGCACGCCGAA GTATGCACAC TTA ACGCGTACGC TGCA GTACTTAAGI TGT GTATCGCC |
| S10-171 | CAGCTG ACGCACGC TAAA ACATACGAAT ATG ACGCGTACGC TGCA GTACTCATAT ICC GCGCATAT |
| S10-338 | CAGCTG ACACGCAT CGAG AACTACGCAT ATG ACGCGTACGC TGCA GTACTCATAT GCI ATAAACGT |
| S10-132 | CAGCTG GTACGCAT CCAC ACGTATGCGC AGA ACGCACATGT CGCA ATGTTTATGC GCT ATGCGTGT |
| S10-104 | CAGCTG ACACGTAT CCGG TCGTACATAT TTA GCGCGTGIGT CGCA ACACCTATAT ATG ACGCGTGT |
| S10-164 | CAGCTG ATACACGT GAGG ATACATACAT TTG ACGCGTGCGT CGCA GCACTCAAAT TGT ACACGTAT |
| S10-102 | CAGCTG ATACAGCAAACTG ACACATACAC ATG GCGCGTGTGC CGCA ACACCCATGI AGT ACGTGTGT |
| S10-303 | CAGCTG ACGCGCAACGTAT GTACTGGCAT GCG ACGCATGTGT CGCA ACATTCGCAG GAA GTATATAC |
| S10-321 | CAGCTG ATATAGAT TTGT GTATGCATAC GTA ACGCATACGC CGCA GTATTTACGT ATG GTATACGC |
| S10-201 | CAGCTG ACAGTGTACATTA GTGCACATAC GAA ACGCATATGT CGCA ATATTTTCGT AGT ATGCCCGC |
| S10-122 | CAGCTG GCACGTAG GATA GTATAAATGG GAA ACGCATACGC CGCA GTATTTGCCC GGA ATATATGT |
| S10-161 | CAGCTG AATATATTCTGTC GCTTATATGT ACG ACGCGTACGT CGCA GTACTCGTAC TAA ACACACAT |
| S10-353 | CAGCTG ACGCACAGTGCTT GCATACATAT ACA ACGCGTACGT CGCA GTACTCGTAC TAA GCACACAC |
| S10-340 | CAGCTG ACAGACAT GCGT CCTTACACAC GAA GCGCGTGTGT CGCA ACACCTTCGI TTG ACAGGCGC |
| S10-123 | CAGCTG GCGCGCAT AACC ACGCACGTAC ATT ICGCGTACGT CGCA GTACAAATGI TTG ACACGCGT |
| S10-175 | CAGCTG GCGTACGT GGTG ATACGTATGC ATG GCGCGTGTGT CGCA ACACCCATGI CTA ATGTACGT |
| S10-323 | CAAGCTGGTGCACGC GGTA GCATATACGT GTG ACGCGTGTGC CGCA ACACTCATAC TAT GTATATGC |
| S10-342 | CAAGCTGGCATACGT AATC ATGCATTCAT ATA ACGCGTGIGT CGCA ACACTTATAT GTA GTATATGC |
| S10-101 | CAGCTG ACATACGC ACTG GTGCAGTATACGTA ACGCATACGC CGCA GTATTTATGI TAT GCACGTGC |
| S10-215 | CAGCTG GTAGGCAC TCAT GCGTGCACAT ATG ACGCATACGT CGCA GTATTCATAT TTC ACATGCGC |
| S10-217 | CAGCTG GCATCCGT ACGA GCACATACAC GTG ACGCATATGT CACA ATATTCACGI ATT ATGTGCGC |
| S10-355 | CAGCTG GTACACCT TCGG AGATAIACGT ATC GCTCACACGC CGCA GTGTGTACGT AAT ATCTACAT |
| S10-124 | CAGCTG ATACACAT TTGC ACCTCGACGC AGA GGATGTGTGT CCGC ATGGACGTAC GGG ATGCATGT |
| S10 | GGGATCCAATAATAGGACAAACGCACACGGCGCAGTGTTTTGACCTACTTAGCCGACGCTGTCCCCG |
| S10-173 | GGATCC TGTTACTATAAACGCTACTGTCGCAAGTATTTATAGTCACTTACTGACCACTCAGCCTGC |
| S10-205 | GGATCC ATCGTAATTCAATTCACTGATAACATGCCATCGTCGCAGATGTGTTATTCTGATATTGCC |
| S10-346 | GGATCC ATCTCCTATAAATGCCTATGCCGCAATAGTTTATAGCCTCTGCAACTGGCTCGTCTGCCCC |
| S10-314 | GGATCC AAAGCTTGACCGTCATGTACAAAACACCCATGATGCCAATGCCGCAATTGTCATGGACGT |
| S10-115 | GGACC CGCGGTAAGITGTGITTGCTCCCCGACGCAGGGGACACAAATACCCTACTGTCTCTCGCT |
| S10-113 | GGATCC ATTTGAAGATTAGCAAACCICGCGCCGATTGCAGGCAGGTTTGATTGATGACCTGGCCCC |


| S10-114 | CAGCTG ACACGCGT TATT GGGTAACTGT CCA CCACGCATGA GGGC TCACATACGT ACA GTGTATGG |
| :---: | :--- |
| S10-111 | CAGCTG ACCTATCT GGTC GGGTTTATAT TAA ACATATACAT TAGA ATACGTTTGT ACC GCGCGTAT |
| S10-162 | CAGCTG GTATACGATCAGA GTACGCATAT CAT ACGCGGGTGT TGCT CCCTATGTAC TAT GCGCACGT |
| S10-144 | CAGCTG GCATGCGC AGAT GTATCCACAC GTA ACGCACACAT CGGT GTTTACGGGC GGT ACTCGTGC |
| S10-155 | CAGCTG ACGCATAT CCGT ACGTATGCAT GGA GTGAATGAGT CGCA ACGCGTATTT GGG ATACTTGC |
| S10-121 | GGATCC GGCCAGCACTCTGTTACGCGTAATTGGGTTACTAACATATCCTGGGACTCTCGTAGCCCT |

Table S4a. Streptavidin selection round 10 sequences.

| clone | percent of round 10 | library | motif | major predicted fold displays motif? | predicted energy of <br> folding ( $\mathrm{kcal} / \mathrm{mol}$ ) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| S10-317 | 1\% | R*Y* | standard | yes | -17.9 |
| S10-134 | 15\% | R*Y* | standard | yes | -17.1 |
| S10-171 | 1\% | R*Y* | standard | yes | -16.8 |
| S10-338 | 1\% | R * $\mathrm{Y}^{*}$ | standard | yes | -20.1 |
| S10-132 | 1\% | R * $\mathrm{Y}^{*}$ | standard | yes | -20.2 |
| S10-104 | 3\% | $\mathrm{R} * \mathrm{Y}^{*}$ | standard | yes | -15.9 |
| S10-164 | 1\% | $\mathrm{R} * \mathrm{Y}^{*}$ | standard | yes | -17.5 |
| S10-102 | 1\% | R* $\mathrm{Y}^{*}$ | standard | yes | -19.2 |
| S10-303 | 3\% | R* ${ }^{*}$ | standard | yes | -20.8 |
| S10-321 | 1\% | R* ${ }^{*}$ | standard | yes | -14.1 |
| S10-201 | 12\% | R*Y* | standard | yes | -14.0 |
| S10-122 | 1\% | R*Y* | standard | no | -13.0 |
| S10-161 | 1\% | R*Y* | standard | no | -14.5 |
| S10-353 | 1\% | R*Y* | standard | no | -13.6 |
| S10-340 | 1\% | $\mathrm{R}^{*} \mathrm{Y}^{*}$ | standard | no | -20.6 |
| S10-123 | 1\% | R * $\mathrm{Y}^{*}$ | standard | no | -17.5 |
| S10-175 | 1\% | R*Y* | standard | no | -19.9 |
| S10-323 | 1\% | R * $\mathrm{Y}^{*}$ | standard | no | -21.3 |
| S10-342 | 3\% | R * $\mathrm{Y}^{*}$ | standard | no | -15.5 |
| S10-101 | 5\% | R * $\mathrm{Y}^{*}$ | standard | no | -18.3 |
| S10-215 | 5\% | R* $\mathrm{Y}^{*}$ | standard | no | -17.1 |
| S10-217 | 3\% | R*Y* | *GTCACA | yes | -19.0 |
| S10-355 | 1\% | R* ${ }^{*}$ | *5-5-6 | yes | -16.1 |
| S10-124 | 1\% | R*Y* | *5-4-6 | yes | -20.2 |
| S10-103 | 11\% | $\mathrm{N}_{60}$ | standard | yes | -14.8 |
| S10-173 | 1\% | $\mathrm{N}_{60}$ | standard | yes | -13.2 |
| S10-205 | 1\% | $\mathrm{N}_{60}$ | *TGC | yes | -9.0 |
| S10-346 | 1\% | $\mathrm{N}_{60}$ | *TGC | yes | -11.9 |
| S10-314 | 1\% | $\mathrm{N}_{60}$ | *TGC | yes | -17.5 |
| S10-115 | 1\% | $\mathrm{N}_{60}$ | *5-4-6 | yes | -19.1 |
| S10-113 | 4\% | $\mathrm{N}_{60}$ | *3-3-7 | no | -16.4 |
| S10-114 | 1\% | R * $\mathrm{Y}^{*}$ | unknown |  |  |
| S10-111 | 1\% | R * $\mathrm{Y}^{*}$ | unknown |  |  |
| S10-162 | 1\% | R * $\mathrm{Y}^{*}$ | unknown |  |  |
| S10-144 | 1\% | $\mathrm{R} * \mathrm{Y}^{*}$ | unknown |  |  |


| S10-155 | $1 \%$ | $\mathrm{R}^{*} \mathrm{Y}^{*}$ | unknown |  |  |
| :---: | :---: | :---: | :---: | :--- | :--- |
| S10-121 | $3 \%$ | $\mathrm{~N}_{60}$ | unknown |  |  |

Table S4b. Summary of streptavidin selection round 10 clones.
We synthesized minimized forms of five sequences from among the round 10 clones, including several with the standard bulge/loop sizes and also one each with an expanded bulge and expanded loop. Because the motif was apparent by inspection, minimal sequences were analyzed by CE (Table S5, bulge/loop sequences are shown in italics).

| clone | sequence |
| :---: | :--- |
| S10-101 | CACGTAACGCATACGCCGCAGTATTTATGTG |
| S10-103 | TAGGACAAACGCACACGGCGCAGTGTTTTGACCTA |
| S10-104 | CATATTTAGCGCGTGTGTCGCAACACCTATATATG |
| S10-113 | CAAACCTCGCGCCGATTGCAGGCAGGTTTG |
| S10-115 | CTTGTGTTTGCTCCCC GACGCAGGGGACACAAG |
| consensus | CGCTGACGCGTACGTCGCAGTACTCAGCG |
| NRR | CTGTGAGACGACGCACCGGTCGCAGGTTTTGTCTCACAG |

Table S5. Minimal streptavidin binding motif analyzed by capillary electrophoresis.
IgE Selection Sequences
The round 9 pool from the IgE selection was sequenced, and 23 distinct sequences were found (Table S6). I9-102 occurred 60 times, while the other 22 sequences were unique.

| clone | library | sequence (variable region; full length = TGTCGCTGCGTCGCCTG-variable-CACCGGAAGACGCACGC) |
| :---: | :---: | :---: |
| I9-101 | R*Y* | CAGCTGACGTGTAATGTTGATGCAAACATCGTACACACGCGTTCTGGCCCGACGCATGCGGCACGCGC |
| 19-102 | $\mathrm{R}^{*} \mathrm{Y}^{*}$ | CAGCTGACGTACGTGCATGGCAAACACACTTCATCCGTACCTTCTAGTGGGTGTGTAGCAAGCGCGC |
| 19-103 | $\mathrm{R}^{*} \mathrm{Y}^{*}$ | CAGCTGACATGTATCCCGATACATGCCTGATCCACACGCATCACGACATACGCGCCACGNNCGGG |
| 19-104 | R * $\mathrm{Y}^{*}$ | CAGCTGATGTATCTTCGTGCGGGCACAAATCATATATGCGTCAATGACACGTAAGCGGCATGTGTGC |
| 19-107 | $\mathrm{R}^{*} \mathrm{Y}^{*}$ | CAGCTGGGGGCCTATTGCAGTAAGCACGCCGCGCGCATACGCCNTCGGATGGACGCAAGACACGTGT |
| I9-110 | RY | GCTAGGCGTGTACGTTGTGGGCACACACACTAAATGTACATGCGGAGACACACGCGCGCGACACATGC |
| I9-111 | RY | GCTAGCGCGTACGCTACGACATGTGCGCGGAATGTGTATATCTAGGCACACGTGCCAAATATGTAT |
| 19-113 | N | GGATCCTCGTCGGAAACAAAACCCCGTTTCGGTGATTGGGGATCAAGGGCGACTCAGGGAGAGCATA |
| 19-115 | R* $\mathrm{Y}^{*}$ | CAGCTGATAGGCTATTCTTGTACATGCAGTAAAACGTACGCACTCCCACCCATATATCGCGCATATAT |
| I9-116 | $\mathrm{R}^{*} \mathrm{Y}^{*}$ | CAGCTGATGTGTGTTCCTGTATGCGAGAACACCATCTACGCTCGGGTAGACGCATTGGGGCACGTGC |
| I9-117 | $\mathrm{R}^{*} \mathrm{Y}^{*}$ | CAGCTGCCATCCATCGCCACGCCCGTACCCCACGCACACTCTCCCATCTACCTACGCCACACATTT |
| I9-119 | N | GGATCCGATTGGATCATAGGTAAGAAGGCAGGGAGATGCGCTTATGTAGGGGGACCCGCGGGTGG |
| 19-202 | N | GGATCCTTCGGGACGTCGGAAGCCAGGTTAAGATGATCCGAGGCACACCATACTCACACAAGACCGTG |
| 19-204 | N | GGATCCATTAATCCGTTCTTTATCCTCCACCCTCTCAATTCCCTAGTATTTACCCATCAGGCCTACG |
| 19-211 | N | GGATCCGTTCCTGGTAAGAGTTGTAAACATAACTGAAACTGAGGGGGGAGAACACAGGGACGCGCG |
| 19-216 | $\mathrm{R} \mathrm{Y}^{*}$ | CAGCTGATACGTGGGAGATGGTGTAGACACCCCATACGCGTGATAAGGGCTGATGTGTGAGACGCGCGC |
| I9-219 | $\mathrm{R}^{*} \mathrm{Y}^{*}$ | CAGCTGATGCACGCGAGGGTGCTAATGCGGCAAGCGCAGGCAGGGACACGTGCACATGGTACATGT |
| I9-224 | N | GGATCCCACTTCCCTTCCACCATCCCCCGATCTTTGTTACCTCAACGTAGGCCTCCCAGCAACACC |
| I9-230 | RY | GCTAGCGTATATGTCCACACATGCGTGTGGAACGTGTACGTAGAAATGCGTATGCAGCGCGCGTAT |
| 19-301 | RY | GGCTAGCACACGCACGGATACGCACGTATTCGGTGTGTGCATCCATATACGTACGCGCGACACGTAC |
| 19-309 | N | GGATCCATATCTCCCGTTCTTTGCCCCTCGCCCTTACTCCTCTTTTCGGTCCCATAAATCTTCACT |


| $19-313$ | $\mathrm{R}^{*} \mathrm{Y}^{*}$ | CAGCTGATGCACGCTAGAGGTGCTACACGCGTAACACATATTCAGCTGTGCATATGCATGACGCAGAT |
| :---: | :---: | :---: | :---: |
| $\mathrm{I9-317}$ | N | GGATCCAAACGTGCTGCGGCACCGAGCGATCACTGATTTACGACCTTGGGACAGCATGGAATCGACG |

Table S6. IgE selection round 9 sequences.

## IgE Binding Analysis

In contrast with the streptavidin selection results, no common motifs were apparent by inspection. Therefore, all 23 clones were analyzed for binding to IgE-linked beads. Only those clones with binding activity of $\sim 1 \%$ or more are shown in Figure S6.
a)

b)


Figure S6. Binding activity of the most active IgE clones to (a) immobilized IgE, and (b) free IgE by nitrocellulose filter binding. Error bars reflect the standard error of two replicates, except bead binding of I9-102, which is three replicates.

Binding constants were determined from nitrocellulose binding data by fitting to the curve:

$$
\text { signal }=\min +\max \times\left(\frac{K_{d}+D N A+I g E-\sqrt{\left(K_{d}+D N A+I g E\right)^{2}-4 D N A \times I g E}}{2 D N A}\right)
$$

where the DNA concentration was constant and much less than the $K_{d}$; the IgE concentration was the independent variable; and min and max signals are parameters optimized by the fit. The standard deviation of the $\mathrm{K}_{\mathrm{d}}$ was determined using a statistics package to determine the variance matrix of the parameters based on all of the independent data points.

## VEGF Selection Sequences

The round 9 and 10 pools surviving VEGF selection were sequenced, and 26 distinct sequences were determined. Several of these sequences occurred multiple times. Sequences and abundances are given in Table S7a and b. Mutated library tag sequences are underlined in Table S7a.

| clone | sequence (variable region; full length = TGTCGCTGCGTCGCCTG-variable-CACCGGAAGACGCACGC) |
| :---: | :--- |
| V9-101 | GGATCCGCTGCCTGTCGCGTGGGTCCGGATGGCGCAAGGTTTGCTTCGCGGCAGCTTATTGGGAA |
| V9-103 | CAGCTTGCGTAGTGAGTCCGAATGGGTGCACAAAGTGAGCGTATGCCAGTGCGCGCGCCATATACATAC |
| V9-104 | GGAATCCCTGCAGGCCCGGGCCAAAACACTGAAATCCGTACTTGCGGTGGAAGTCCGAATGGGTGTC |
| V9-105 | GGATCCCATATGGTTTACGTATTCCTGGTGCTACCCTGACGCCGGCACTCAGGCGCAGCCGGAAAG |
| V9-110 | GGGATCCGATTATGCTTAACAGCAGAGAGCCTGGCAGACTAGAGTGCAGCAGCGACTAACTTTAATA |
| V9-112 | GGATCCGCGTCCGAATGGCGCACTGAACCCAACGCACGACATTTCGCGAGAAACAGCCATCATCTA |
| V9-114 | CAGCTGAAGCAAGTCCGAATGGGTGTGTTCAGCATATGCACTGCGACGTGCGTACACCATACACGC |
| V9-132 | CAGCTTGGTATGCATACTAACTTACATACATGGTATATGAGTCCGAATGGGTGCATATAATATGTAC |
| V9-201 | GGATCCACGTAGACGCGTATCCAACGTTGACACTCGACTGCATCATCTGAGCTAGCAATGCTAGT |


| V9-204 | GGATCCCGGCCGGCATAAGAGTCCGAATGGGTGCTTACAGTCTCGAATGGGCTTGCGATAGGGGAC |
| :---: | :--- |
| V9-209 | GGATCCTTTTCAGATACCCGGCACACCTCTGCAATTGCGGAGGCAAGGTCTAACTTCGACCAGGCA |
| V9-215 | GGATCCGAATGGGTCACACATGGGCTCACACAATAAGAGGTCCGAAGGGGACTCTTTTGAATCGCT |
| V9-218 | GGATCCGCGTGCAGGAAAAGGGCCGTGACGCGGCGCGAGCGTTCTTCATGGACCTGAACGCCAAAC |
| V9-224 | CAGCTGAGTACGTACTTTAATGCACAGCATGGTATATACTTGTAGGTGTACGCACACCCGACACGTGT |
| V9-228 | GGATCCCAGCGACTAATAATGCTACCCCGCAGCGCGTTAATATTTGCTGCTAGCACATTTTCAACTA |
| V9-229 | CAGCTGCTGTTTGTTTATACGTGTATACTCAATACGCACGCAACTGCAAACGCATACGATGTGTGC |
| V10-122 | GGAATCCAGCTGAGTCCGAATGGGTGCAGCCGGGCCAGGCAAAGCGAGTCCACCGGCCATTCATAAA |
| V10-208 | GGATCCCAACAAAATGGTCCGGATGGGTCAGTGCTTGGGGTCATGTCCGCATCCAGGCGACACGCG |
| V10-247 | GGATCCTCTGTTCGTCCAAACTACCGTGGACCTGTCGGTTTTGGACTAGAGGGCAGATACGGGGGA |
| V10-254 | GGATCCCCGTCCGAATGGCAGTCTCACTCTGTGTACGTGGGGTTAAGGCAACCAGCGGGCTCATCG |
| V10-209 | GGATCCGCTCTATGAAATTATTTTAAACGTATGTTAAAAATCGCCGCGCAGCCAGAGAGCTCAGG |
| V10-229 | GGATCCGCCTCCTCCCGCCGGGTGTTTGTTGAGTCCGAATGGGTGCCAAACGAGCGCGACACTGTC |
| V10-232 | GGATCCACGGTGTGCTTTGGTGTACAGCCCGTCGAAGACAAGAGCGCAGGGCTATCAGACCATGCA |
| V10-235 | GGATCCCATGGAGCTCAGATCAGGAAGGGACGCGGGGAGAATTGTGACGTATCCGGCTAAGGTACAT |
| V10-238 | GGATCCGTAAGCCGGTAGCCACGTCCGAATGGTGTGGTGTACGTCCGAATGGCGGAAGGGATGAGAT |
| V10-245 | GGATCCGCCTGTCGAATGAGTCCGAATGGGTGCAATCGTCGTTACCAATATTTCGCAAATCCCTCTA |

Table S7a. VEGF selection round 9 and round 10 sequences.

| clone | library | \% of round 9 pool | \% of round 10 pool |
| :---: | :---: | :---: | :---: |
| V9-101 | $\mathrm{N}_{60}$ | $13 \%$ | $28 \%$ |
| V9-103 | $\mathrm{R}^{*} \mathrm{Y}^{*}$ | $40 \%$ | $38 \%$ |
| V9-104 | $\mathrm{N}_{60}$ | $3 \%$ | $0 \%$ |
| V9-105 | $\mathrm{N}_{60}$ | $16 \%$ | $13 \%$ |
| V9-110 | $\mathrm{N}_{60}$ | $2 \%$ | $0 \%$ |
| V9-112 | $\mathrm{N}_{60}$ | $2 \%$ | $0 \%$ |
| V9-114 | $\mathrm{R}^{*} \mathrm{Y}^{*}$ | $2 \%$ | $1 \%$ |
| V9-132 | $\mathrm{R}^{*} \mathrm{Y}^{*}$ | $2 \%$ | $0 \%$ |
| V9-201 | $\mathrm{N}_{60}$ | $2 \%$ | $0 \%$ |
| V9-204 | $\mathrm{N}_{60}$ | $5 \%$ | $4 \%$ |
| V9-209 | $\mathrm{N}_{60}$ | $2 \%$ | $0 \%$ |
| V9-215 | $\mathrm{N}_{60}$ | $6 \%$ | $0 \%$ |
| V9-218 | $\mathrm{N}_{60}$ | $2 \%$ | $0 \%$ |
| V9-224 | $\mathrm{R}^{*} \mathrm{Y}^{*}$ | $2 \%$ | $0 \%$ |
| V9-228 | $\mathrm{N}_{60}$ | $2 \%$ | $0 \%$ |
| V9-229 | $\mathrm{R}^{*} \mathrm{Y}^{*}$ | $2 \%$ | $0 \%$ |
| V10-122 | $\mathrm{N}_{60}$ | $0 \%$ | $1 \%$ |
| V10-208 | $\mathrm{N}_{60}$ | $0 \%$ | $2 \%$ |
| V10-247 | $\mathrm{N}_{60}$ | $0 \%$ | $2 \%$ |
| V10-254 | $\mathrm{N}_{60}$ | $0 \%$ | $2 \%$ |
| V10-209 | $\mathrm{N}_{60}$ | $0 \%$ | $1 \%$ |
| V10-229 | $\mathrm{N}_{60}$ | $0 \%$ | $1 \%$ |
| V10-232 | $\mathrm{N}_{60}$ | $0 \%$ | $1 \%$ |
| V10-235 | $\mathrm{N}_{60}$ | $0 \%$ | $1 \%$ |


| V10-238 | $\mathrm{N}_{60}$ | $0 \%$ | $1 \%$ |
| :--- | :--- | :--- | :--- |
| V10-245 | $\mathrm{N}_{60}$ | $0 \%$ | $1 \%$ |

Table S7b. Summary of VEGF selection round 9 and round 10 clones.
a)
clone tag digestion

b)

9-103 quantification


Figure S7. Tag mutation among clones in the VEGF selection. (a) Digestion of common VEGF clones with cognate library tagging enzymes; (b) quantification of V9-103 by digestion with ApaLI.

As indicated in Table S7, several of the VEGF clones included insertions in the library tagging sequence that prevent restriction enzyme digestion, including the most common $\mathrm{R} * \mathrm{Y}^{*}$ clone, V9-103. The round 10 pool of the VEGF selection (Figure S5c) included a substantial amount of uncut dsDNA in the samples treated with all three enzymes ( $30 \%$ of the lane). In addition, $15-20 \%$ of the pool was cut in the presence of all three enzymes but not in the presence of any one enzyme alone. The three most common clones were analyzed individually by tag digestion (Figure S7a). As predicted by sequencing, clone V9-105 was fully digested by BamHI, and clone V9-103 was unaffected by PvuII. However, clone V9-101, despite its sequence indicating an intact tag, was only partially digested by BamHI.

In order to independently quantify the amount of V9-103 in the pool by digestion, we used the ApaLI restriction enzyme, which is predicted to digest clone V9-103 within its variable region but is not predicted to cut any of the other repeated clones listed in Table 5. We experimentally confirmed its specificity for V9-103 by showing that it completely digested this clone while not digesting the
other two most common clones, V9-101 and V9-105 (Figure S7b). Finally, we used this enzyme to quantify the amount of V9-103 in the VEGF selection round 9 and 10 pools. By digestion, the round 10 pool includes $23 \%$ clone V9-103 (Figure S7b).

## VEGF Binding Analysis

No common structural motifs were apparent by inspection, so we analyzed full-length VEGF clones. We tested those clones that occurred more than once in rounds 9 and 10 , and all of the tested clones bound VEGF beads (Figure S8). Given the prevalence of binding activity among these clones, it is probable that some or all of the unique clones also bind VEGF. We assume that the best binders are those which have enriched appreciably over the course of the selection and which therefore occur multiple times.


Figure S8. Analysis of VEGF clones observed multiple times during DNA sequencing by (a) VEGFlinked bead binding assay, and (b) free VEGF binding assay by nitrocellulose filter binding.

## Streptavidin Binding Motif Probability Calculation

Because individual sequence survival is stochastic during the early rounds of a selection, and because an input of $10{ }^{14}$ molecules covers $<1 \%$ of all sequences possible in an $\mathrm{N}_{60}$ library, the results of any given selection must be considered only one amongst many possible outcomes. An alternative approach to evaluating the functional potential of a nucleic acid library is to calculate the expected probabilities of a known motif occurring in the patterned and standard libraries.

The most common binding motif from the selection for streptavidin binding was:
XXXXXX-YGC-XXXX-GNYGCA-XXXX-XXXXXX,
where X indicates a position that must form a base pair across a stem. A single frame in the patterned library fits the bulge/loop motif better than any other frame. This frame is shown relative to the pattern:

$$
\begin{aligned}
& \text { XXXXXX-YGC-XXXX-GNYGCA-XXXX-XXXXXX } \\
& \text { RYNNNR-YRY-RYRY-RYNNNN-RYRY-RYRYRY }
\end{aligned}
$$

Alignment of the round 10 sequences from the $\mathrm{R}^{*} \mathrm{Y}^{*}$ library with the pattern revealed that, indeed, all 22 instances of the standard motif in the structured library occurred in this predicted frame (Table S4a). In contrast, one $\mathrm{R}^{*} \mathrm{Y}^{*}$ sequence ( C 4 ) with the expanded 5 -base bulge -TTCGW- contained the motif in a different frame. However several other frames of the $\mathrm{R} * \mathrm{Y}^{*}$ pattern fit the bulge/loop motif slightly less well but still add significantly to the overall likelihood of the motif occurring in the
library. The binding motif was compared to every register of the $\mathrm{R} * \mathrm{Y}^{*}$ pattern and the probability of motif occurrence was calculated, as discussed in the following pages.

Unlike $\mathrm{R}^{*} \mathrm{Y}^{*}$, every frame of $\mathrm{N}_{60}$ is alike, so the motif would be predicted to occur with equal frequency in any frame of the variable region. Indeed, the five round 10 sequences from the $\mathrm{N}_{60}$ library include the motif in different registers. Therefore, in considering the overall likelihood of the motif, the $\mathrm{N}_{60}$ library has 32 registers that could include a 29 -base motif.

For any given frame in a library variable region, the probability of motif occurrence is the product of the frequency of the required base(s) at each bulge/loop position times the product of the probability of ten base pairs. These values depend on the base frequencies observed in each mix from sequencing the input library (Table S3). As an example, the bulge/loop motif probability is calculated for the observed frame from the $\mathrm{R}^{*} \mathrm{Y}^{*}$ library and for any frame in the $\mathrm{N}_{60}$ library (Table S 8 ).

|  | frame | Y | G | C | G | N | Y | G | C | A | TOTAL |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{N}_{60}$ | any | $\mathrm{N}-.56$ | $\mathrm{~N}-.18$ | $\mathrm{~N}-.28$ | $\mathrm{~N}-.18$ | $\mathrm{~N}-1.0$ | $\mathrm{~N}-.56$ | $\mathrm{~N}-.18$ | $\mathrm{~N}-.28$ | $\mathrm{~N}-.26$ | $3.72 \times 10^{-5}$ |
| $\mathrm{R}^{*} \mathrm{Y}^{*}$ | observed | $\mathrm{Y}^{*}-.96$ | $\mathrm{R}^{*}-.41$ | $\mathrm{Y}^{*}-.40$ | $\mathrm{R}^{*}-.41$ | $\mathrm{Y}^{*}-1.0$ | $\mathrm{~N}-.56$ | $\mathrm{~N}-.18$ | $\mathrm{~N}-.28$ | $\mathrm{~N}-.26$ | $4.74 \times 10^{-4}$ |

Table S8. Probability of the bulge/loop motif in the observed frames in the $\mathrm{N}_{60}$ and $\mathrm{R} * \mathrm{Y}^{*}$ libraries used for the streptavidin selection.

The stem probability is equal to the likelihood of ten base pairs forming, where each base pair could be either of the two Watson-Crick pairs or a G-T wobble.
For the $\mathrm{N}_{60}$ library:
Likelihood of any two ' N ' making a pair AT $0.26 \times 0.28 \quad 0.0728$

| TA | $0.28 \times 0.26$ | 0.0728 |
| :--- | :--- | :--- |
| CG | $0.28 \times 0.18$ | 0.0504 |
| GC | $0.18 \times 0.28$ | 0.0504 |
| GT | $0.18 \times 0.28$ | 0.0504 |
| TG | $0.28 \times 0.18$ | 0.0504 |
| Total |  | 0.3472 |

For the $\mathrm{R} * \mathrm{Y}^{*}$ library:
Likelihood of any $\mathrm{R}^{*}$ and $\mathrm{Y}^{*}$ making a pair

| AT | $0.52 \times 0.56$ | 0.2912 |
| :--- | :--- | :--- |
| GC | $0.41 \times 0.40$ | 0.1640 |
| GT | $0.41 \times 0.56$ | 0.2296 |
| TA | $0.03 \times 0.02$ | 0.0006 |
| CG | $0.04 \times 0.02$ | 0.0008 |
| TG | $0.03 \times 0.02$ | 0.0006 |
| Total |  | 0.6868 |

By analogous calculations,
Likelihood of R* and R* making a pair 0.0886
Likelihood of $\mathrm{Y}^{*}$ and $\mathrm{Y}^{*}$ making a pair 0.0608
Likelihood of $\mathrm{Y}^{*}$ and N making a pair 0.3352
Likelihood of $\mathrm{R}^{*}$ and N making a pair 0.3956
Likelihood of N and N making a pair 0.3472
As an example, for the observed frame in the $\mathrm{R}^{*} \mathrm{Y}^{*}$ library, the probability of ten base pairs forming would be:

Probability of $\left(6 \mathrm{R}^{*}-\mathrm{Y}^{*}+1 \mathrm{R}^{*}-\mathrm{R}^{*}+2 \mathrm{Y}^{*}-\mathrm{N}+1 \mathrm{R}^{*}-\mathrm{N}\right)$ base pairs $=$
$(0.6868)^{6} \times(0.0886) \times(0.3352)^{2} \times(0.3956)=4.13 \times 10^{-4}$
Therefore, the total probability for the observed frame in $\mathrm{R}^{*} \mathrm{Y}^{*}$ would be:
Loop probability x stem probability $=4.74 \times 10^{-4} \times 4.13 \times 10^{-4}=1.96 \times 10^{-7}$

## Streptavidin Binding Motif Total Probability

The frequency of the required base(s) at each bulge/loop position and the probability of formation of each base pair were determined for every frame in both the $\mathrm{N}_{60}$ and $\mathrm{R} * \mathrm{Y}^{*}$ libraries using a computer program to assign a value based on the base ratios in the appropriate position in the pattern. These values were then multiplied to determine the overall probability of the motif occurring in each frame (Table S9). The probability in each frame was summed to determine the total probability for the library (Table S9). We treated the frames as independent from each other because the likelihood of the motif occurring in any given frame was so small as to have an insignificant effect on overlapping frames.

| frame | $\mathrm{N}_{60}$ | R*Y* | RY |
| :---: | :---: | :---: | :---: |
| 1 | $9.49 \times 10^{-10}$ | $5.99 \times 10^{-10}$ | 3 loop off |
| 2 | $9.49 \times 10^{-10}$ | $7.64 \times 10^{-11}$ | 4 loop off |
| 3 | $9.49 \times 10^{-10}$ | $1.53 \times 10^{-7}$ | 1 loop off |
| 4 | $9.49 \times 10^{-10}$ | $2.61 \times 10^{-12}$ | 4 loop off; 1 stem off |
| 5 | $9.49 \times 10^{-10}$ | $6.96 \times 10^{-11}$ | 1 loop off; 2 stem off |
| 6 | $9.49 \times 10^{-10}$ | $8.84 \times 10^{-12}$ | 2 loop off; 3 stem off |
| 7 | $9.49 \times 10^{-10}$ | $3.39 \times 10^{-15}$ | 4 loop off; 4 stem off |
| 8 | $9.49 \times 10^{-10}$ | $1.11 \times 10^{-10}$ | 4 stem off |
| 9 | $9.49 \times 10^{-10}$ | $1.98 \times 10^{-17}$ | 6 loop off; 4 stem off |
| 10 | $9.49 \times 10^{-10}$ | $5.33 \times 10^{-10}$ | 4 stem off |
| 11 | $9.49 \times 10^{-10}$ | $1.10 \times 10^{-17}$ | 7 loop off; 3 stem off |
| 12 | $9.49 \times 10^{-10}$ | $7.92 \times 10^{-9}$ | 2 stem off |
| 13 | $9.49 \times 10^{-10}$ | $6.80 \times 10^{-16}$ | 7 loop off; 1 stem off |
| 14 | $9.49 \times 10^{-10}$ | $1.39 \times 10^{-7}$ | 1 loop off |
| 15 | $9.49 \times 10^{-10}$ | $3.02 \times 10^{-13}$ | 6 loop off |
| 16 | $9.49 \times 10^{-10}$ | $1.51 \times 10^{-7}$ | 1 loop off |
| 17 | $9.49 \times 10^{-10}$ | $2.39 \times 10^{-11}$ | 4 loop off |
| 18 | $9.49 \times 10^{-10}$ | $6.09 \times 10^{-9}$ | 2 loop off |
| 19 | $9.49 \times 10^{-10}$ | $7.08 \times 10^{-9}$ | 2 loop off |
| 20 | $9.49 \times 10^{-10}$ | $2.60 \times 10^{-11}$ | 4 loop off |
| 21 | $9.49 \times 10^{-10}$ | 1.96x10 ${ }^{-7}$ | 1 stem off |
| 22 | $9.49 \times 10^{-10}$ | $2.94 \times 10^{-13}$ | 4 loop off; 2 stem off |
| 23 | $9.49 \times 10^{-10}$ | $9.81 \times 10^{-12}$ | 2 loop off; 3 stem off |
| 24 | $9.49 \times 10^{-10}$ | $8.16 \times 10^{-13}$ | 3 loop off; 3 stem off |
| 25 | $9.49 \times 10^{-10}$ | $2.22 \times 10^{-13}$ | 4 loop off; 2 stem off |
| 26 | $9.49 \times 10^{-10}$ | $3.79 \times 10^{-11}$ | 3 loop off; 1 stem off |
| 27 | $9.49 \times 10^{-10}$ | $2.16 \times 10^{-11}$ | 4 loop off |
| 28 | $9.49 \times 10^{-10}$ | $5.99 \times 10^{-10}$ | 4 loop off |
| 29 | $9.49 \times 10^{-10}$ | $7.64 \times 10^{-11}$ | 4 loop off |
| 30 | $9.49 \times 10^{-10}$ | $1.53 \times 10^{-7}$ | 1 loop off |
| 31 | $9.49 \times 10^{-10}$ | $2.61 \times 10^{-12}$ | 4 loop off; 1 stem off |


| 32 | $9.49 \times 10^{-10}$ | $6.96 \times 10^{-11}$ | 2 loop off; 2 stem off |
| :---: | :---: | :---: | :---: |
| total | $3.04 \times 10^{-8}$ | $8.16 \times 10^{-7}$ | impossible |

Table S9. Streptavidin-binding motif likelihood in each library.
Note that five frames contribute significantly to the overall motif probability for the $\mathrm{R}^{*} \mathrm{Y}^{*}$ library (probability greater than $1 \times 10^{-7}$ ). These likely $\mathrm{R}^{*} \mathrm{Y}^{*}$ frames have two or fewer mismatches for the binding motif bulge/loop positions and one or fewer mismatched pairing positions in the stem. The observed frame (21) is the most likely frame in $\mathrm{R}^{*} \mathrm{Y}^{*}$, and is 6.4 -fold more likely to contain the binding motif than the cumulative probability for every frame of $\mathrm{N}_{60}$. Including every frame in both libraries, the streptavidin-binding hexaloop motif is 27 -fold more likely in the $\mathrm{R}^{*} \mathrm{Y}^{*}$ library than in the $\mathrm{N}_{60}$ library.

A comparison of the binding motif to the RY pattern indicates that every frame contains at least one mismatched bulge/loop position or one mismatched base pair. Although the RY patterned library was not included in the selection for streptavidin binding, motif probability indicates that it would have failed to result in aptamers with the consensus motif.

## IgE Aptamer 9-102 Minimization and Motif Analysis

9-102 Minimization and Mutational Analysis
We identified the important region for binding IgE by synthesizing a series of sequences based on truncations and mutations of I9-102 (sequences shown in Table S10, loop sequences in italics, mutations in minimized sequence stems underlined). The results are summarized in Figure S9 and Figure 5a in the text.

| construct | sequence |
| :--- | :--- |
| $102 \_29-83$ | CGTGCATGGCAAACACACTTCATCCGTACCTTCTAGTGGGTGTGTAGCAAGCGCG |
| $102 \_29-83 \mathrm{~m}$ | CGTGCATGGCAAACACACTTCATGTGTGTAGCAAGCGCG |
| $102 \_1-26$ | TGTCGCTGCGTCGCCTGCAGCTGACG |
| 102 min A | GCACACACTTCATCCGTACCTTCTAGTGGGTGTGTGC |
| 102 minB | GCACACACCCGTACCTTCTAGTGGGTGTGTGC |
| 102 minD | GCACACACTTCATCCGTACCTTCTAGTCCGTGTGTGC |
| 102 minE | GCACACACTTCATGGGTACCTTCTAGTCCGTGTGTGC |
| 102 minG | GCACACICTTCATCCGTACCTTCTAGTGGCTCTGTGC |
| 102 minh | GCACAGTGTTCATCCGTACCTTCTAGTGGCACTGTGC |
| 102 minI | GCACAGAGTTCATCCGTACCTTCTAGTGGGGTGTGC |

Table S10. Sequences for I9-102 minimization and mutational analysis.


Figure S9. Predicted fold and binding activities of minimized IgE clone 9-102 variants.

## 102min Reselection

Having isolated the IgE binding activity in the large loop (bases 46-67 by full length I9-102 numbering), we wished to determine which of the positions in the loop were important for binding, and which, if any, were flexible. We designed and synthesized a library that was based on 102 minA , but which included variability at each position. The library sequence was:
5'ACCTATCGTATCCTACCGATTTgcacacacttcatccgtaccttctagtgggtgtgtgcTTTGTGGAGTAAGGT AGACTCA), where lower case bases are a mixture that gives ( $79 \%$ indicated, $7 \%$ each of the other bases). Fifty sequences from the input library were analyzed, and the base ratios are indicated in Figure S10.


Figure S10. Base ratios by DNA sequencing of the 102 min starting library, where each position was intended to be $79 \%$ consensus base and $7 \%$ each of the other three bases. Created with enoLOGOS. ${ }^{2}$

Selection for IgE binding starting with the 102 min library resulted in binding activity after four rounds, and sequencing showed that the pool had largely converged back to the 102 min sequence (Figure 6 in the main text). The resulting 59 total sequences, containing 42 unique sequences, were analyzed first for stem requirements, then for loop requirements for binding.

## 102min Motif Analysis

While many individual mutations were observed in the stem-forming region, wobble and covariation preserved base pairing across the stem. Of the 42 unique sequences, all eight base pairs were maintained in 25 cases, and seven of the eight were preserved in another 16 cases. All told, at least seven out of eight base pairs were preserved in 41 out of 42 cases. In addition, the outermost and two innermost base pairs were preserved in all 42 unique sequences. The significance of this preservation depends on the probability of maintaining these $5 \mathrm{G}: \mathrm{C}$ base pairs and $3 \mathrm{~A}: \mathrm{T}$ base pairs by chance in the starting library.

The probability of maintaining a base pair at any given pairing position is calculated from the frequencies of each base in the starting library. The probability of maintaining a base pair at a position that is $\mathrm{A}: \mathrm{T}$ or $\mathrm{T}: \mathrm{A}$ in the starting library is given below as an example:

$$
\begin{array}{lll}
\operatorname{Prob}\left(\mathrm{AT}_{\text {pair }}\right)= & \mathrm{AT}=0.801 \times 0.815= & 0.6528 \\
\mathrm{GT}=0.092 \times 0.815= & 0.0750 \\
\mathrm{CG}=0.056 \times 0.070= & 0.0039 \\
\mathrm{GC}=0.092 \times 0.064= & 0.0059 \\
\mathrm{TA}=0.052 \times 0.052= & 0.0027 \\
\mathrm{TG}=0.052 \times 0.070= & 0.0036 \\
\hline
\end{array}
$$

By an analogous calculation, the probability of maintaining a base pair at a position that is $\mathrm{G}: \mathrm{C}$ or $\mathrm{C}: \mathrm{G}$ in the starting library is $\operatorname{Prob}\left(\mathrm{GC}_{\text {pair }}\right)=0.6986$. Therefore, the probability of losing a base pair at a position that is A:T in the starting library is: $\operatorname{Prob}\left(\sim \mathrm{AT}_{\text {pair }}\right)=1-0.7439=0.2561$ and the probability of losing a base pair at a position that is $\mathrm{G}: \mathrm{C}$ in the starting library is: $\operatorname{Prob}\left(\sim \mathrm{GC}_{\text {pair }}\right)=0.3014$.

Using these probabilities, the probability of seven out of the eight base pairing positions in the stem being maintained in any sequence from the starting library can be calculated by:

The probability of all 8 base pairs being maintained

$$
(\mathrm{P}(\mathrm{GC}))^{5} \times(\mathrm{P}(\mathrm{AT}))^{3}=(0.6986)^{5} \times(0.7439)^{3}=0.16640 \times 0.41166=0.0685
$$

The probability of $7 / 8$ base pairs being maintained (with the three outer pairs fixed)

$$
\operatorname{Prob}(\text { outer }) \times \operatorname{Prob}(\text { variable })=
$$

$$
[\mathrm{P}(\mathrm{GC}))^{2} \mathrm{x}(\mathrm{P}(\mathrm{AT})] \mathrm{x}\left[3 \mathrm{x}(\mathrm{P}(\sim \mathrm{GC})) \mathrm{x}(\mathrm{P}(\mathrm{GC}))^{2} \mathrm{x}(\mathrm{P}(\mathrm{AT}))^{2}+2 \mathrm{x}(\mathrm{P}(\sim \mathrm{AT})) \mathrm{x}(\mathrm{P}(\mathrm{GC}))^{3} \mathrm{x}(\mathrm{P}(\mathrm{AT}))\right]
$$

$$
\left[(0.6986)^{2}(0.7439)\right] \times\left[3(0.3014)(0.6986)^{2}(0.7439)^{2}+2(0.2561)(0.6986)^{3}(0.7439)\right]=0.1358
$$

The probability of At least 7 pairs by chance in any one sequence

$$
=\operatorname{Prob}(8)+\operatorname{Prob}(7 / 8)=0.0685+0.1358=0.2043
$$

The probability of at least seven base pairs being maintained in any given sequence from the starting library is 0.2043 . Therefore, the binomial probability of at least seven base pairs occurring in 41 out of 42 sequences in the output pool by chance is less than 0.0001 ( $p$-value $<0.0001$ ). The $9-102$ motif for IgE binding is considered to be a stem with at least seven out of eight base pairs, with the loop described below.

The loops of the 42 unique clones in the round 4 pool are summarized in Table S11 (position numbering based on 102 minA ). White columns indicate entirely conserved positions, while increasing blue color indicates increasing flexibility at the position.

| position: |  | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 29 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| original |  | T | T | C | A | T | C | C | G | T | A | C | C | T | T | C | T | A | G | T | G |
| G |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $\#$ | A | 0 | 0 | 0 | 42 | 0 | 0 | 0 | 0 | 0 | 23 | 1 | 0 | 0 | 0 | 0 | 0 | 42 | 0 | 0 | 0 |
|  | C | 0 | 0 | 29 | 0 | 0 | 42 | 42 | 0 | 0 | 4 | 41 | 42 | 0 | 5 | 41 | 1 | 0 | 0 | 0 | 0 |
|  | G | 0 | 0 | 5 | 0 | 0 | 0 | 0 | 42 | 0 | 4 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 42 | 0 | 42 | n

Table S11. Summary of 102 min reselection loop sequences in the round 4 pool
For the conserved (white) positions, the significance of all 42 clones maintaining the original base can be calculated by determining the binomial probability of 'at least $42 / 42$ ' given the base ratios in the starting library. The ratios and significances for the conserved (white) positions are given in Table S12. All of the conserved (white) positions can be considered fixed in the binding motif with a significance $>0.999$.

| original base | frequency in input | $p$-value <br> prob(at least 42/42 in input) |
| :---: | :---: | :---: |
| A | 0.801 | 0.0001 |
| C | 0.734 | $<0.0001$ |
| G | 0.824 | 0.0003 |
| T | 0.815 | 0.0002 |

Table S12. Significance of highly conserved residues in the 102 min binding loop.
For the semi-conserved (light blue) positions, the significance of 41 of 42 clones maintaining the original base can be calculated by determining the binomial probability of 'at least 41/42,' given the base ratios in the starting library. The ratios and significances for the semi-conserved positions are given in Table S13. All of the semi-conserved (light blue) positions can be considered fixed in the binding motif with a significance $>0.99$.

| position | original base | frequency in input | $p$-value <br> prob(at least 41/42 in input) |
| :---: | :---: | :---: | :---: |
| 19,23 | C | 0.734 | $<0.0001$ |
| 24 | T | 0.815 | 0.0020 |

Table S13. Significance of semi-conserved residues in the 102 min binding loop.
Determining the requirements for the flexible positions (dark blue - positions 11, 18, and 22) requires the calculation of 'at most' and 'at least' binomial probabilities for each base. In each case, the frequencies imply a preference, although in most cases there are no statistically significant requirements. For example, for position 22, the observed number of Cs is higher than would be expected, given the starting ratios, but only barely significant ( $\sim 0.95$ ). The preferences indicated in Table S14 were employed as the position requirements for the binding motif in the motif probability calculations below.

| position | base | frequency in input | k (\# in output) | $p$-value |  | preference |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | Prob(at least $\mathrm{k} / 42$ ) in input | Prob(at most k/42) in input |  |
| 11 | A | 0.070 | 0 | 1 | 0.0475 | not A |
|  | C | 0.734 | 29 | 0.7945 | 0.3140 |  |
|  | G | 0.111 | 5 | 0.5056 | 0.6788 | C, G, or T all acceptable |
|  | T | 0.086 | 8 | 0.0250 | 0.9916 |  |
| 18 | A | 0.801 | 23 | >0.9999 | 0.0002 | dislikes A <br> C or G acceptable prefers T |
|  | C | 0.056 | 4 | 0.2073 | 0.9159 |  |
|  | G | 0.092 | 4 | 0.5480 | 0.6569 |  |
|  | T | 0.052 | 11 | <0.0001 | > 0.9999 |  |
| 22 | A | 0.052 | 0 | 1 | 0.1062 | C or T acceptable |
|  | C | 0.064 | 5 | 0.1288 | 0.9503 |  |
|  | G | 0.070 | 0 | 1 | 0.0475 |  |
|  | T | 0.815 | 37 | 0.1854 | 0.9097 |  |

Table S14. Base preferences of flexible residues.
Reselection identifies only one position (18) that is not ideal in the starting sequence. Because the original clone showed activity, however, and all other bases at this position survived the reselection at least as well as the original base, the requirement at this position is 'any base.'

Taken together, the IgE 102 min reselection results indicate that the binding motif isolated in the IgE selection is a loop with the sequence indicated in Table S15 flanked by a stem with at least seven out of eight base pairs. The likelihood of this motif occurring in each library is discussed on the following pages.

| position: | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| original | T | T | C | A | T | C | C | G | T | A | C | C | T | T | C | T | A | G | T | G | G |
| consensus | T | T | T | G | A | T | C | C | G | T | C | C |  |  |  |  |  |  |  |  |  |
| G | C | C | T | C | or | C | T | A | G | T | G | G |  |  |  |  |  |  |  |  |  |

Table S15. IgE 102min binding motif loop consensus sequence.

## IgE Binding Motif Probability Calculation

The probability of the above motif occurring in each library can be calculated as: (loop probability x stem probability), summed for all frames. Because every 37 base frame in $\mathrm{N}_{60}$ is the same as every other, the calculation for motif probability for $\mathrm{N}_{60}$ can be done once and multiplied by 24 to indicate that it can occur in any register. However, every register along the $\mathrm{R}^{*} \mathrm{Y}^{*}$ pattern is different, and the motif probability must be calculated separately for each.

## IgE Motif Loop Probability

The loop motif probability will be the product of the likelihoods of the required base(s) occurring at each position along the motif. The individual position probabilities reflect the frequencies of the bases in each mix in the starting $\mathrm{N}_{60}$ or $\mathrm{R}^{*} \mathrm{Y}^{*}$ libraries, based on sequencing (Table 1 in the main text; the relevant percentages are reproduced in Table S16).

| library | mix | A | C | G | T |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{N}_{60}$ | N | 27.2 | 23.4 | 26.6 | 22.8 |
| $\mathrm{R}^{*} \mathrm{Y}^{*}$ | N | 30.9 | 23.0 | 18.1 | 28.1 |
|  | $\mathrm{R}^{*}$ | 45.8 | 3.5 | 47.9 | 2.8 |
|  | $\mathrm{Y}^{*}$ | 2.7 | 48.8 | 3.0 | 45.6 |

Table S16. Base ratios at each position in the $\mathrm{N}_{60}$ and $\mathrm{R} * \mathrm{Y}^{*}$ libraries.
The loop probability was determined for every frame in both the $\mathrm{N}_{60}$ and $\mathrm{R} * \mathrm{Y} *$ libraries, using a computer program to assign a value at each bulge/loop position based on the base ratios in the appropriate position in the pattern. These values were then multiplied to determine the overall probability of the motif occurring in each frame (Table S17). In addition, the eight base pairs flanking the loop motif for each frame were qualitatively classified in order to rank the most likely frames (Table S17).

| frame | $\begin{aligned} & \mathrm{N}_{60} \text { loop } \\ & \text { probability } \end{aligned}$ | R* ${ }^{*}$ * loop probability | $\mathrm{R} * \mathrm{Y} *$ stem fit | $\begin{gathered} \mathrm{R}^{*} \mathrm{Y}^{*} \\ \text { likelihood } \\ \text { rank } \end{gathered}$ | RY loop mismatch |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $2.80 \times 10^{-12}$ | $1.92 \times 10^{-16}$ | 6 on; 2-N |  | 7 off |
| 2 | $2.80 \times 10^{-12}$ | $6.05 \times 10^{-14}$ | 4 on; 4-N | 3 | 5 off |
| 3 | $2.80 \times 10^{-12}$ | $6.21 \times 10^{-19}$ | 2 on; 6-N |  | 9 off |
| 4 | $2.80 \times 10^{-12}$ | $8.48 \times 10^{-15}$ | 1 on ; 7-N |  | 6 off |
| 5 | $2.80 \times 10^{-12}$ | $8.14 \times 10^{-20}$ | 2 on; 4-N; $2 \mathrm{~N}-\mathrm{N}$ |  | 10 off |
| 6 | $2.80 \times 10^{-12}$ | $1.19 \times 10^{-15}$ | 4 on; $4 \mathrm{~N}-\mathrm{N}$ |  | 7 off |
| 7 | $2.80 \times 10^{-12}$ | $2.02 \times 10^{-19}$ | 2 on; 4-N; $2 \mathrm{~N}-\mathrm{N}$ |  | 10 off |
| 8 | $2.80 \times 10^{-12}$ | $3.39 \times 10^{-17}$ | 1 on; 7-N |  | 8 off |
| 9 | $2.80 \times 10^{-12}$ | $3.87 \times 10^{-17}$ | 2 on; 6-N |  | 7 off |
| 10 | $2.80 \times 10^{-12}$ | $6.34 \times 10^{-16}$ | 4 on; 4-N |  | 6 off |
| 11 | $2.80 \times 10^{-12}$ | $1.83 \times 10^{-16}$ | 6 on; 2-N |  | 6 off |
| 12 | $2.80 \times 10^{-12}$ | $7.16 \times 10^{-17}$ | 7 on; 1-N |  | 7 off |
| 13 | $2.80 \times 10^{-12}$ | $4.34 \times 10^{-14}$ | 8 on | 2 | 5 off |
| 14 | $2.80 \times 10^{-12}$ | $7.22 \times 10^{-18}$ | 7 on; 1-N |  | 8 off |
| 15 | $2.80 \times 10^{-12}$ | $1.06 \times 10^{-11}$ | 6 on; 2-N | 1 | 3 off |
| 16 | $2.80 \times 10^{-12}$ | $4.07 \times 10^{-19}$ | 4 on; 4-N |  | 9 off |
| 17 | $2.80 \times 10^{-12}$ | $5.25 \times 10^{-14}$ | 3 on; 5-N | 4 | 5 off |
| 18 | $2.80 \times 10^{-12}$ | $5.03 \times 10^{-20}$ | 2 on; 6-N |  | 10 off |
| 19 | $2.80 \times 10^{-12}$ | $1.05 \times 10^{-14}$ | 4 on; 2-N; $2 \mathrm{~N}-\mathrm{N}$ | 4 | 6 off |
| 20 | $2.80 \times 10^{-12}$ | $9.29 \times 10^{-20}$ | 4 on; 2-N; $2 \mathrm{~N}-\mathrm{N}$ |  | 10 off |
| 21 | $2.80 \times 10^{-12}$ | $6.04 \times 10^{-16}$ | 2 on; 6-N |  | 7 off |
| 22 | $2.80 \times 10^{-12}$ | $4.50 \times 10^{-19}$ | 3 on ; 5-N |  | 9 off |
| 23 | $2.80 \times 10^{-12}$ | $9.04 \times 10^{-15}$ | 4 on; 4-N |  | 5 off |
| 24 | $2.80 \times 10^{-12}$ | $1.28 \times 10^{-17}$ | 6 on; 2-N |  | 7 off |

Table S17. Loop occurrence probabilities for every frame in the $\mathrm{N}_{60}$ and $\mathrm{R}^{*} \mathrm{Y}^{*}$ libraries. In addition, stem fits are described to identify the most likely frames.

Of all of the registers along the $\mathrm{R} * \mathrm{Y}^{*}$ pattern, frame 15 , in which the motif was observed in the original selection, fits it the best:

XXXXXXXX-TTCATCCGTACCTTCTAGTGG-XXXXXXXX
RYRYRYRY-NNNRYRYRYRYRYNNNNRYRY-RYRYRYNN
RYRYRYRY-NNNRYRYRYRYRYNNNNRYRY-RYRYRYNN
3 loop motif bases off pattern, 6 stem base pairs on pattern/2 stem base pairs with N
The next most likely frame, 13 , which lies two positions to the left along the pattern, is:

## XXXXXXXX-ITCATCCGTACCTICTAGTGG-XXXXXXXX RYRYRYRY-RYNNNRYRYRYRYRYNNNNRY-RYRYRYRY

5 loop motif bases off pattern, 8 stem base pairs on pattern
The stem fits this register better, because all eight base pairs are between an $\mathrm{R}^{*}$ and a $\mathrm{Y}^{*}$ position, but the loop fits significantly worse, with five off-pattern positions, instead of three.

Comparison of the loop motif to the other 22 registers in $\mathrm{R} * \mathrm{Y}^{*}$ reveals that every other frame will fit the loop motif less well than these two frames (greater than or equal to five loop motif bases off pattern, less than eight stem base pairs on pattern), and the motif likelihoods in those registers will not be significant in comparison to those of the two most likely frames. Because every frame in the patterned library contains at least three off-pattern positions, this binding motif is not found in the pure RY library.

## IgE Motif Stem Probability

Having identified the most likely frames in which the motif could appear and calculated the loop motif probability for each, the stem probabilities were calculated. These calculations were performed for each frame individually.

For the $\mathrm{N}_{60}$ library:
Likelihood of any two ' N ' making a pair

| AT | $0.272 \times 0.228=0.0620$ |
| :---: | :---: |
| TA | $0.228 \times 0.272=0.0620$ |
| CG | $0.234 \times 0.266=0.0622$ |
| GC | $0.266 \times 0.234=0.0622$ |
| GT | $0.266 \times 0.228=0.0606$ |
| TG | $0.266 \times 0.228=0.0606$ |
| Total | 0.3696 |
|  | 0.6304 |

Likelihood of any two ' N ' not making a pair 0.6304

Therefore, the probability of at least seven out of eight base pairs in a stem in the $\mathrm{N}_{60}$ library
$\operatorname{Prob}(7 / 8$ base stem $)=\operatorname{Prob}(3$ fixed base pairs $) \times \operatorname{Prob}(4 / 5$ variable base pairs $)=$ $\mathrm{P}(\text { pair })^{3} \times\left[5 \times P(\sim\right.$ pair $\left.) \times \mathrm{P}(\text { pair })^{4}\right]=$ $(0.3696)^{3} \times\left[5(0.6304)(0.3696)^{4}\right]=0.00297$
$\operatorname{Prob}(8$ base stem $)=$
$\mathrm{P}(\text { pair })^{8}=(0.3696)^{8}=0.00035$
$\operatorname{Prob}($ stem $)=0.00297+0.00035=\mathbf{0 . 0 0 3 3 2}$
For the $\mathrm{R} * \mathrm{Y}^{*}$ library:
Likelihood of any $\mathrm{R}^{*}$ and $\mathrm{Y}^{*}$ making a pair AT $0.458 \times 0.456=0.2088$
GC $\quad 0.479 \times 0.488=0.2338$
GT $\quad 0.479 \times 0.456=0.2184$
TA $\quad 0.028 \times 0.027=0.0008$

| CG | $0.035 \times 0.030$ | $=0.0011$ |
| :--- | ---: | :--- |
| TG | $0.028 \times 0.030$ | $=0.0008$ |
| Total | 0.6781 |  |
|  | 0.3219 |  |
|  |  |  |
|  | 0.3936 |  |
|  | 0.6064 |  |
|  | 0.3346 |  |
|  | 0.6654 |  |

Therefore the probability of at least seven out of eight base pairs in a stem in the $\mathrm{R} * \mathrm{Y} *$ library is:
In the observed frame:
$\operatorname{Prob}(8 \mathrm{bp}$ stem $)$
$\mathrm{P}\left(\mathrm{R}^{*} \mathrm{~N}\right) \times \mathrm{P}\left(\mathrm{Y}^{*} \mathrm{~N}\right) \times \mathrm{P}\left(\mathrm{R}^{*} \mathrm{Y}^{*}\right)^{6}=0.3936 \times 0.3346 \times(0.6781)^{6}=0.0128$
$\operatorname{Prob}(7 / 8 \mathrm{bp}$ stem $)=\operatorname{Prob}(3$ fixed base pairs $) \mathrm{x} \operatorname{Prob}(4 / 5$ variable base pairs $)$
$\left[\mathrm{P}(\mathrm{R} * \mathrm{~N}) \mathrm{xP}\left(\mathrm{R}^{*} \mathrm{Y}^{*}\right)^{2}\right] \mathrm{x}\left[4 \mathrm{xP}\left(\sim \mathrm{R} * \mathrm{Y}^{*}\right) \mathrm{x} \mathrm{P}\left(\mathrm{R} * \mathrm{Y}^{*}\right)^{3} \mathrm{x} \mathrm{P}\left(\mathrm{Y}^{*} \mathrm{~N}\right)+\mathrm{P}\left(\mathrm{R}^{*} \mathrm{Y}^{*}\right)^{4} \mathrm{x} \mathrm{P}\left(\sim \mathrm{Y}^{*} \mathrm{~N}\right)\right]$
$\left[(0.3936)(0.6781)^{2}\right] \times\left[4(0.3219)(0.6781)^{3}(0.3346)+(0.6781)^{4}(0.6654)\right]=0.0498$
$\operatorname{Prob}($ stem $)=0.0128+0.0498=\mathbf{0 . 0 6 2 6}$
In the second most likely frame:
$\operatorname{Prob}(8$ bp stem $)=P\left(\mathrm{R} * \mathrm{Y}^{*}\right)^{8}=$ $(0.6781)^{8}=0.0447$
$\operatorname{Prob}(7 \mathrm{bp}$ stem $)=\operatorname{Prob}(3$ fixed base pairs $) \times \operatorname{Prob}(4 / 5$ variable base pairs $)=$ $\mathrm{P}\left(\mathrm{R}^{*} \mathrm{Y}^{*}\right)^{3} \times\left[5 \mathrm{xP}\left(\sim \mathrm{R} * \mathrm{Y}^{*}\right) \mathrm{x} \mathrm{P}\left(\mathrm{R}^{*} \mathrm{Y}^{*}\right)^{4}\right)=$ $(0.6781)^{3} \times 5(0.3219)(0.6781)^{4}=0.1061$
$\operatorname{Prob}($ stem $)=0.0447+0.1061=\mathbf{0 . 1 5 0 8}$

## IgE Binding Motif Total Probability

Based on these values, the overall probability of the full binding motif occurring in the library is calculated in Table S18.

| library | frame | loop motif <br> probability | stem <br> probability | registers | total <br> probability |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{N}_{60}$ | Any | $2.80 \times 10^{-12}$ | 0.00297 | 24 | $2.0 \times 10^{-13}$ |
| $\mathrm{R}^{*} \mathrm{Y}^{*}$ | Current | $1.06 \times 10^{-11}$ | 0.0626 | 1 | $6.6 \times 10^{-13}$ |
| $\mathrm{R}^{*} \mathrm{Y}^{*}$ | Second | $4.34 \times 10^{-14}$ | 0.1508 | 1 | $6.5 \times 10^{-15}$ |

Table S18. IgE-binding motif likelihood in each library
Therefore, the likelihood of the full motif (21 base loop surrounded by a stem with at least seven out of eight base pairs) occurring in the $\mathrm{N}_{60}$ library is $2.0 \times 10^{-13}$, while the likelihood of it occurring in the $\mathrm{R} * \mathrm{Y}^{*}$ library is approximately $6.7 \times 10^{-13}$. The motif is $\sim 3.4$-fold more likely in the $\mathrm{R} * \mathrm{Y}^{*}$ library than in the standard $\mathrm{N}_{60}$ library.

## Katilius/Woodbury Motif Comparison

D17.4
TTTATCCGTCCCTCCTAGTGG
D17 (original consensus)
102 (original)

## TTYATCCGTYHCTCYYAGTGG <br> TTCATCCGTACCTTCTAGTGG

102 (reselection)
D17.4 (microarray)

TTBATCCGTNCCTYCTAGTGG
TTBATCCGTHYCTYYYAGTGG

The D17.4 binding motif as determined by Katilius et al using a microarray screen is very similar to the 102 min motif determined here. They assigned position 18 (102minA numbering) as 'not $G$ ' instead of ' N ' and assigned all of the light blue semi-conserved positions as ' Y ' instead of ' C .' In general, the two techniques identified the same positions as fixed, conserved positions, but differed slightly in the assignment of the semi-conserved or variable positions.

## VEGF Binding Motif

Alignment of the variable regions of the 16 unique sequences from round 10 of the VEGF selection revealed that twelve share a common sequence (GTCCGGAATGG-N ${ }_{(0-4)}$-GTGC). In contrast with the streptavidin and IgE cases, however, this consensus sequence was not predicted by OMP to occur in a common context, and variations from the consensus within the 16 unique clones do not correlate with changes in VEGF binding affinity. The motif was therefore considered not sufficiently conserved to enable rigorous probability calculations.

None of the VEGF clones selected here contained the previously published VEGF DNA aptamers: ATACCAGTCTATTCAATTGGGCCCGTCCGTATGGTGGGTGTGCTGGCCAGATAGTATGTGCAATCA ${ }^{3}$ or TGTGGGGGTGGACGGGCCGGGTAGA ${ }^{4}$

## Effects of Divalent Cation Concentration on Aptamer Function and Predicted Structure



Figure S11. Binding of the best $\mathrm{R}^{*} \mathrm{Y}^{*} \operatorname{IgE}$ aptamer and the best $\mathrm{N}_{60}$ IgE aptamer to immobilized $\operatorname{IgE}$ is comparable at 1 mM versus 10 mM MgCl 2 . No significant binding was observed in the presence of 50 mM MgCl 2 . Clones were bound to IgE beads as described in the main text in PBS supplemented with 1,10 , or 50 mM MgCl 2 .

|  | energy of folding (average $\pm$ standard deviation in kcal/mol) |  |
| :---: | :---: | :---: |
| library | 1 mM Mg | 10 mM Mg |
| $\mathrm{N}_{60}$ | $-16.2 \pm 3.3$ | $-18.3 \pm 3.3$ |
| $\mathrm{R}^{*} \mathrm{Y}^{*}$ | $-20.6 \pm 3.6$ | $-22.4 \pm 4.0$ |
| $\Delta \Delta \mathrm{G}$ | -4.4 | -4.1 |
| Z-score | 1.33 | 1.24 |

Table S19. Predicted folding energies using OMP of $\mathrm{N}_{60}$ and $\mathrm{R} * \mathrm{Y}^{*}$ libraries in 1 mM versus 10 mM $\mathrm{MgCl}_{2}$. Z -score is defined as ( $\Delta \Delta \mathrm{G} /$ standard deviation).

|  | 1 mM Mg |  |  | 10 mM Mg |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{N}_{60}$ | $\mathrm{R}^{*} \mathrm{Y}^{*}$ | ratio | $\mathrm{N}_{60}$ | $\mathrm{R}^{*} \mathrm{Y}^{*}$ | ratio |
| top 5\% $\mathrm{N}_{60}$ | $5 \%$ | $34 \%$ | 6.8 | $5 \%$ | $31 \%$ | 6.2 |
| I 102 | $25 \%$ | $69 \%$ | 2.8 | $22 \%$ | $66 \%$ | 3.0 |
| Top 3 VEGF | $8 \%$ | $41 \%$ | 5.1 | $9 \%$ | $43 \%$ | 4.8 |

Table S20. Percentage of $\mathrm{N}_{60}$ and $\mathrm{R}^{*} \mathrm{Y}^{*}$ libraries that are predicted to be at least as structured as aptamers in 1 mM versus 10 mM MgCl .

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