

Supporting Information:

Interlayer Coupling in Twisted WSe₂/WS₂ Bilayer Heterostructures Revealed by Optical Spectroscopy

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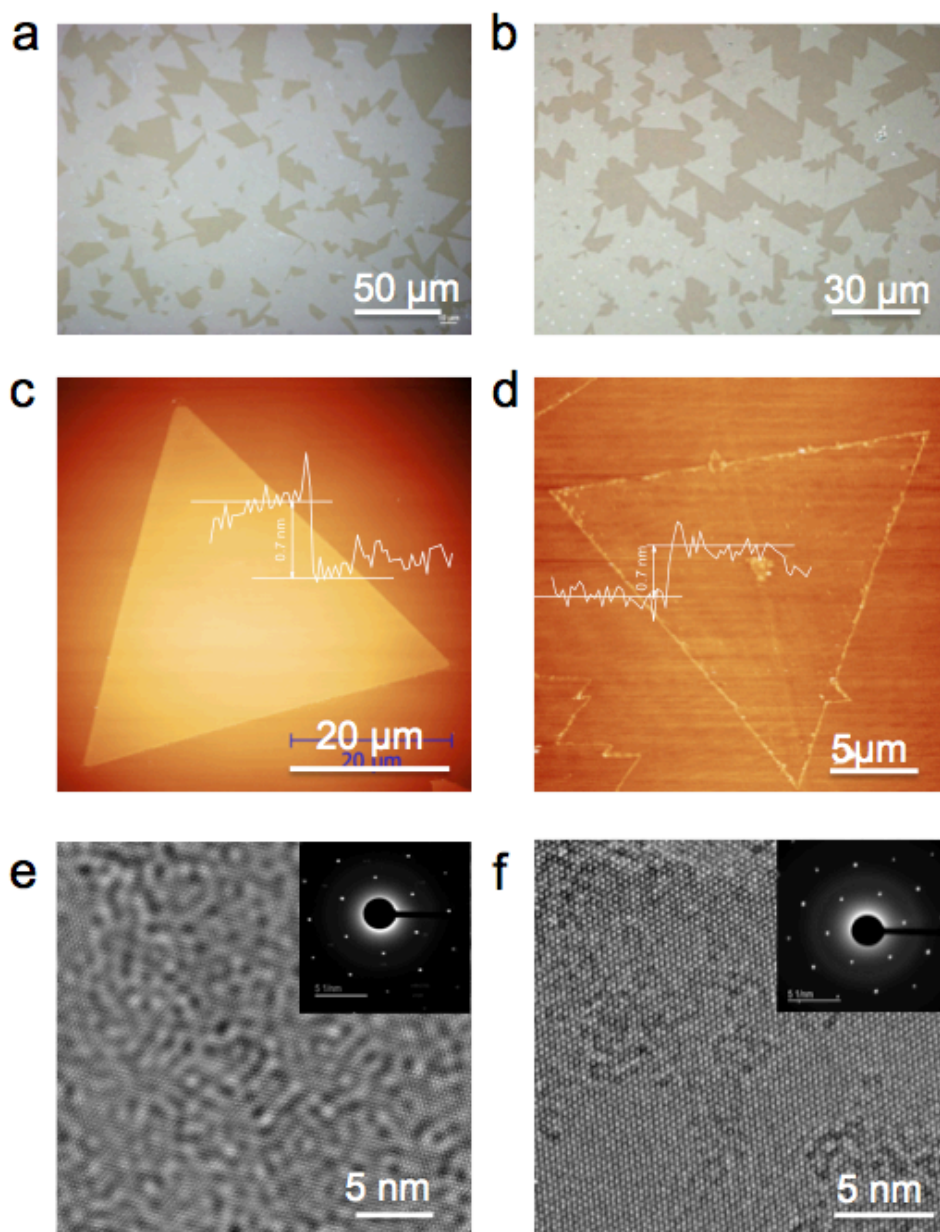


Figure S1. Structural analysis of WS₂ and WSe₂ 2D flakes directly grown on sapphire substrate by CVD. (a) and (b) optical microscope images of WS₂ and WSe₂ flakes. (c) and (d) AFM images and the edge profiles of ML WS₂ and WSe₂ triangular flake. (e) and (f) HRTEM images taken from ML WS₂ and WSe₂ flakes. Insets are the corresponding selected area electron diffraction (SEAD) patterns, respectively.

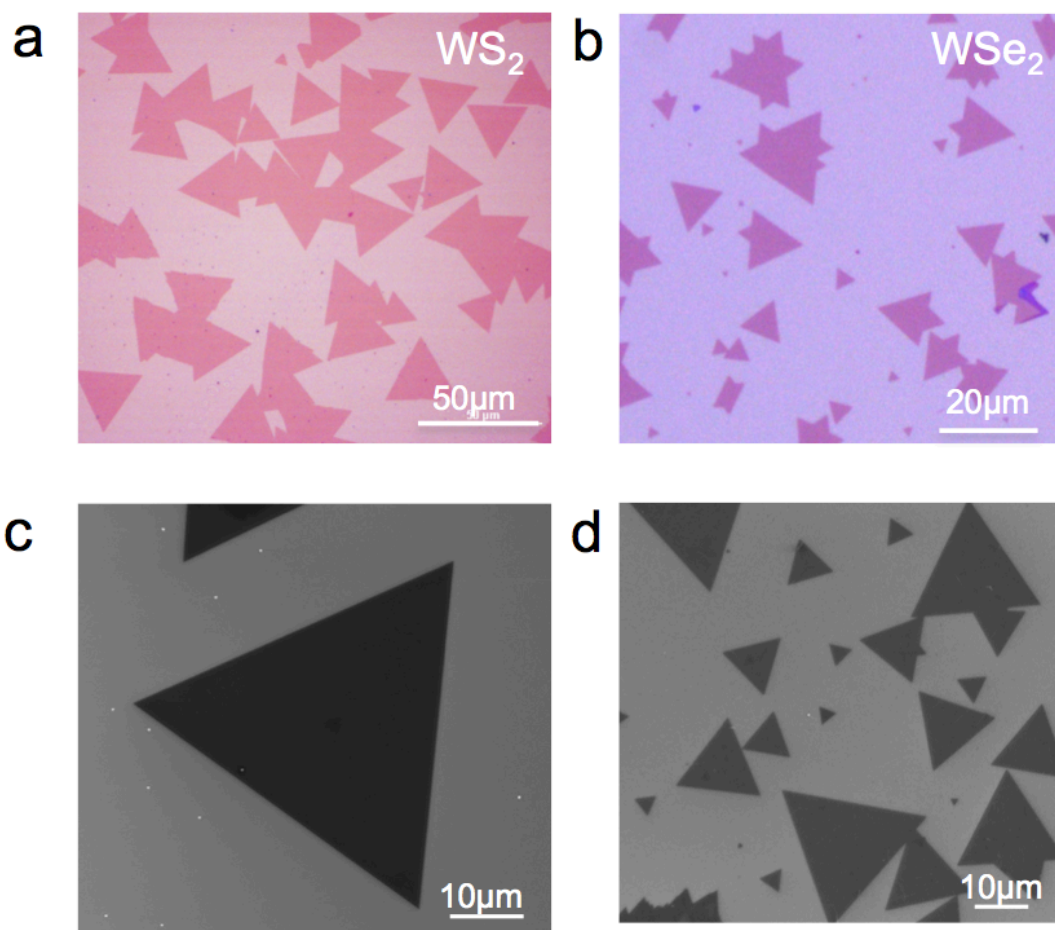


Figure S2 Size and shapes of WSe₂ and WS₂ 2D flakes directly grown on SiO₂/Si substrate by CVD. (a) and (b) optical microscope images of WS₂ and WSe₂ flakes. (c) and (d) SEM images of ML WS₂ and WSe₂ triangular flakes.

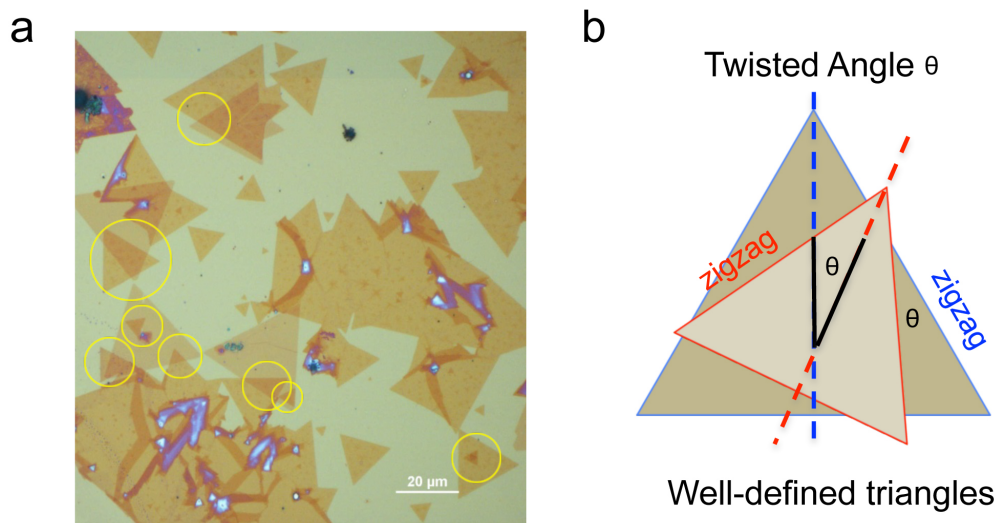


Figure S3. (a) Optical microscope image of stamped WSe₂/WS₂ BLs on SiO₂/Si substrate showing 8 different twist angles. (b) Schematic used to define the twist angles between the two layers. The perfect symmetry of as-transferred flakes before and after annealing allows us to precisely determine the twist angles using optical images.

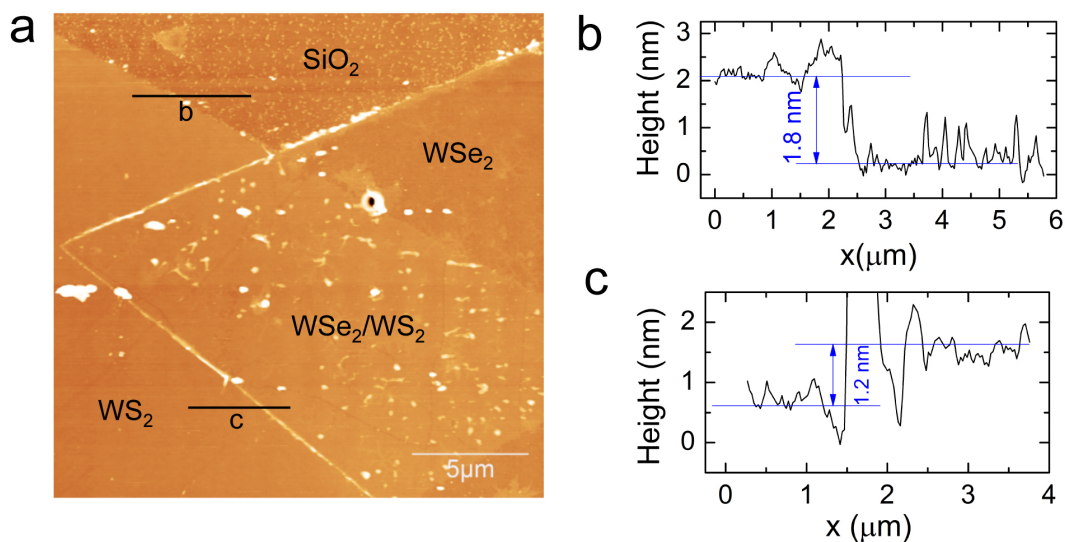


Figure S4. Influence of annealing on the distance between layers. (a) AFM image of a WSe₂/WS₂ BL before annealing. (b) and (c) Height profiles taken at the position of the black lines in (a). Without annealing, the measured height profiles of ML WS₂ on SiO₂ substrate and ML WSe₂ are 1.8 nm and 1.2 nm, respectively, which are larger than the thickness (~ 0.8 nm) of ML WS₂ measured after annealing. This indicates that the majority of any trapped water vapor or the polymer residue left on the sample is removed by annealing in Ar.

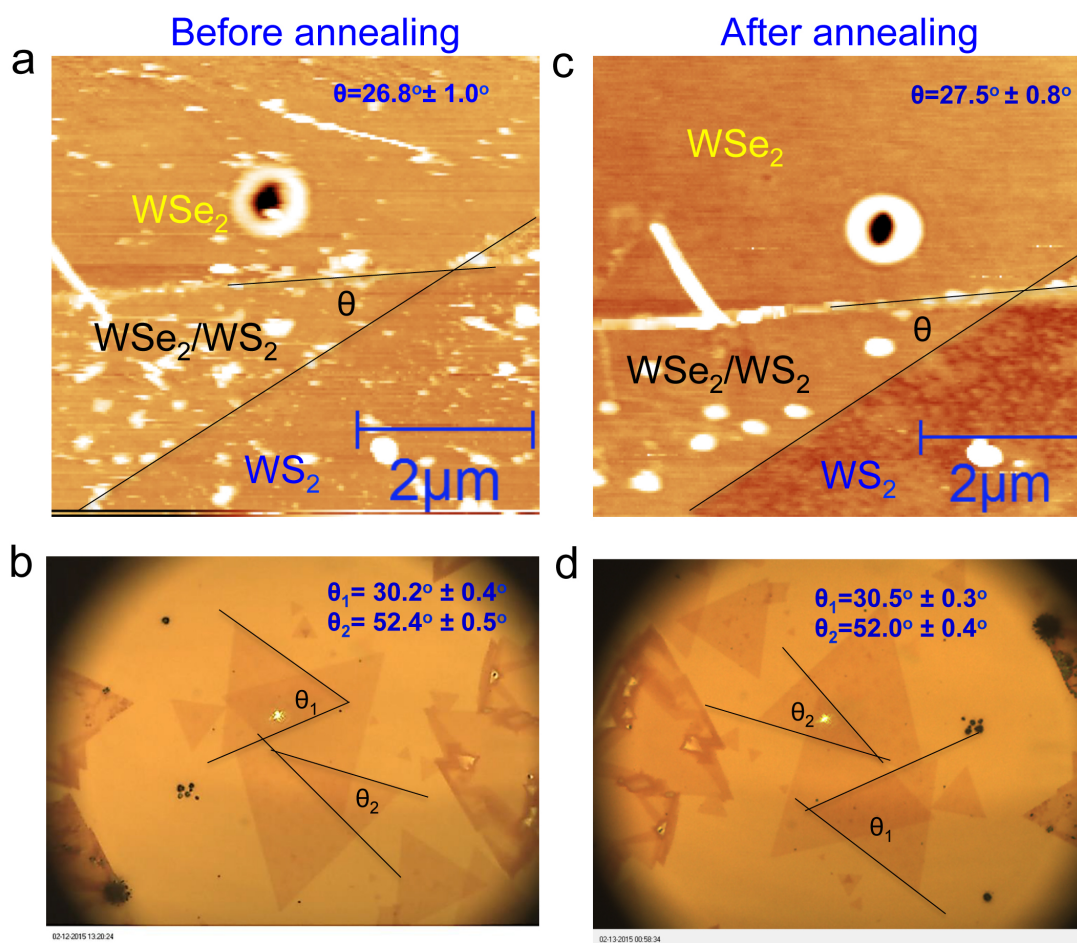


Figure S5. Influence of annealing on the twist angles. AFM images and optical microscope images of WSe_2/WS_2 bilayers before annealing ((a) and (b)) and after annealing ((c) and (d)). The twist angles change before and after annealing is within the experimental uncertainty of $\pm 0.5^\circ$.

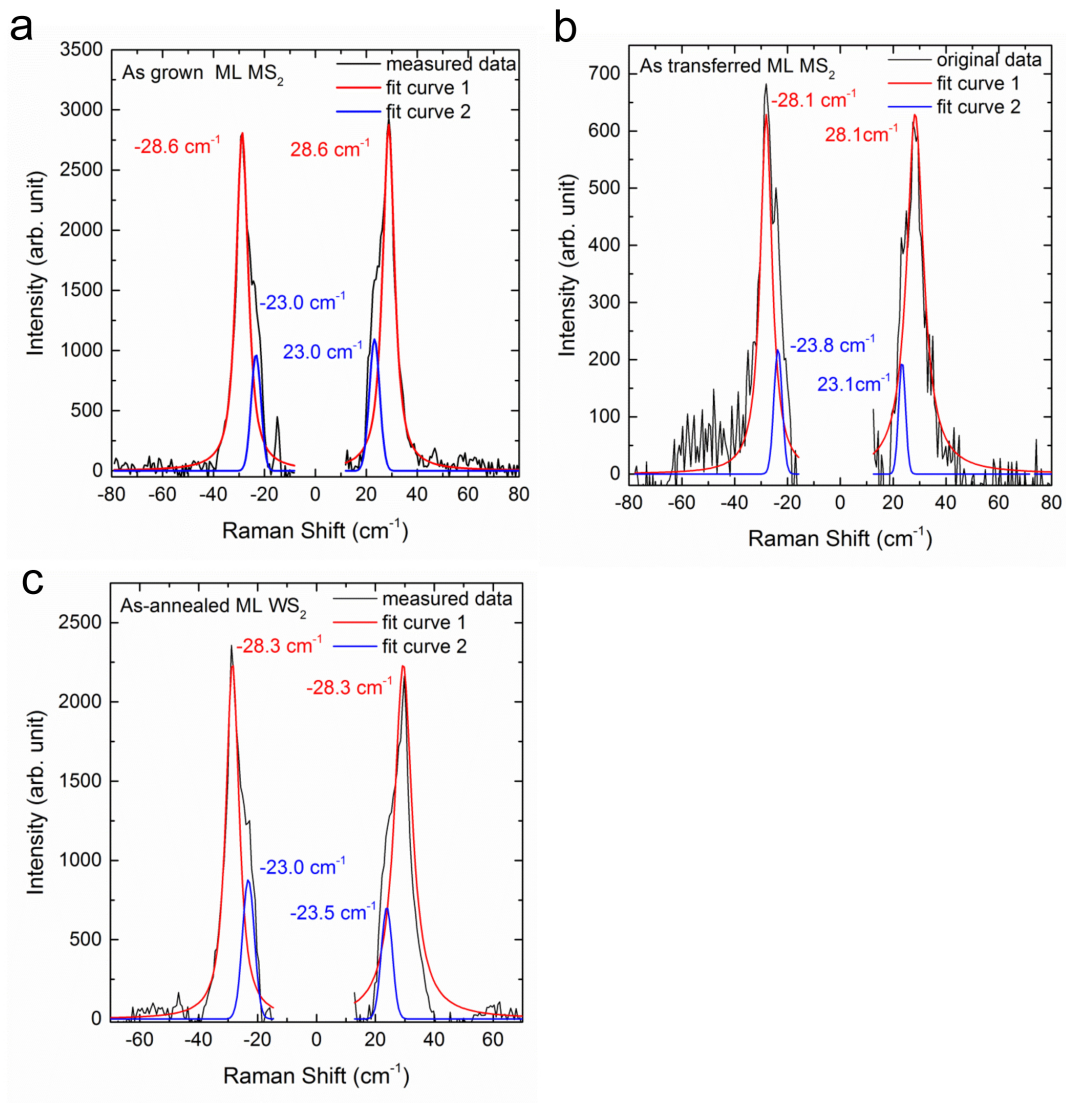


Figure S6. Low-frequency (LF) Raman spectra taken from ML WS_2 on SiO_2/Si substrates. (a) as-grown, (b) as-transferred, and (c) as-annealed. The black curve is the measured LF Raman spectrum after subtracting the background, which can be fitted by a main peak (in red) and a small peak (in blue).

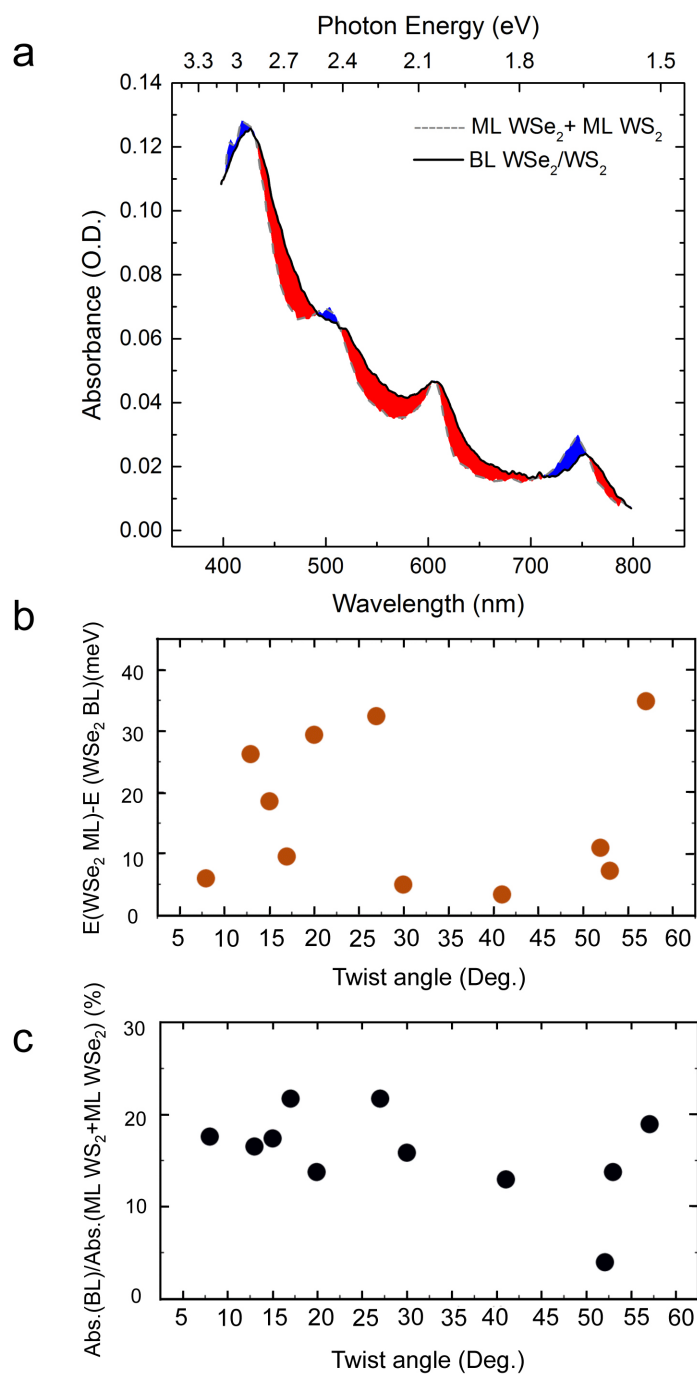


Figure S7. Absorption in WSe₂/WS₂ BL. (a) WSe₂/WS₂ BL shows ~10 % enhancement in absorbance range of 400 nm~800 nm, as indicated by the red shaded regions. (b) Statistical analysis of the redshifts of the WSe₂ exciton A band in BL relative to that in ML, $E(\text{WSe}_2 \text{ ML}) - E(\text{WSe}_2 \text{ BL})$. (c) Ratio of absorbances, $\text{Abs.}(\text{BL})/\text{Abs.}(\text{ML WS}_2 + \text{ML WSe}_2)$. Note that the absorbances were integrated from 570 nm (2.17 eV) to 800 nm (1.55 eV).

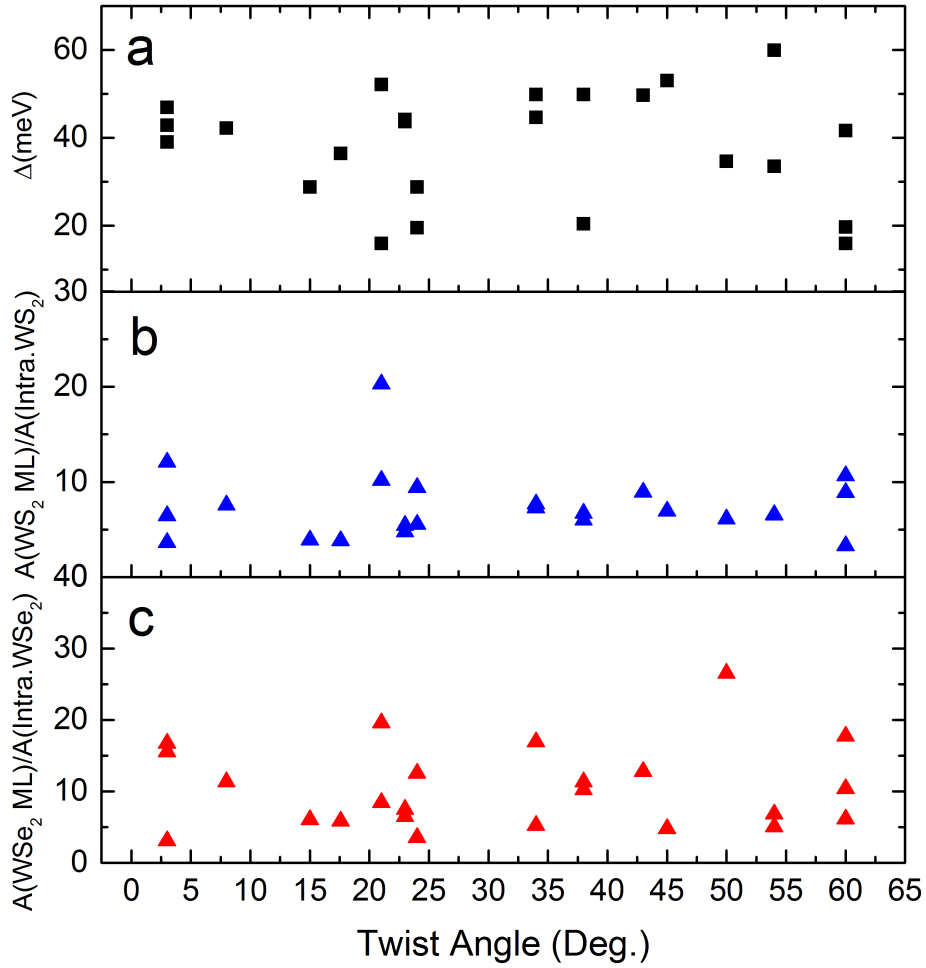


Figure S8. Statistical analysis of PL data for WSe₂/WS₂ BLs. (a) the redshift (Δ) of the WSe₂ exciton A band in BL relative to that in ML, $E(\text{WSe}_2 \text{ ML}) - E(\text{WSe}_2 \text{ BL})$, and the ratio of PL intensity: (b) $A(\text{WS}_2 \text{ ML})/A(\text{Intra.WS}_2)$ for WS₂ and (c) $A(\text{WSe}_2 \text{ ML})/A(\text{Intra.WSe}_2)$ for WSe₂, respectively. To determine the quenching magnitudes in PL intensity, we compared the integrated area under the spectra from 1.85 eV to 2.15 eV for WS₂ and from 1.5 eV to 1.78 eV for WSe₂. No clear trends of the redshift and the magnitudes of intralayer PL quenching with the twist angle were observed.

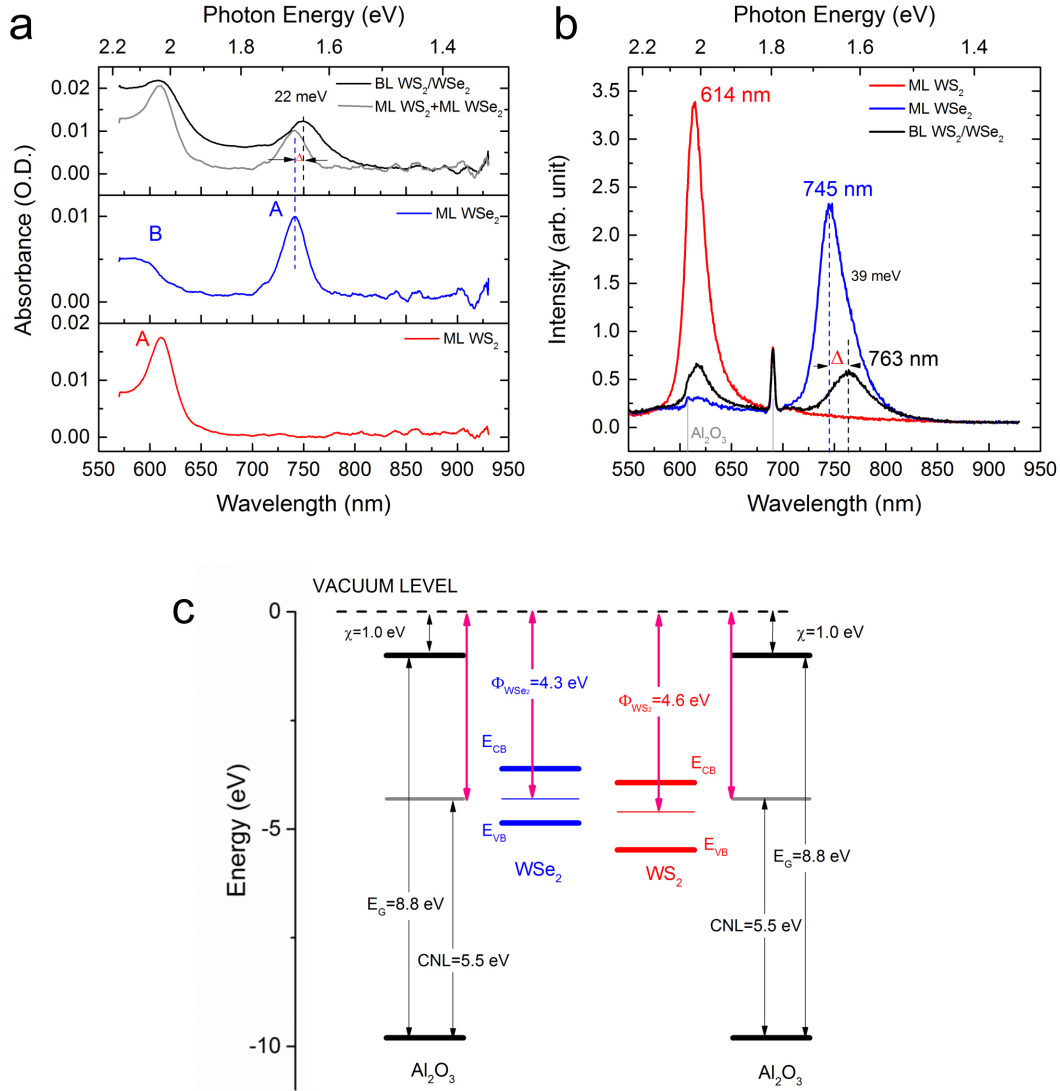


Figure S9. Light absorption and emission characteristics of WS_2/WSe_2 BLs on sapphire substrate and associated energy level diagram. (a) Absorption and (b) photoluminescence spectra taken from ML WSe_2 , ML WS_2 and WS_2/WSe_2 BLs on a sapphire substrate. (c) Schematic diagram of the energy level in $\text{Al}_2\text{O}_3/\text{WSe}_2/\text{WS}_2$ and $\text{Al}_2\text{O}_3/\text{WS}_2/\text{WSe}_2$ sandwich structures. For the work function of ML WSe_2 and ML WS_2 (Φ_{WSe_2} and Φ_{WS_2}), we use the values of 4.6 eV and 4.3 eV [Britnell, *et al.* Science, 340, 1311 (2013)]; for the bandgap of WSe_2 and WS_2 , we use the calculated data from the literature [Kang, *et al.* Appl. Phys. Lett, 102, 012111 (2013)]. The electron affinity (EA), band gap (E_g), and charge neutrality level (CNL) of Al_2O_3 , were adapted from the literature [Pecock, *et al.* J. Appl. Phys, 92, 4712 (2002)].

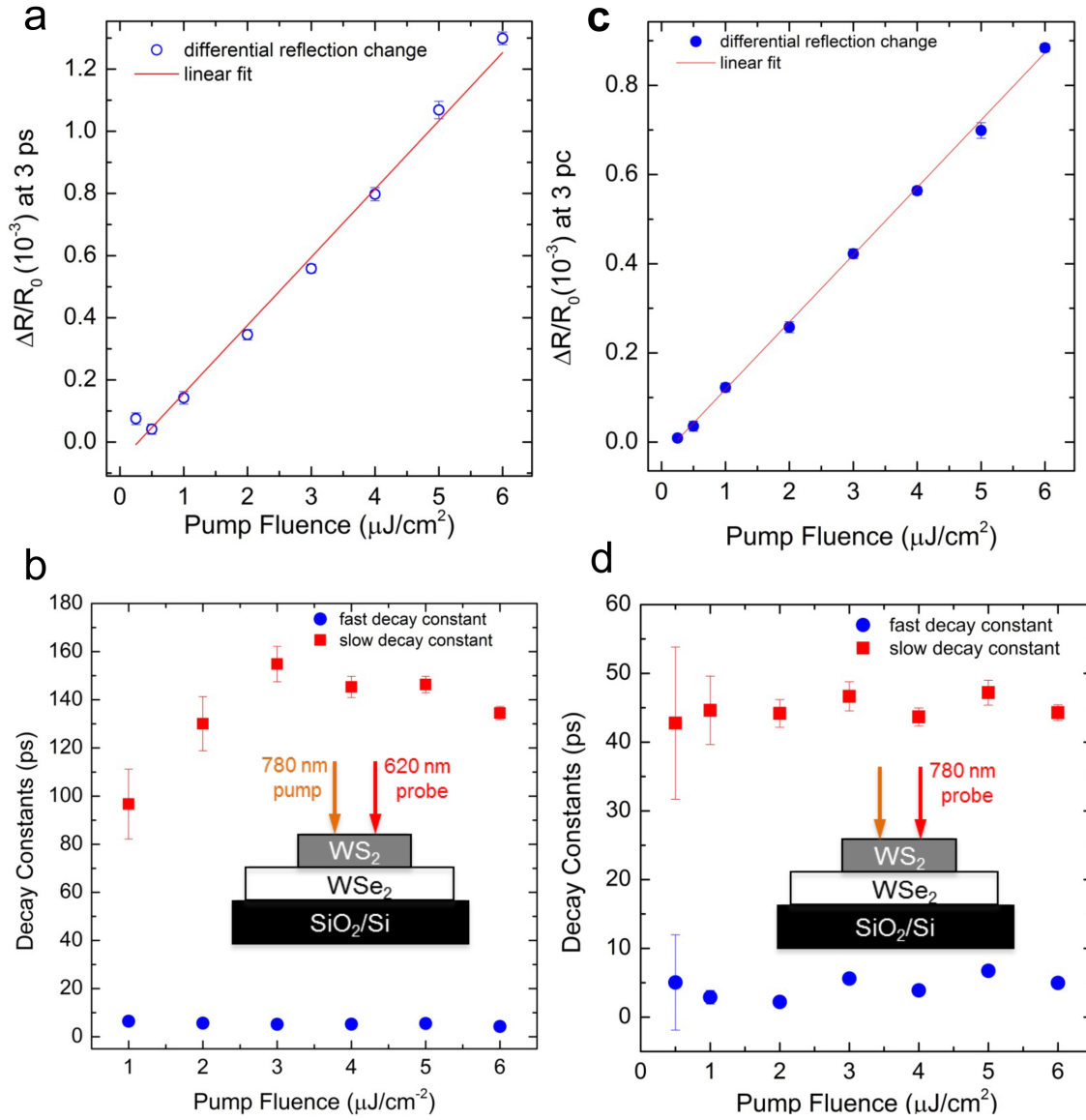


Figure S10. Pump-fluence-dependent differential reflectance and fitted decay time constants. (a) and (b) are collected using a 780 nm pump wavelength and a 620-nm probe pulse. (c) and (d) are collected with a 620 nm pump and a 780-nm probe pulse. Insets of (b) and (d) illustrate the corresponding pump-probe configurations.

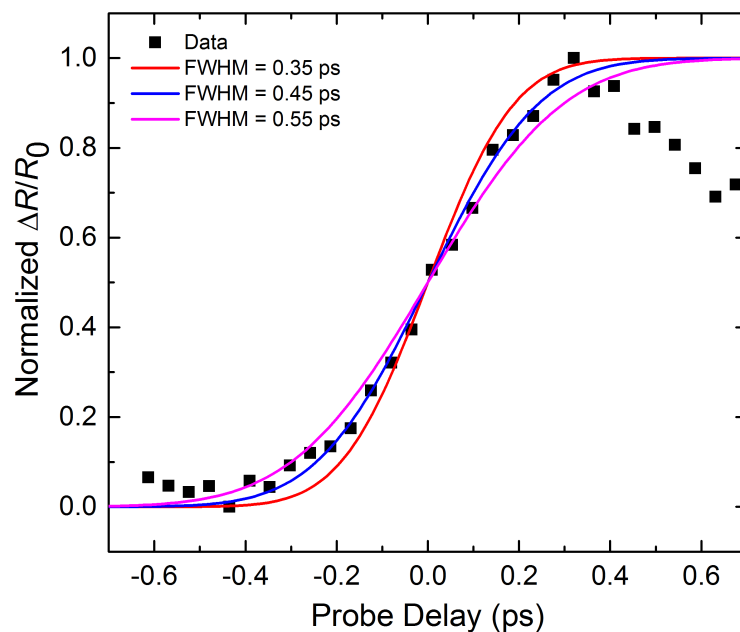


Figure S11. Instrument response determination for femtosecond transient absorption spectroscopy. Assuming that the response of the sample is instantaneous and the pump and probe pulses are infinitely narrow, $\Delta R/R_0$ should be a step function that jumps at zero delay (ignoring decay of the signal). Here the width of the cross correlation of the pump and probe pulses is determined to be ~ 450 fs. That translates to pulse widths of 0.32 ps for each pulse (FWHM intensity), using $0.45/1.414$. Since the sample response cannot be instantaneous, this is actually the upper limit of the pulse width.

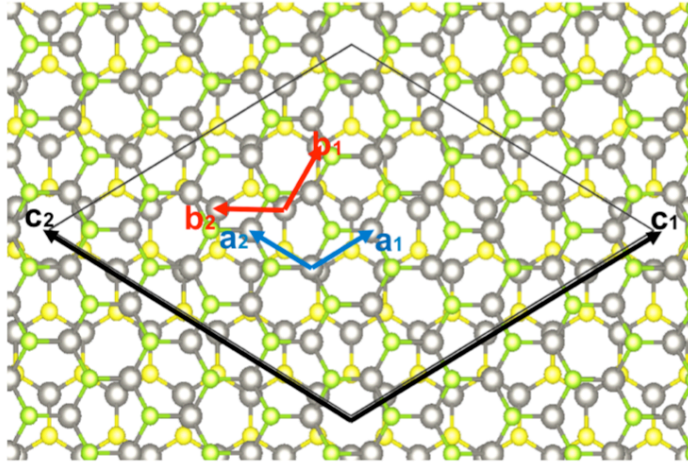


Figure S12. Schematics of a WSe₂/WS₂ supercell. WSe₂/WS₂ supercell is hexagonal with a primitive lattice vector $\vec{C} = n_1\vec{a}_1 + n_2\vec{a}_2 = (1 + \varepsilon)\theta(n_1\vec{b}_1 + n_2\vec{b}_2)$, where \vec{a}_1 and \vec{a}_2 are the lattice vectors of WSe₂, \vec{b}_1 and \vec{b}_2 are the lattice vectors of WS₂, and θ is the twist angle between WS₂ and WSe₂ layers.

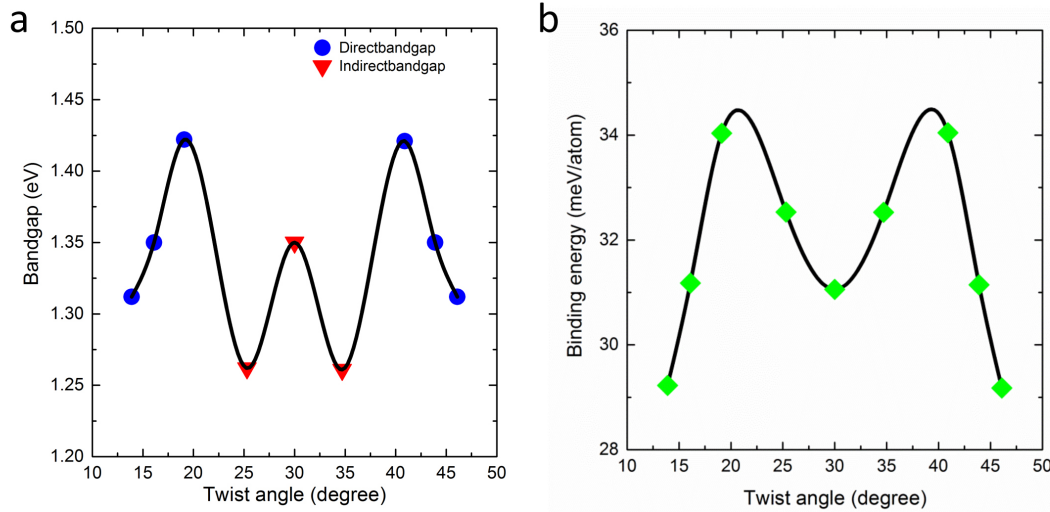


Figure S13. Band Structure calculations of WSe₂/WS₂ by PBE+vdW. (a) The DFT-calculated electronic band gap of a WSe₂/WS₂ heterojunction as a function of twist angle. (b) The DFT-calculated (including van de Waals interactions) binding energy of WSe₂/WS₂ heterojunction as a function of twist angle.

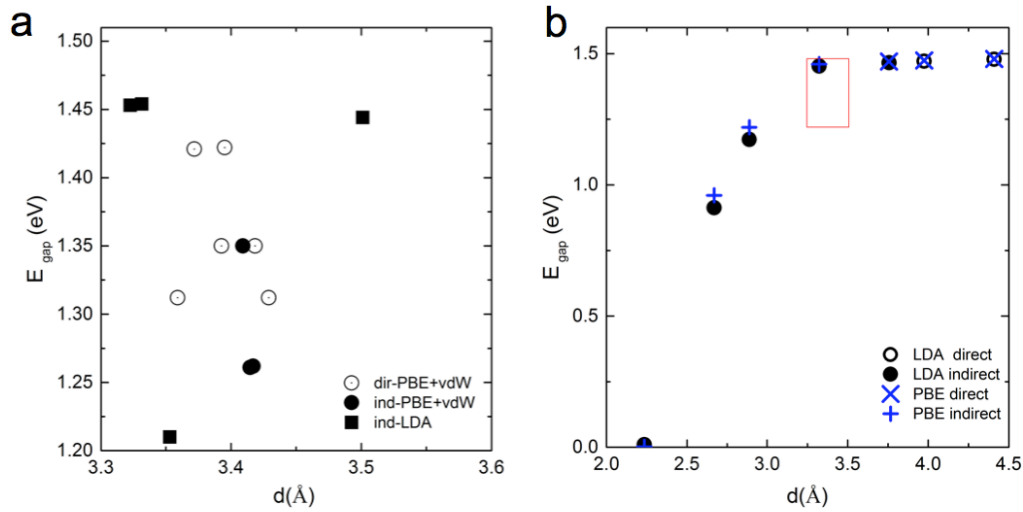


Figure S14 (a) Energy band gaps of structures optimized by either LDA or PBE+vdW functionals, where d is the optimized interlayer spacing of various twist angle structures considered in the study. Types of band gaps (indirect vs. direct) are indicated by the types of data points. (b) Energy band gaps of structures optimized by either LDA or PBE+vdW functionals. Types of band gaps (indirect vs. direct) are indicated by the types of data points.

Figure S14a presents energy gaps and their indirect/direct characteristics of structures fully optimized either by LDA or PBE+vdW. The plot compiles all the energy gaps obtained for the structures considered at various twist angles in terms of their interlayer spacing, d , optimized from the calculations. It clearly shows that direct-gap structures predicted by PBE+vdW are inconsistent with LDA predictions, that is, the PBE-predicted twist angles that indicate a direct band gap can be indirect using LDA and vice versa.

We reveal that interlayer spacing is the most prominent factor in determining energy gaps as well as their characteristics. For example, **Figure S14b** shows electronic energy gaps obtained for a BL structure at 19.1° twist angle for different interlayer spacing. Here the two layers were rigidly translated at different d without allowing a structural relaxation that is strongly affected by the choice of functionals. By this procedure we focus only on the effect of functionals in the electronic structures to draw a general conclusion on the correlation between interlayer distance and electronic structures. For both functionals, we find indirect to direct band gap transitions as interlayer distance increases. The non-

interacting regions clearly show direct band gaps, becoming indirect once the layers strongly interact with each other. However the exact transition point can be slightly different for different atomistic orientations between the layers. The region highlighted by red box is the range from Figure **S14a**, where the strength of the interlayer interaction lies in between non-interacting and strongly interacting. This is the region where the characteristics of the bands can be very easily changed depending on local orbital interactions. Here, the change in the local orbital interaction is so subtle that it is very difficult to deterministically predict direct-gap configurations. This finding is qualitatively consistent with the experimental data showing different PL band shifts even for the same twist angle. Moreover, depending on the experimental synthesis and processing conditions the interlayer distance may change slightly, which could introduce an excitonic peak if the layers are weakly coupled.