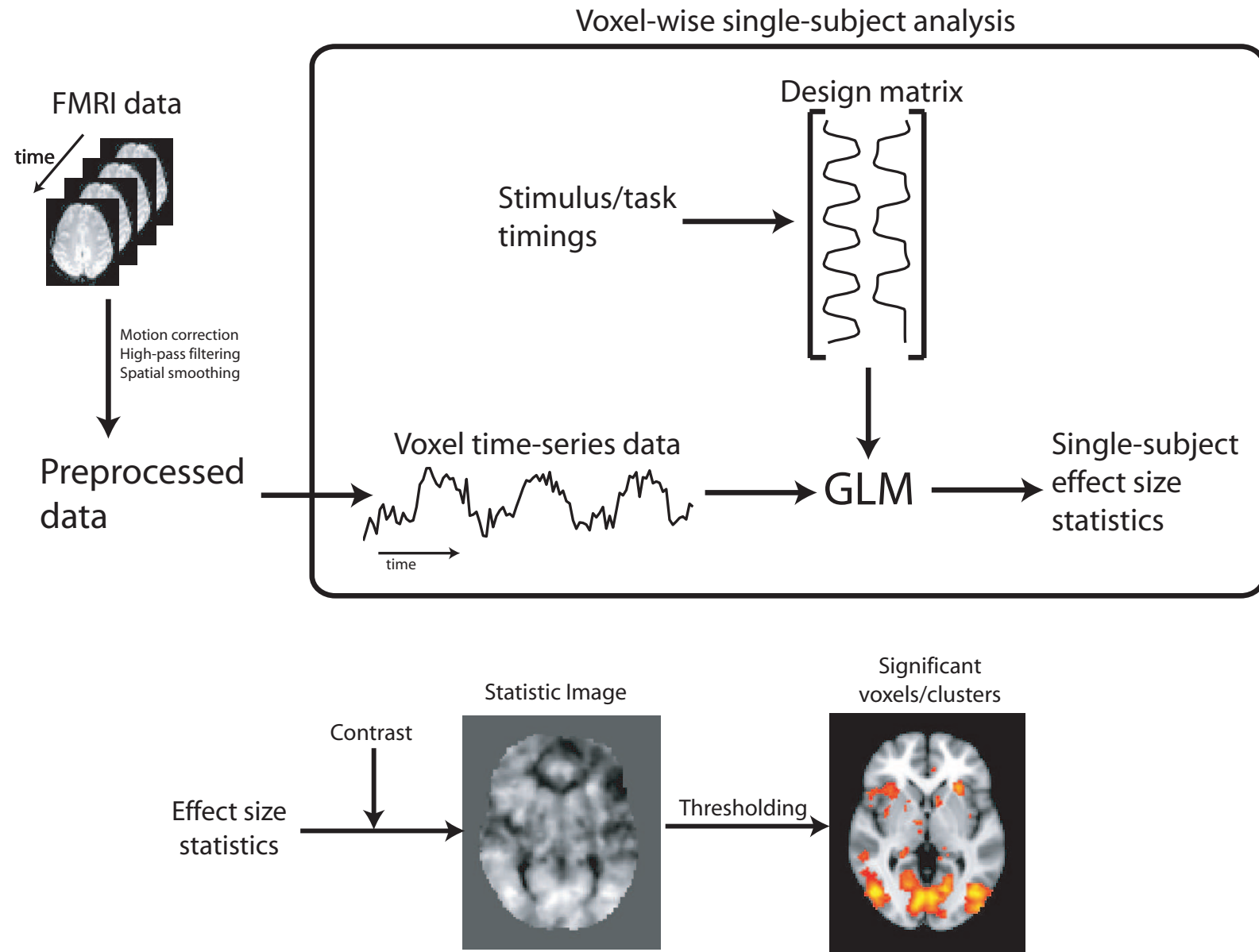


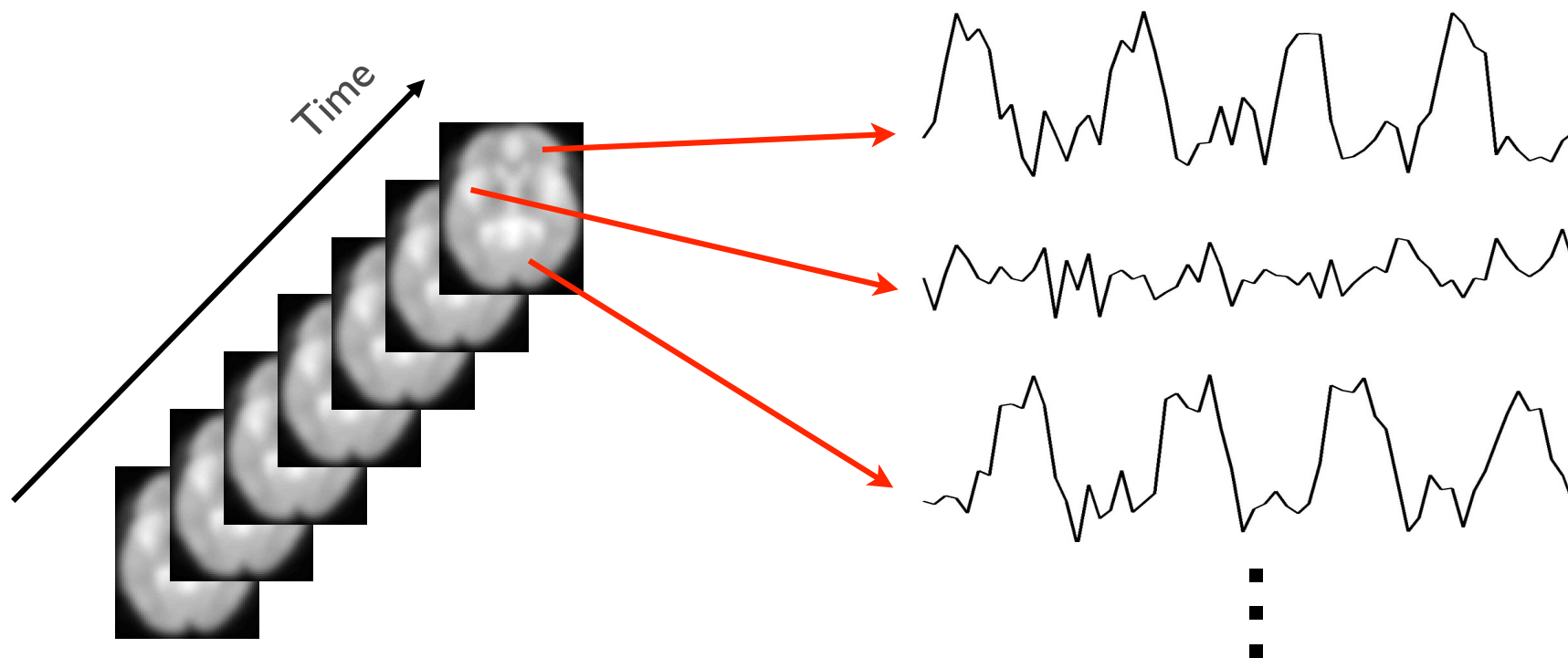


Single-Session Analysis





Two different views of the data



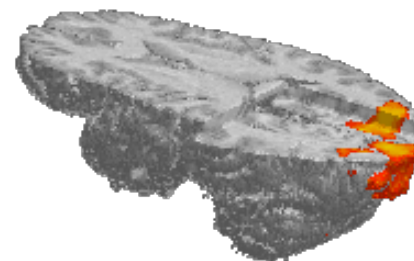
A “smallish”
number of
volumes

A **large**
number of
time series



FMRI Modelling and Statistics

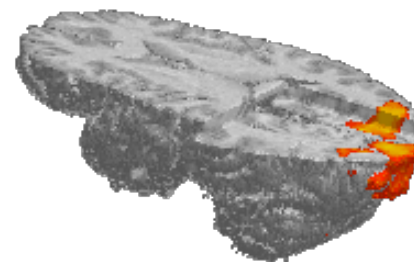
- An example experiment
- Multiple regression (GLM)
- T and F Contrasts
- Null hypothesis testing
- The residuals
- Thresholding: multiple comparison correction





FMRI Modelling and Statistics

- An example experiment
- Multiple regression (GLM)
- T and F Contrasts
- Null hypothesis testing
- The residuals
- Thresholding: multiple comparison correction

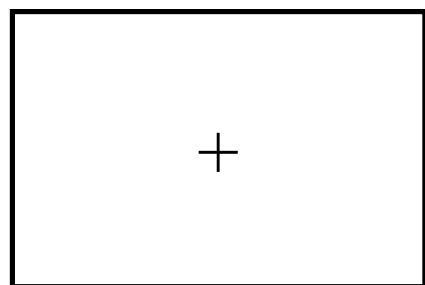




An example experiment

An fMRI adaptation of a classical PET experiment

- Three types of events
- 1st type: Word Generation



Screen

Healthy
Volunteer



Scanner

Bed



An example experiment

An fMRI adaptation of a classical PET experiment

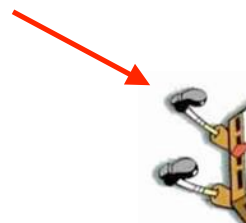
- Three types of events
- 1st type: Word Generation

Noun is presented



Screen

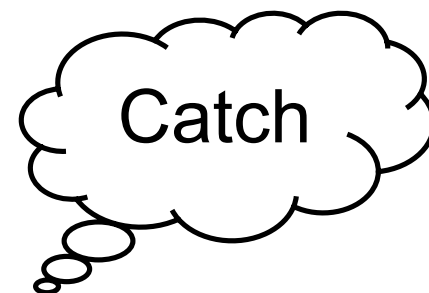
Healthy
Volunteer



Bed



Verb is generated





An example experiment

An fMRI adaptation of a classical PET experiment

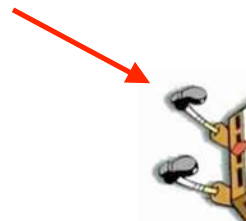
- Three types of events
- 1st type: Word Generation

Noun is presented



Screen

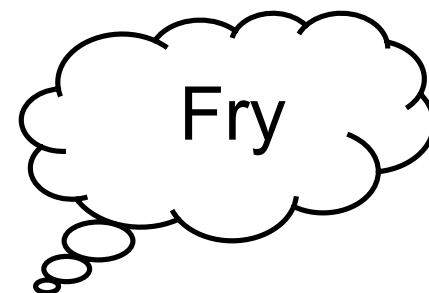
Healthy
Volunteer



Bed

Scanner

Verb is generated



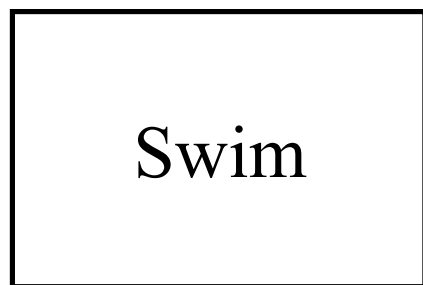


An example experiment

An fMRI adaptation of a classical PET experiment

- Three types of events
- 1st type: Word Generation
- 2nd type: Word Shadowing

Verb is presented



Screen

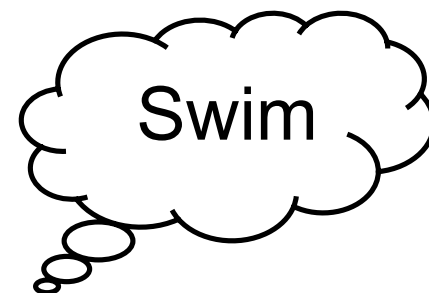
Healthy
Volunteer



Scanner

Bed

Verb is repeated



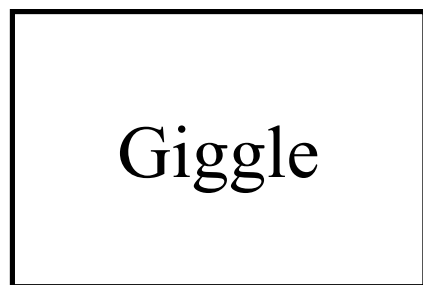


An example experiment

An fMRI adaptation of a classical PET experiment

- Three types of events
- 1st type: Word Generation
- 2nd type: Word Shadowing

Verb is presented



Screen

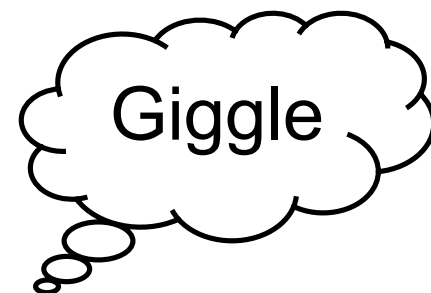
Healthy
Volunteer



Scanner

Bed

Verb is repeated



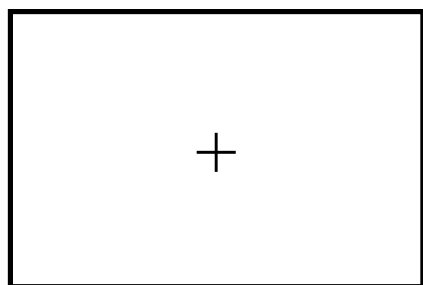


An example experiment

An fMRI adaptation of a classical PET experiment

- Three types of events
- 1st type: Word Generation
- 2nd type: Word Shadowing
- 3rd type: Null event

Crosshair is shown



Screen

Healthy
Volunteer



Scanner

Bed

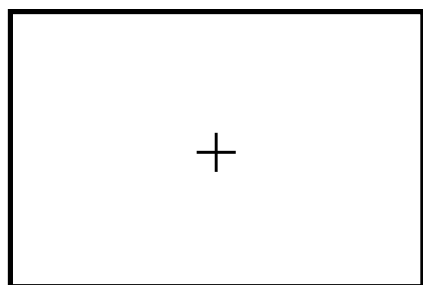


An example experiment

An fMRI adaptation of a classical PET experiment

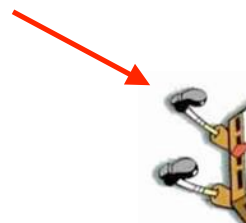
- Three types of events
- 1st type: Word Generation
- 2nd type: Word Shadowing
- 3rd type: Null event

Crosshair is shown



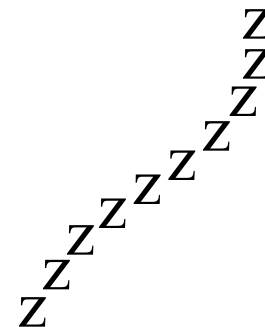
Screen

Healthy
Volunteer



Scanner

Bed

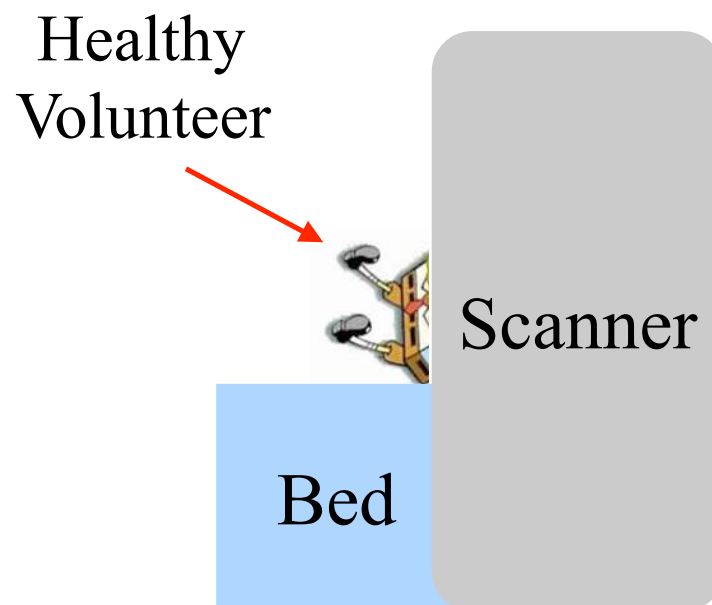
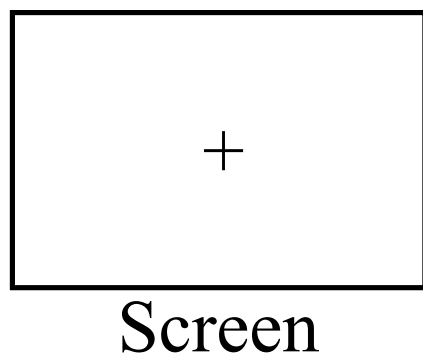




An example experiment

An fMRI adaptation of a classical PET experiment

- Three types of events
- 1st type: Word Generation
- 2nd type: Word Shadowing
- 3rd type: Null event
- 6 sec ISI, random order

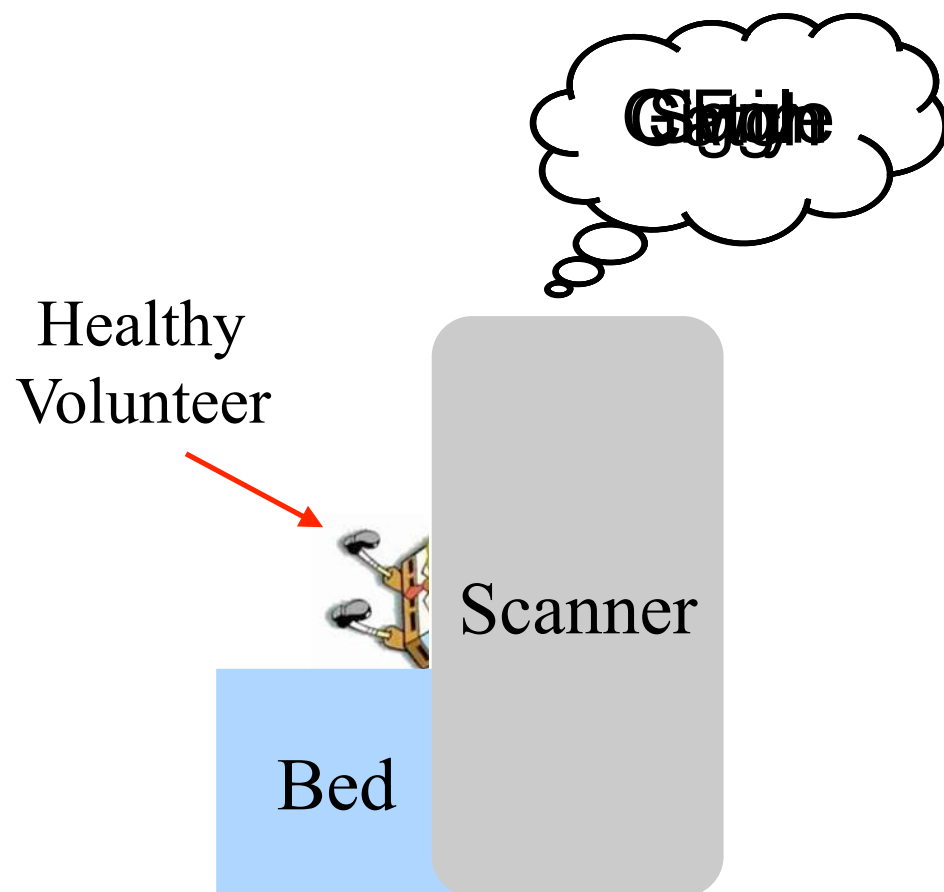
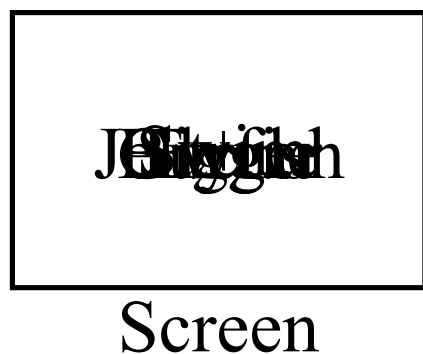




An example experiment

An fMRI adaptation of a classical PET experiment

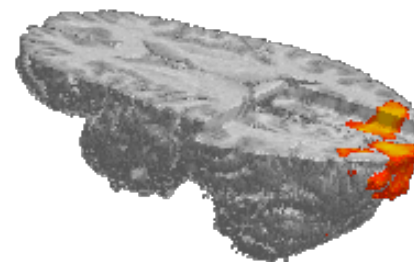
- Three types of events
- 1st type: Word Generation
- 2nd type: Word Shadowing
- 3rd type: Null event
- 6 sec ISI, random order
- For 24 events of each type





FMRI Modelling and Statistics

- An example experiment
- Multiple regression (GLM)
- T and F Contrasts
- Null hypothesis testing
- The residuals
- Thresholding: multiple comparison correction





Building a model

Our task is now to build a model for that experiment

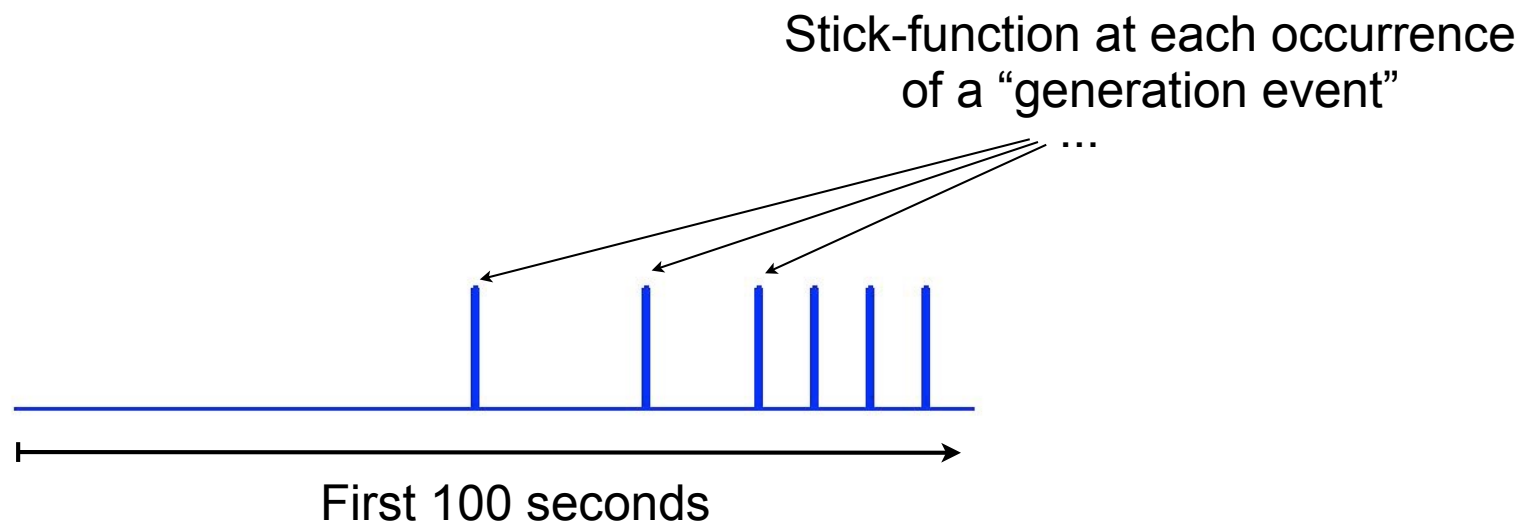
What is our predicted response to the word generation events?



Building a model

Our task is now to build a model for that experiment

What is our predicted response to the word generation events?



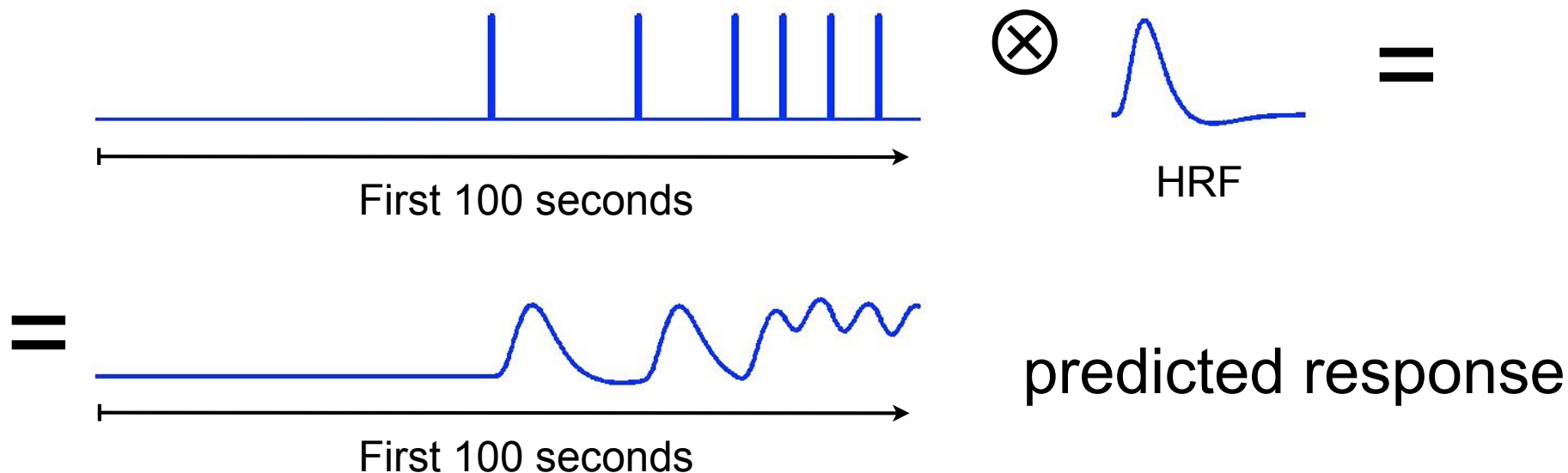
Well, hardly like this...



Building a model

Our task is now to build a model for that experiment

What is our predicted response to the word generation events?



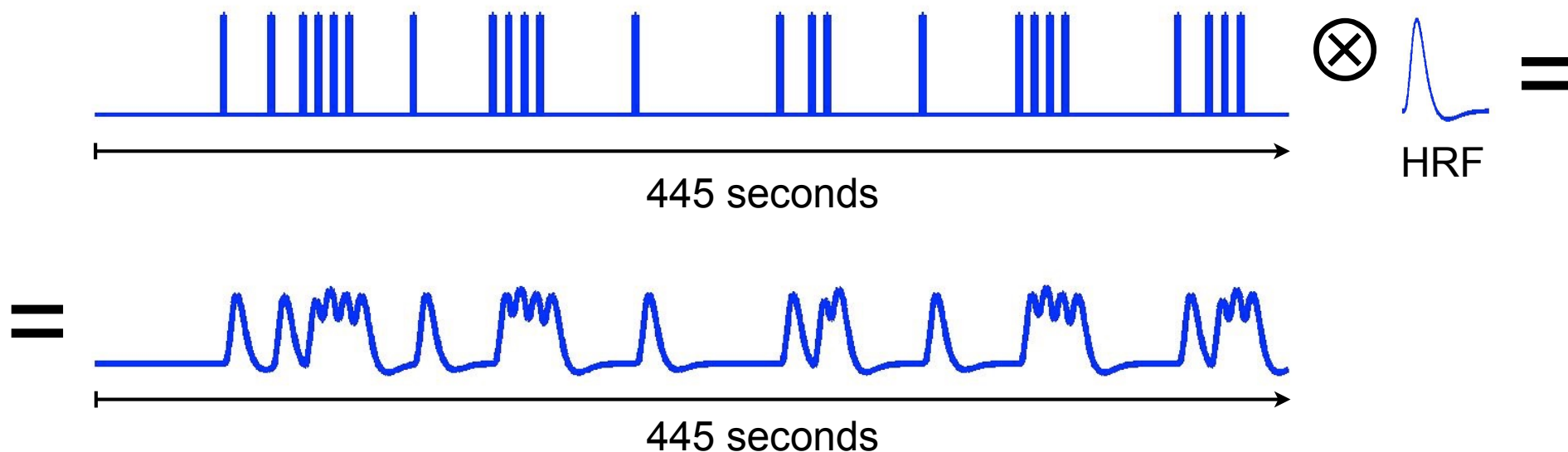
That looks better!



Building a model

Our task is now to build a model for that experiment

What is our predicted response to the word generation events?



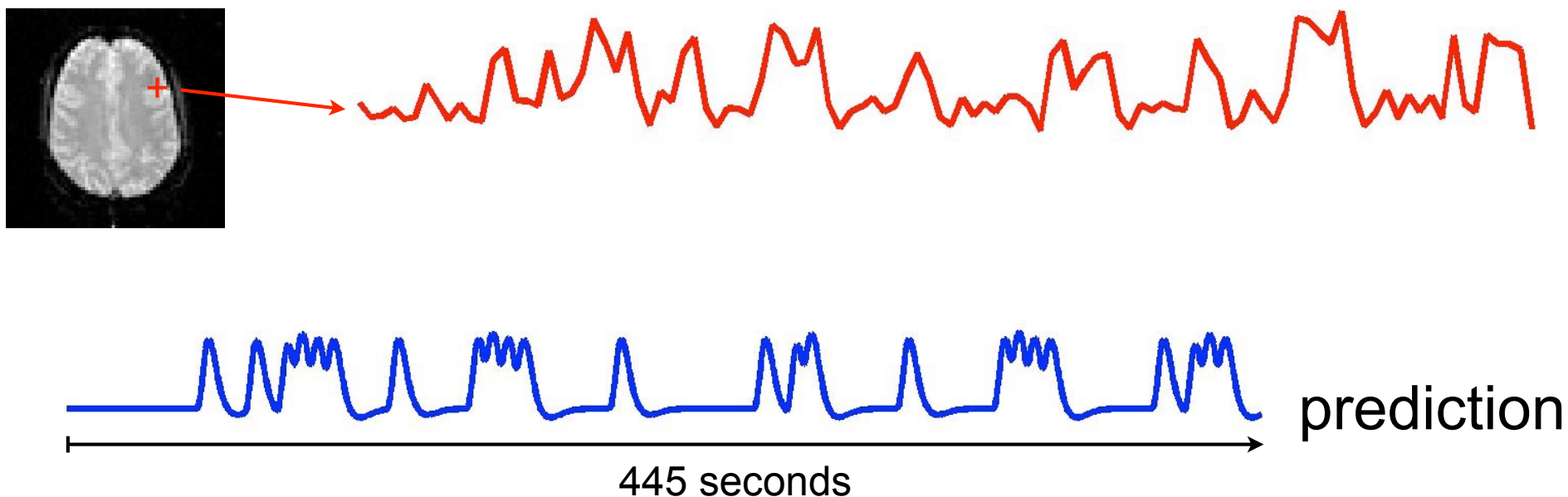
And this is the prediction for the whole time-series



Building a model

Our task is now to build a model for that experiment

What is our predicted response to the word generation events?



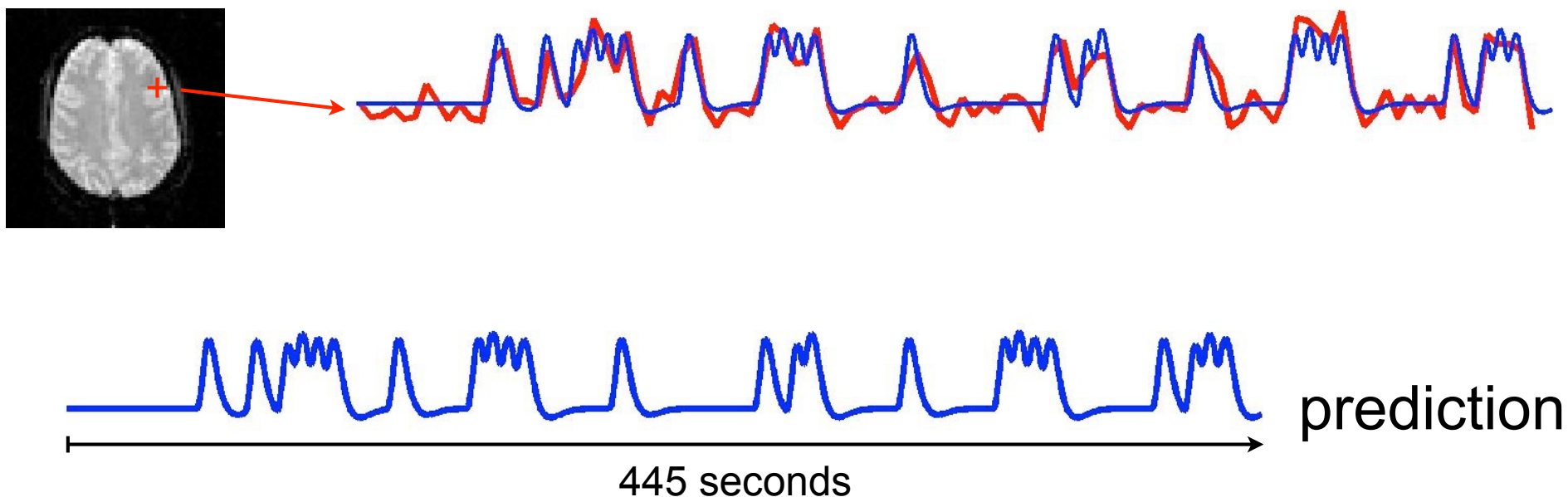
So, if we spot a time-series like this



Building a model

Our task is now to build a model for that experiment

What is our predicted response to the word generation events?



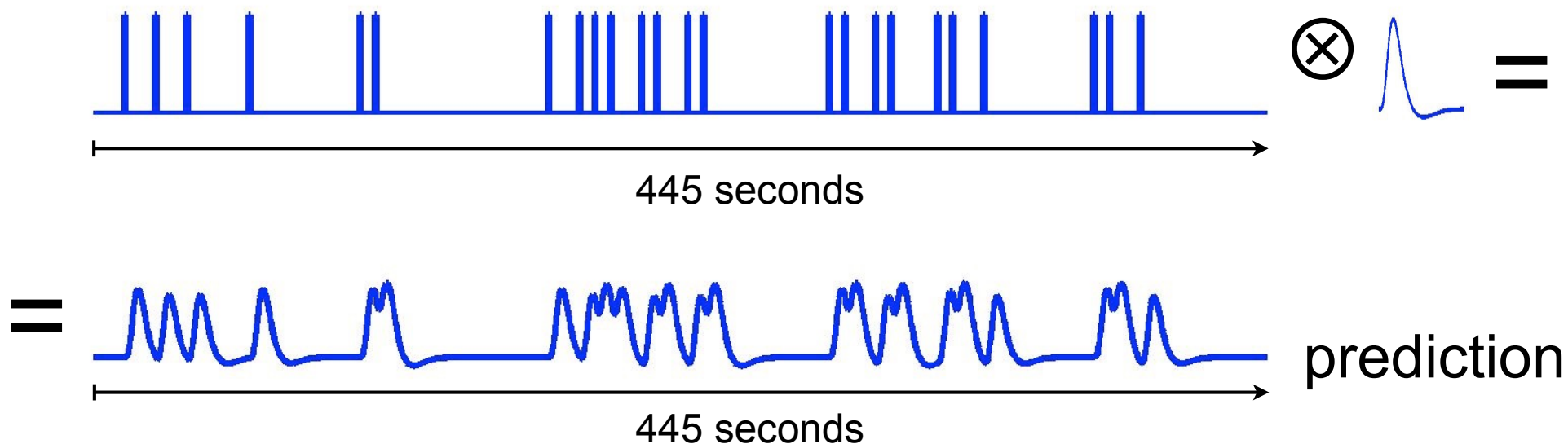
And then check it against our prediction
we can conclude that this pixel is into word generation



Building a model

Our task is now to build a model for that experiment

And we can do the same for the word shadowing events?



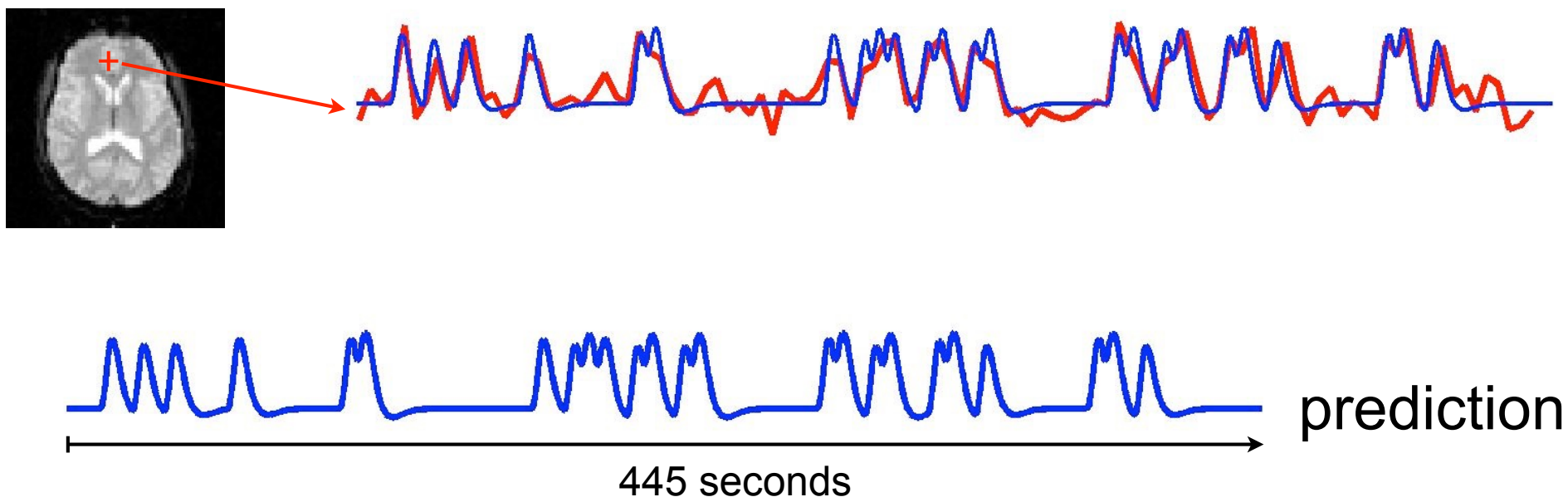
This time we used the onset times for the shadowing events to get the predicted brain response for those



Building a model

Our task is now to build a model for that experiment

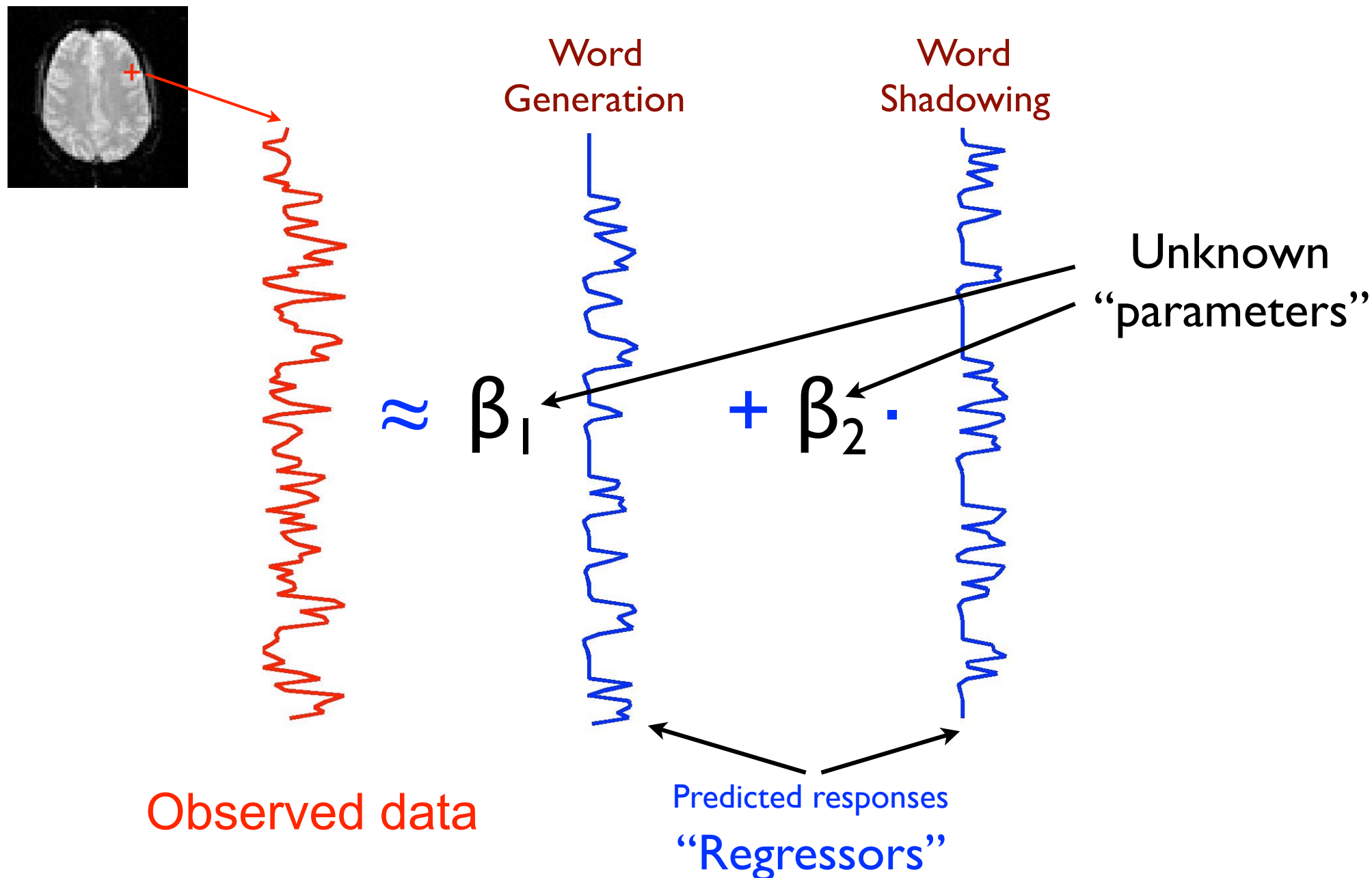
And we can do the same for the word shadowing events?



And we can look for voxels that match that

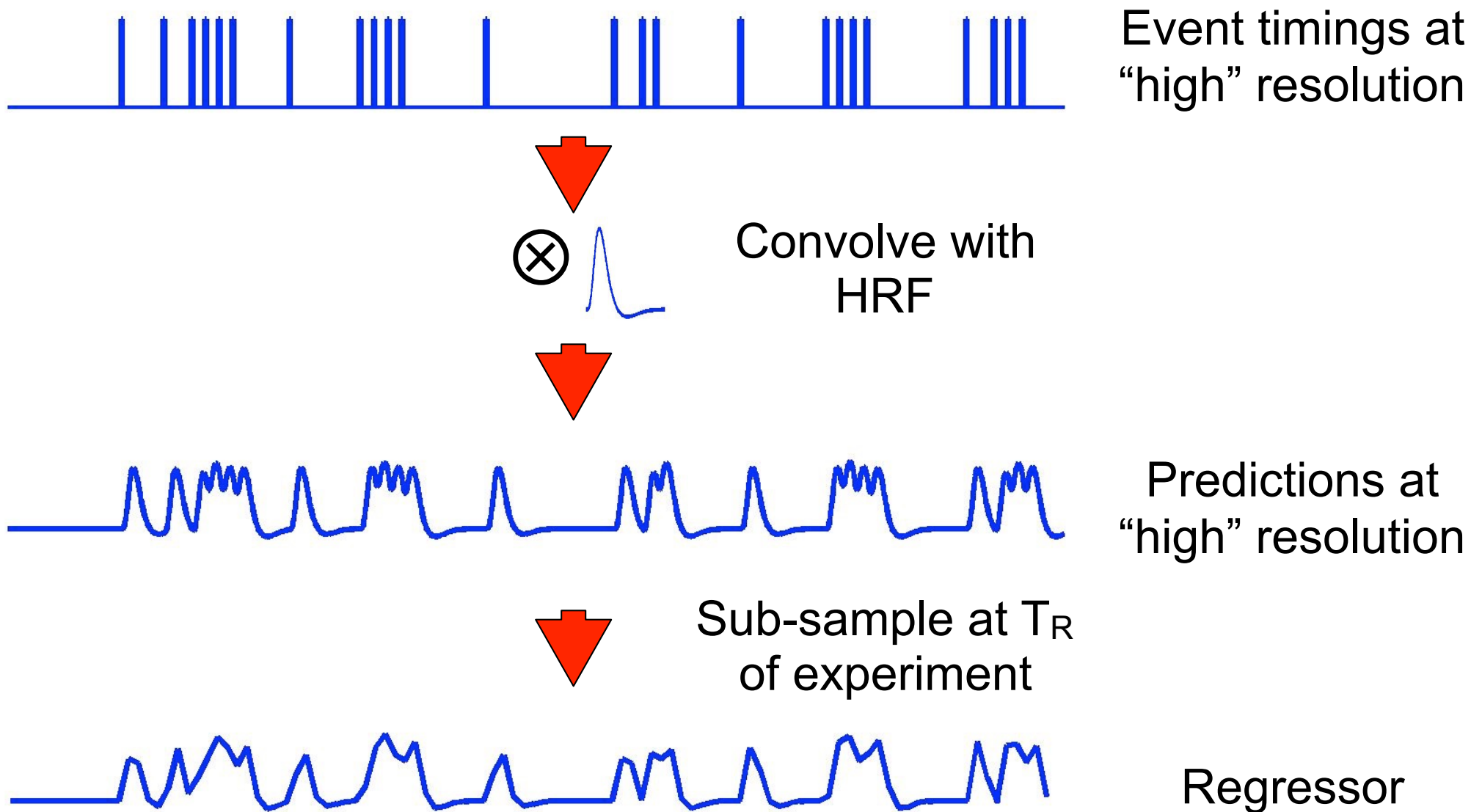


Formalising it: Multiple regression





Slight detour: Making regressors

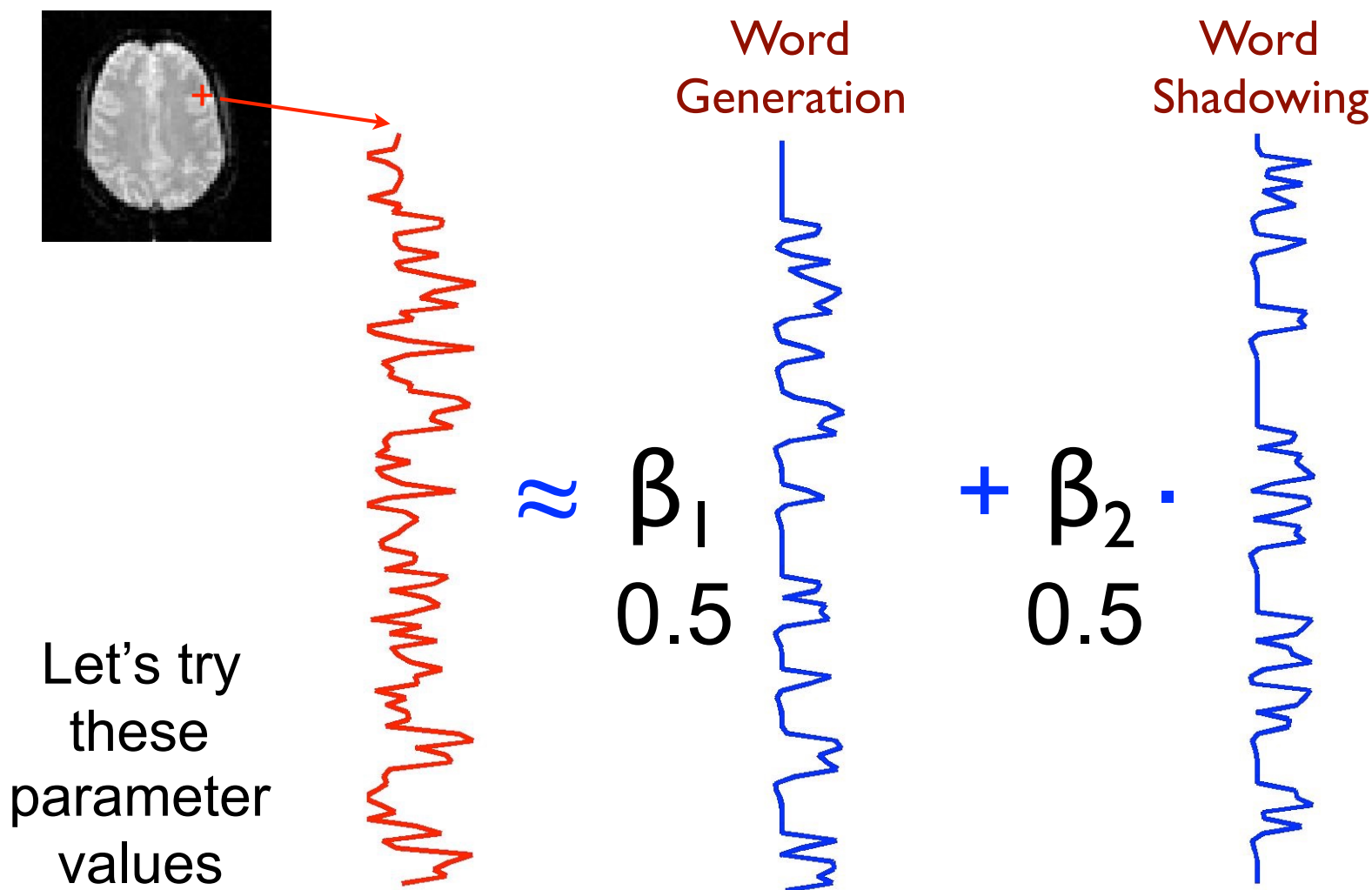




Estimation:

Finding the “best” parameter values

- The estimation entails finding the parameter values such that the linear combination “best” fits the data.

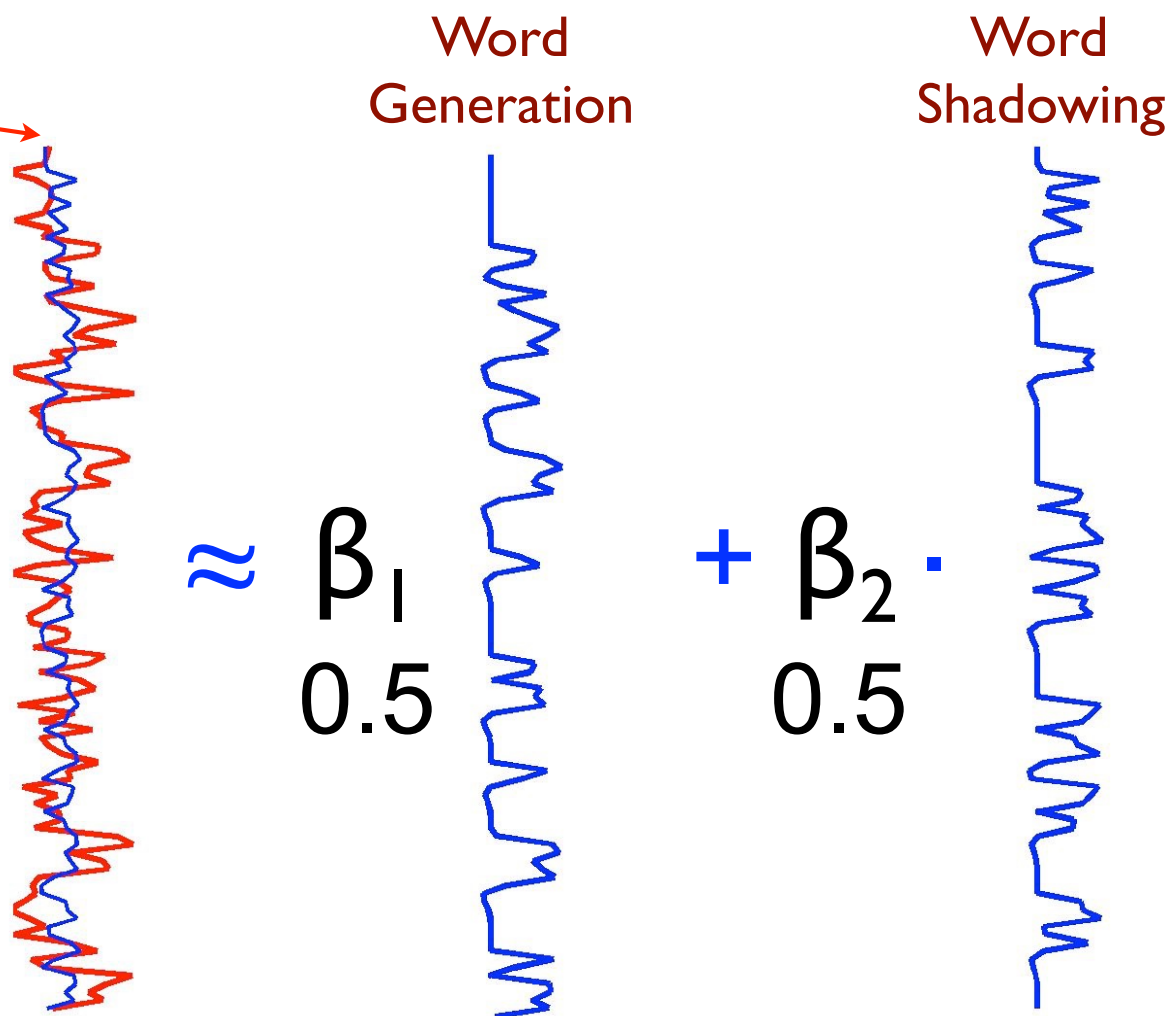
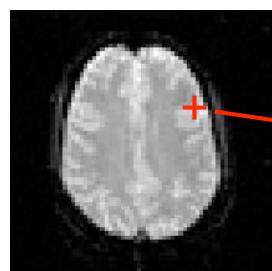




Estimation:

Finding the “best” parameter values

- The estimation entails finding the parameter values such that the linear combination “best” fits the data.



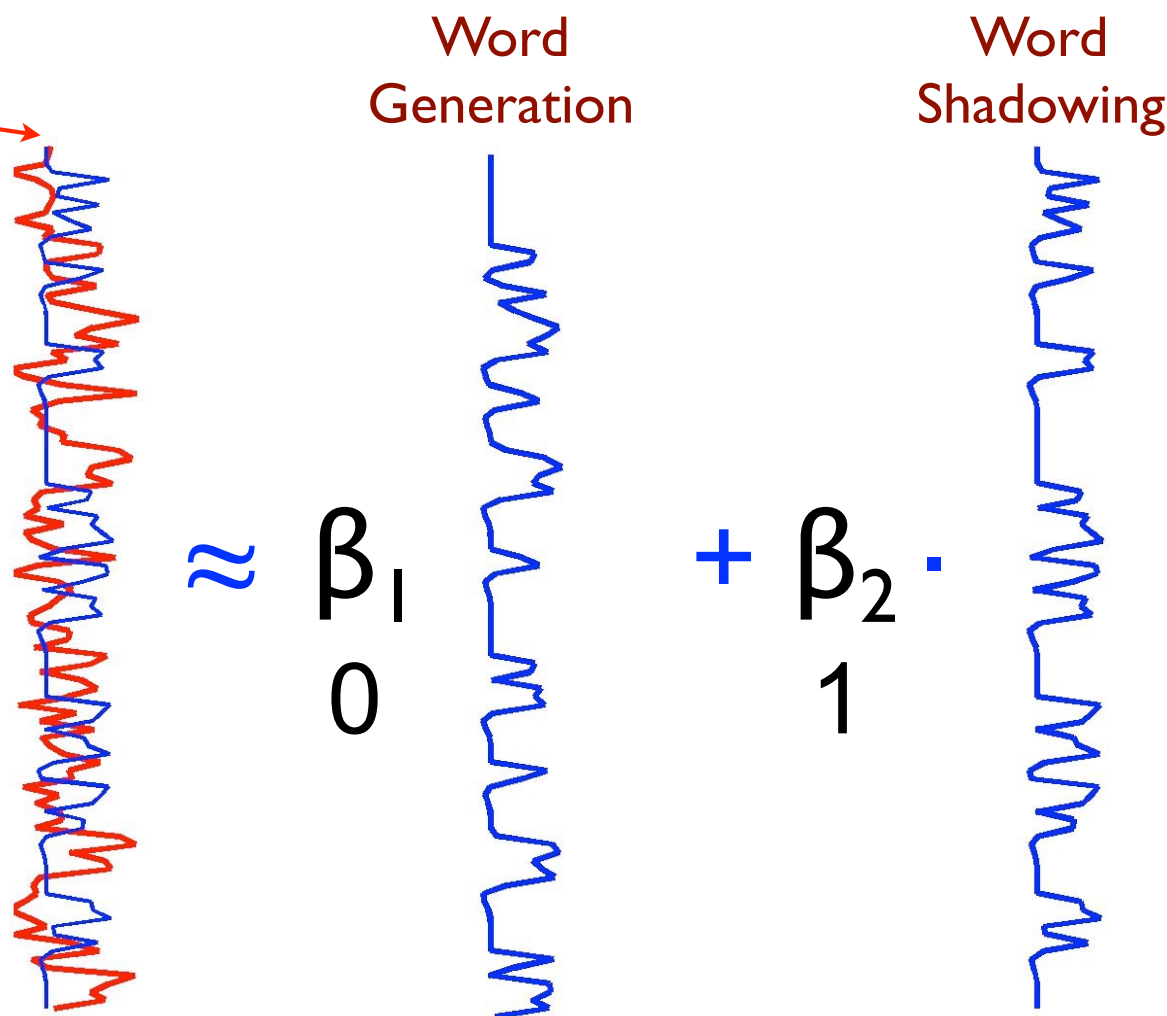
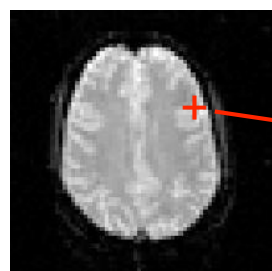
Hmm, not a
great fit



Estimation:

Finding the “best” parameter values

- The estimation entails finding the parameter values such that the linear combination “best” fits the data.



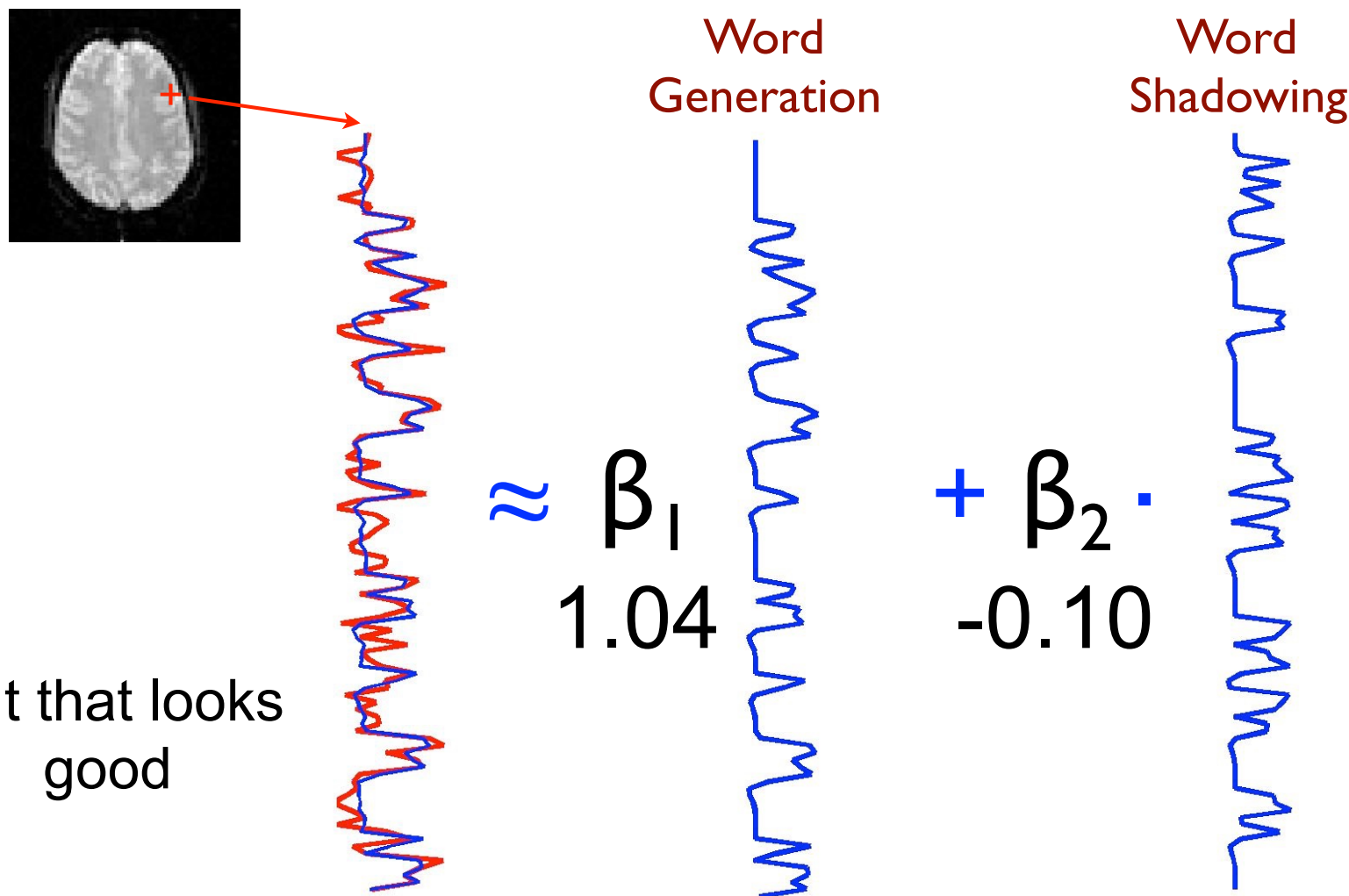
Oh dear,
even worse



Estimation:

Finding the “best” parameter values

- The estimation entails finding the parameter values such that the linear combination “best” fits the data.



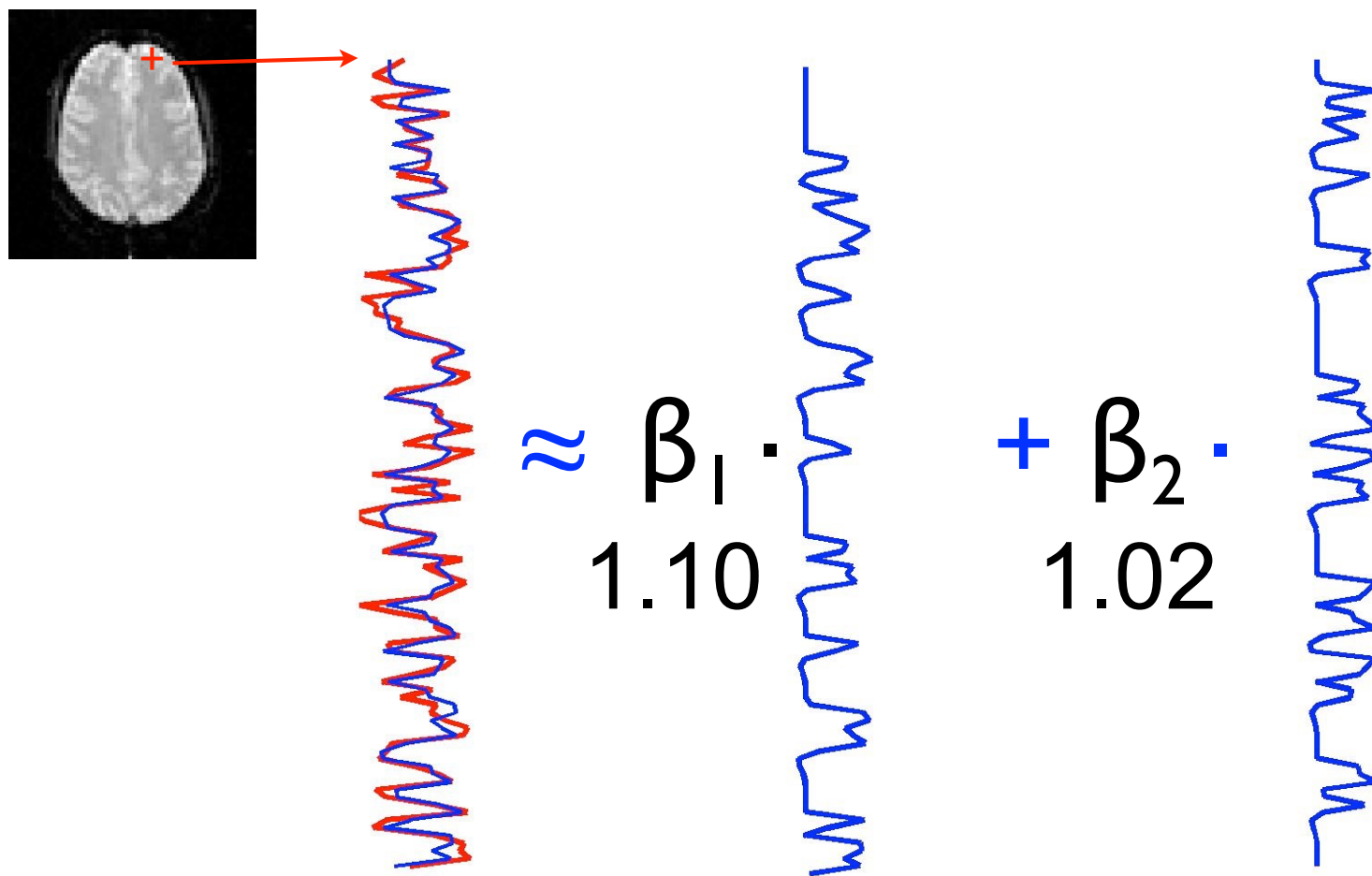
But that looks good



Estimation:

Finding the “best” parameter values

- The estimation entails finding the parameter values such that the linear combination “best” fits the data



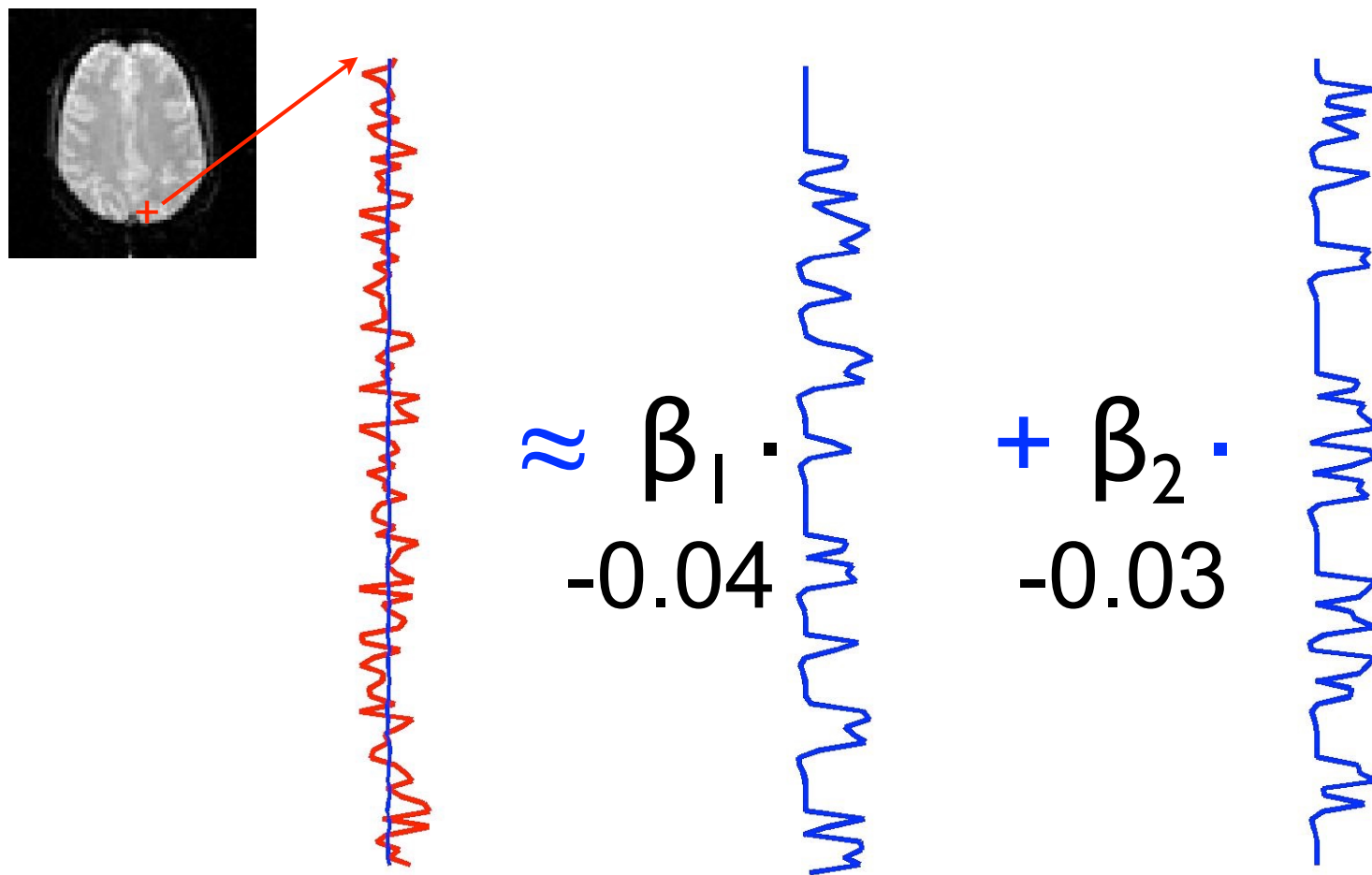
And different voxels yield different parameters



Estimation:

Finding the “best” parameter values

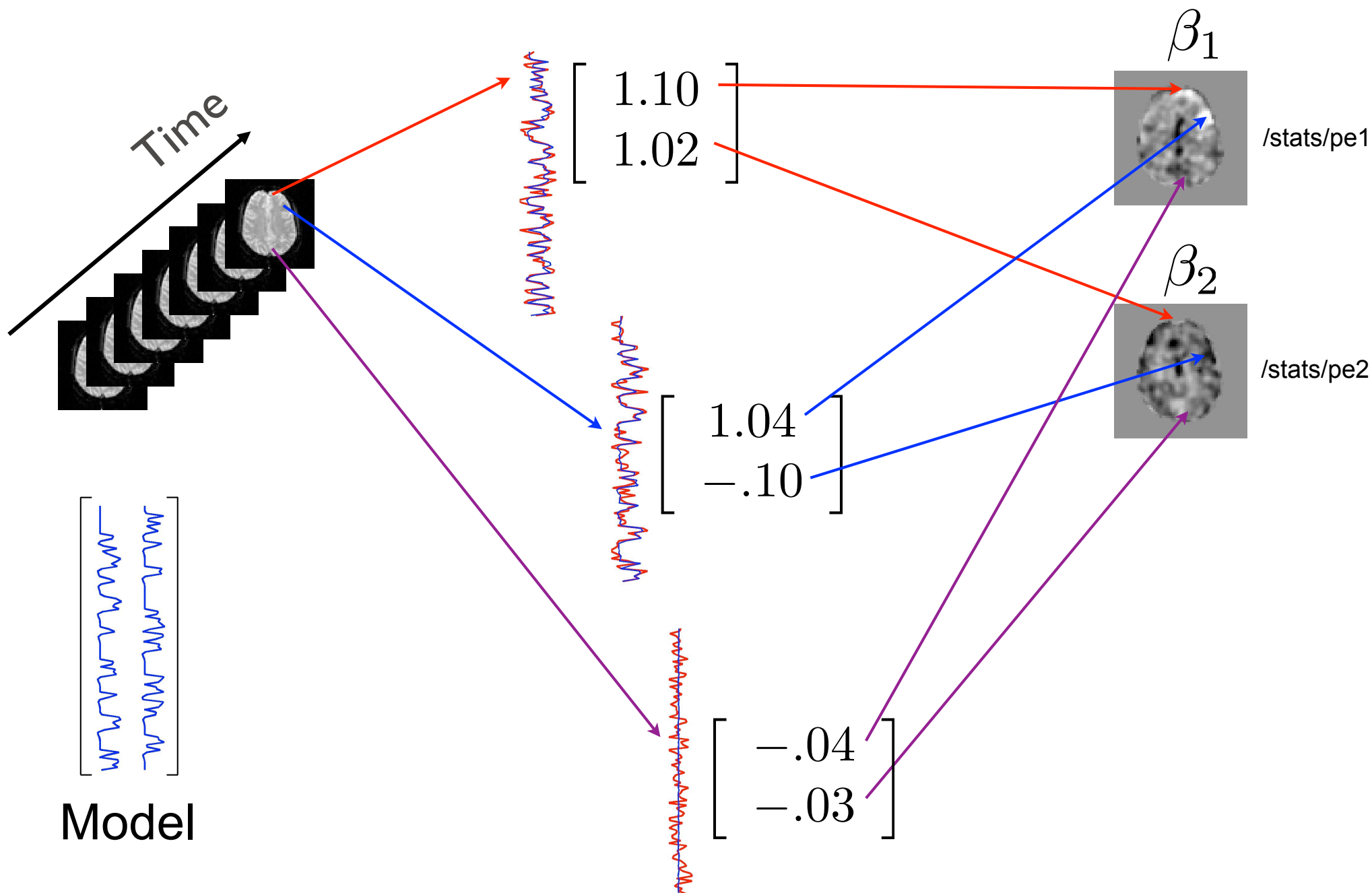
- The estimation entails finding the parameter values such that the linear combination “best” fits the data



And different voxels yield different parameters



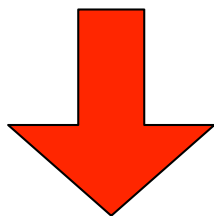
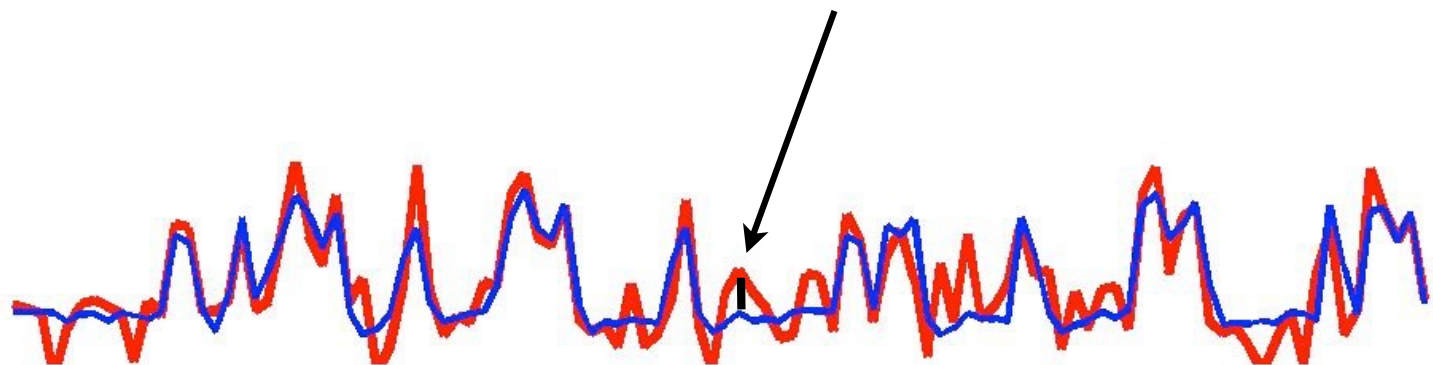
One model to fit them all





And we can also estimate the residual error

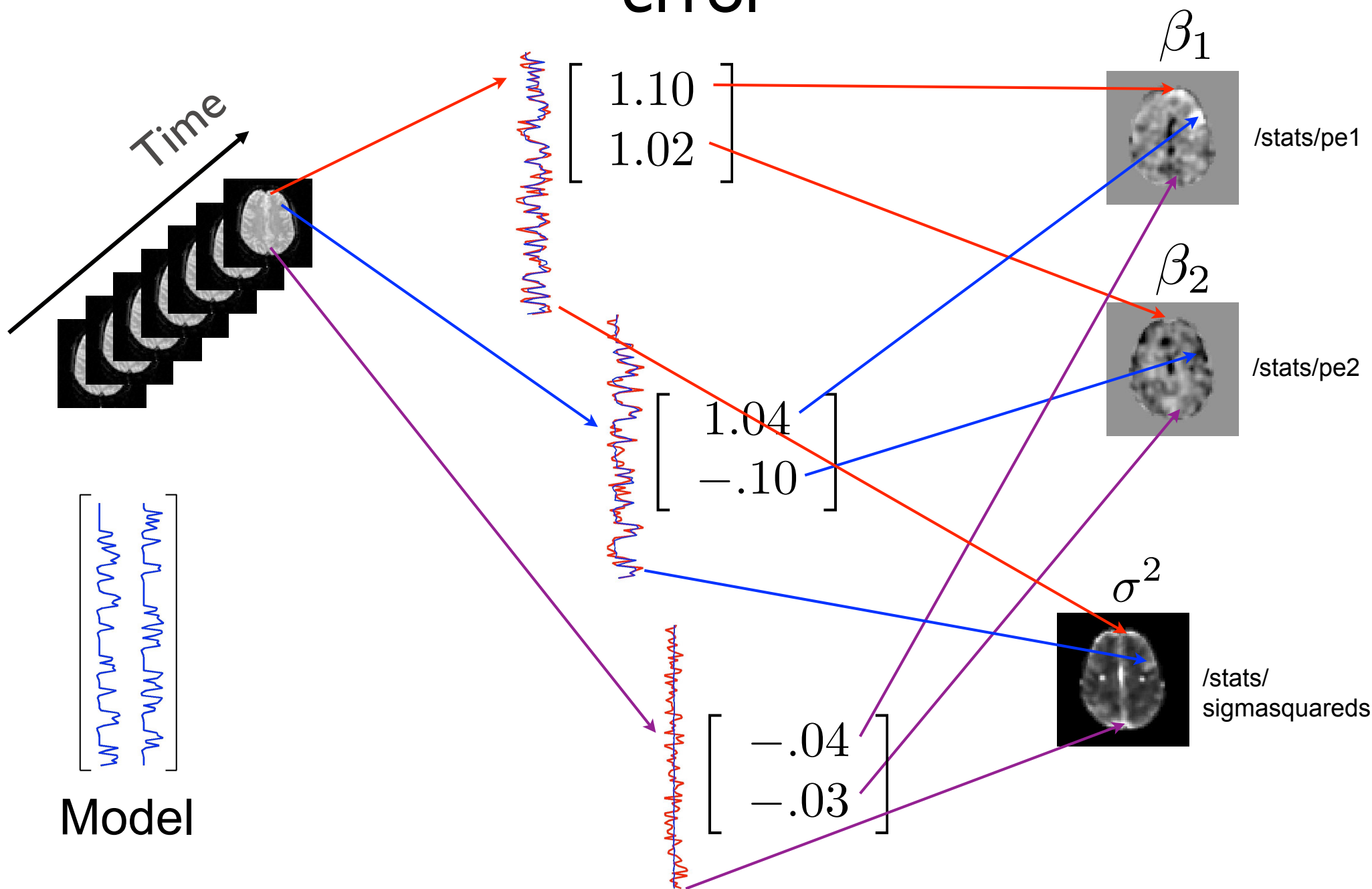
Difference between data and best fit: "Residual error"



Residual errors



And we can also estimate the residual error





Summary of what we learned so far

- The “Model” consists of a set of “regressors” i.e. tentative time series that we expect to see as a response to our stimulus
- The model typically consists of our stimulus functions convolved by the HRF
- The estimation entails finding the parameter values such that the linear combination of regressors “best” fits the data
- Every voxel has its own unique parameter values, that is how a single model can fit so many different time series
- We can also get an estimate of the error through the “residuals”



General Linear Model (GLM)

- This is placed into the General Linear Model (GLM) framework

Regressor, Explanatory Variable (EV)

Regression parameters, Effect sizes

$y = X\beta + e$

Data from a voxel

Design Matrix

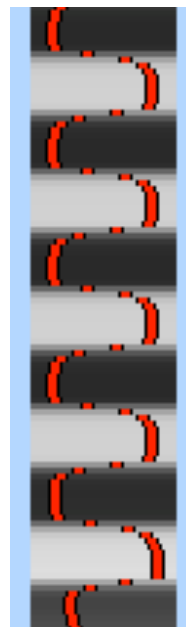
Gaussian noise (temporal autocorrelation)



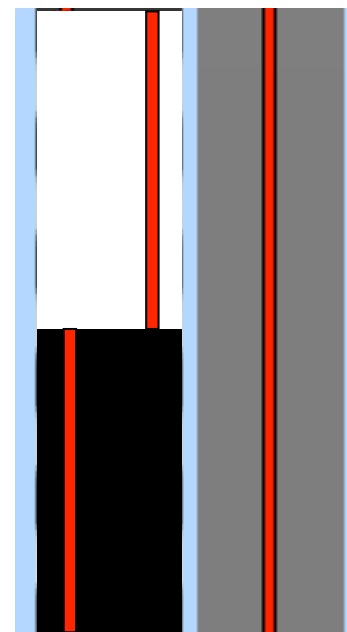
“Demeaning” and the GLM

- The mean value is uninteresting in an FMRI session
- There are two equivalent options:
 - 1.remove the mean from the data and don't model it
 - 2.put a term into the model to account for the mean

option #1



option #2



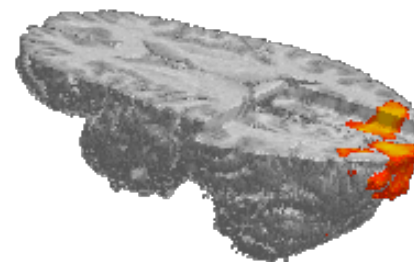
In FSL we use option #1 for first-level analyses and #2 for higher-level analyses

A consequence is that the baseline condition in first-level analysis is **NOT** explicitly modelled (in FSL)



FMRI Modelling and Statistics

- An example experiment
- Multiple regression (GLM)
- **T and F Contrasts**
- Null hypothesis testing
- The residuals
- Thresholding: multiple comparison correction





t-contrasts

- A contrast of parameter estimates (COPE) is a linear combination of PEs:

$$[1 \ 0]: \text{COPE} = 1 \times \hat{\beta}_1 + 0 \times \hat{\beta}_2 = \hat{\beta}_1$$

$$[1 \ -1]: \text{COPE} = 1 \times \hat{\beta}_1 + -1 \times \hat{\beta}_2 = \hat{\beta}_1 - \hat{\beta}_2$$

- Test null hypothesis that $\text{COPE}=0$

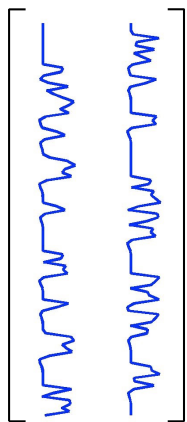
t-statistic: $t = \frac{\text{COPE}}{\text{std}(\text{COPE})}$



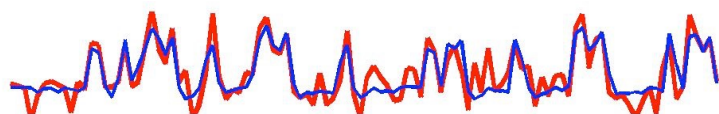
t-contrasts

$$t = \frac{COPE}{std(COPE)}$$

Depends on



$[1 \ 0]$



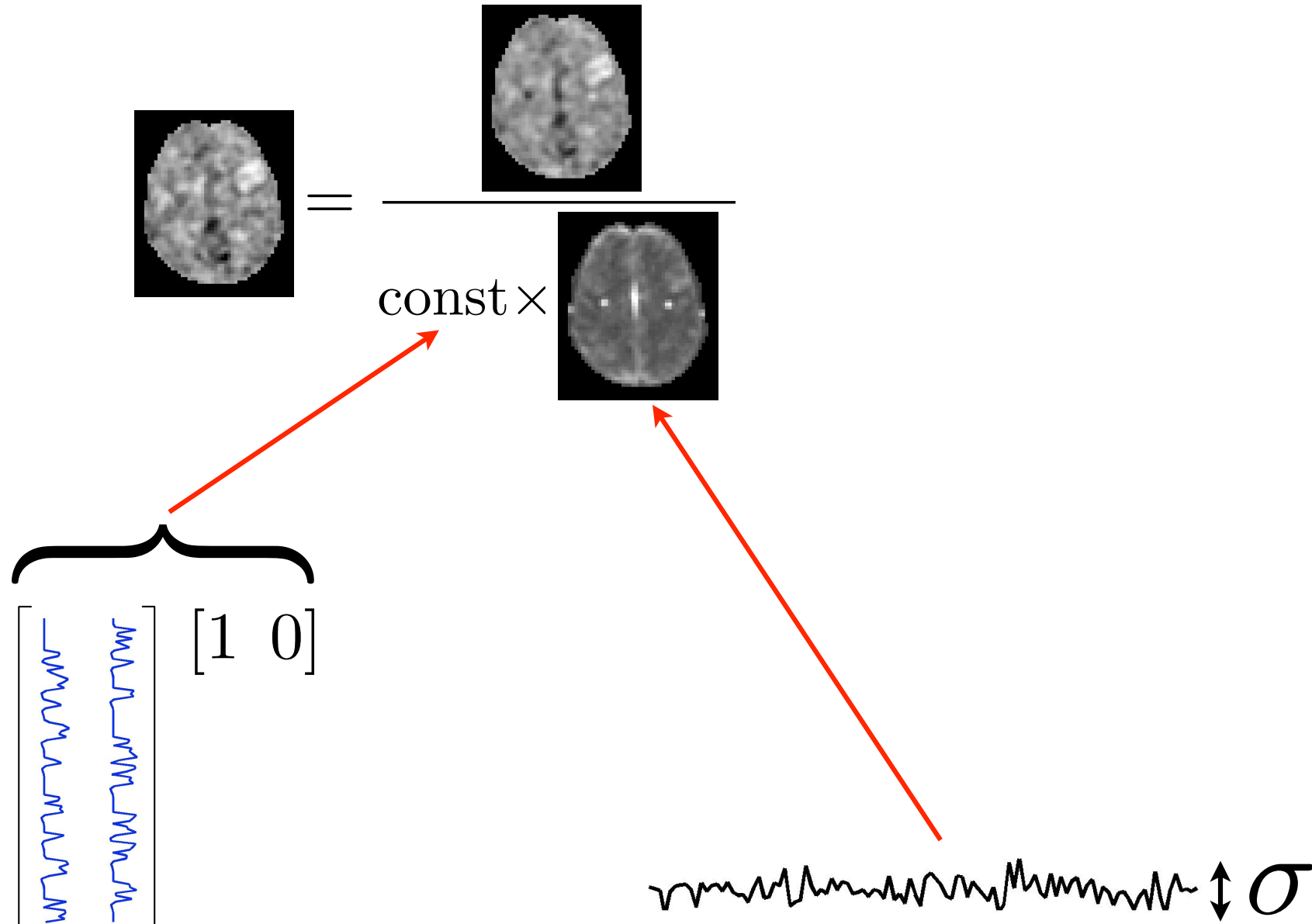
The Model

,the Contrast

and the Residual Error



t-contrasts



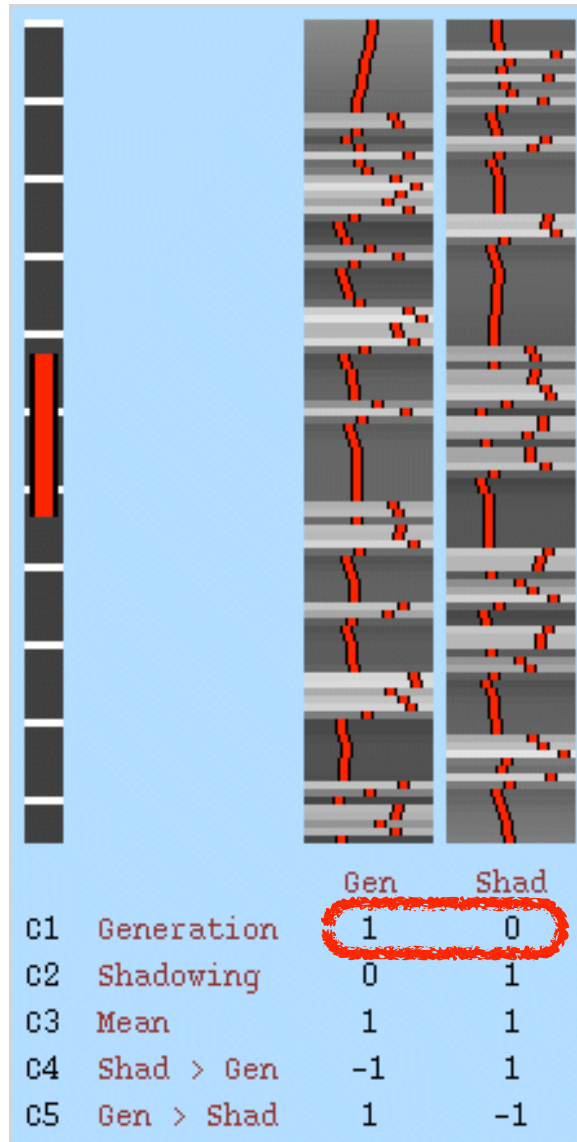
The Model & the Contrast

and the Residual Error



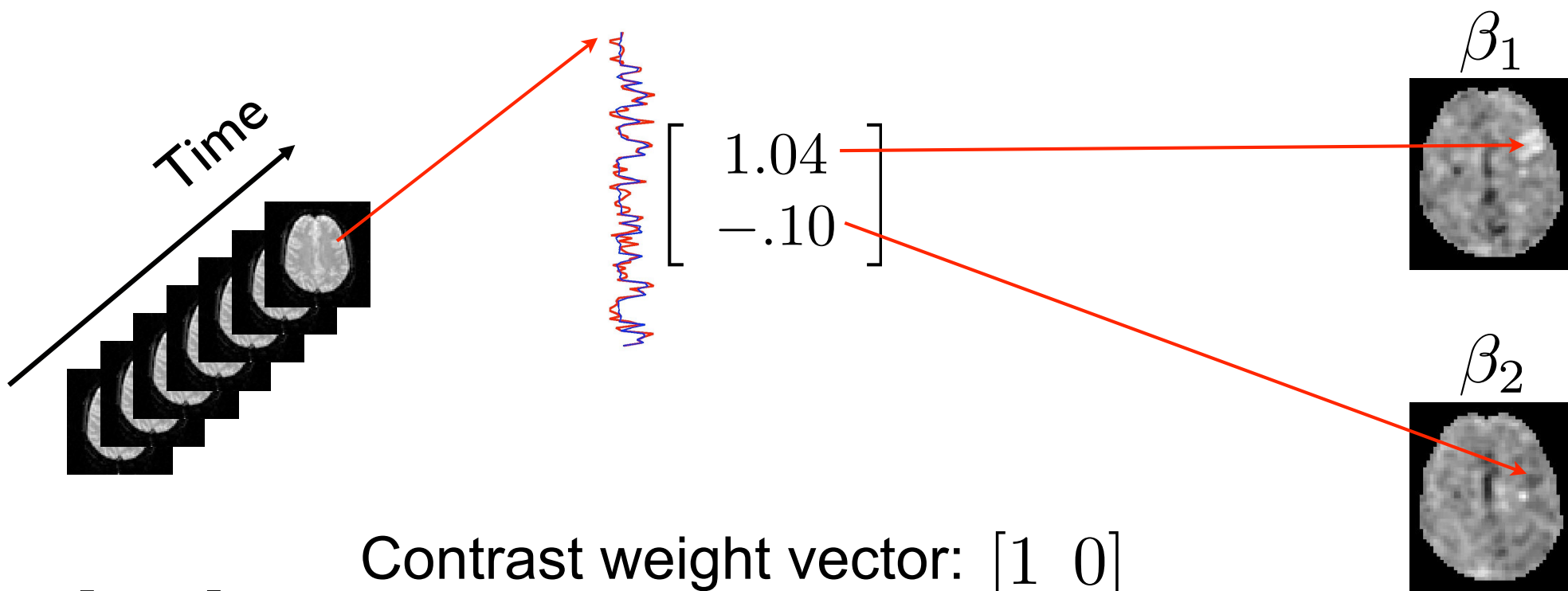
t-contrasts

- $[1 \ 0]$: EV1 only (i.e. Generation vs rest)
- $[0 \ 1]$: EV2 only (i.e. Shadowing vs rest)



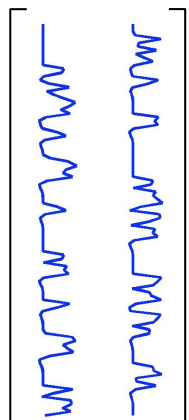


t-contrasts



Contrast weight vector: $\begin{bmatrix} 1 & 0 \end{bmatrix}$

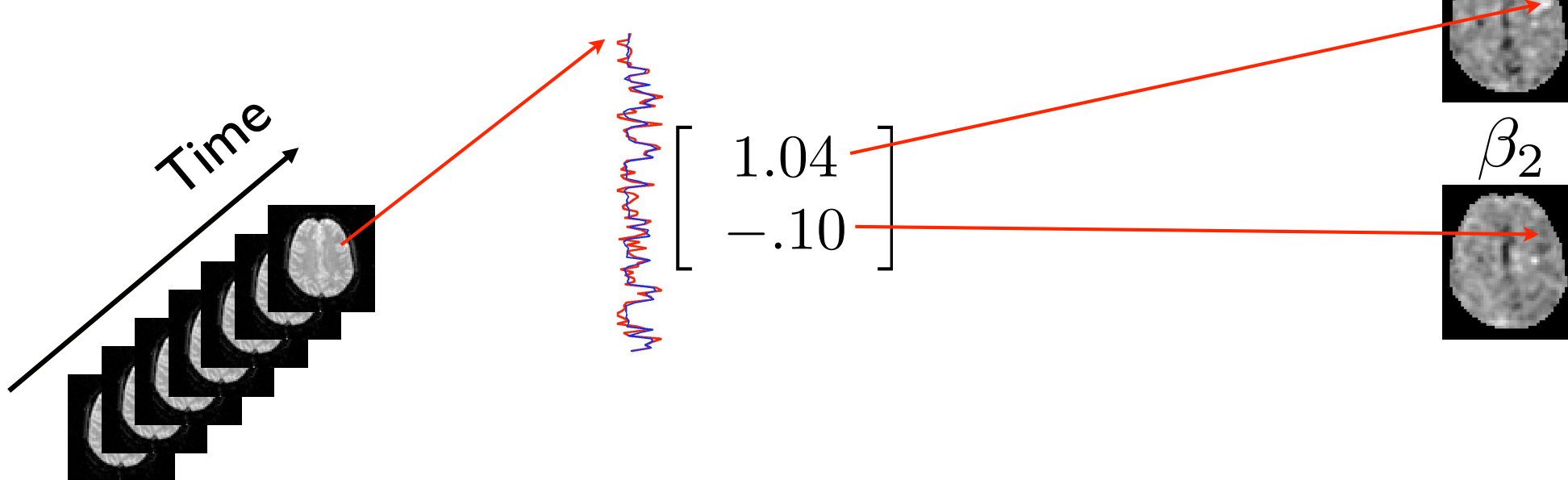
Asks the question: Where do we need this regressor to model the data, i.e. what parts of the brain are used when seeing nouns and generating related verbs?



Model

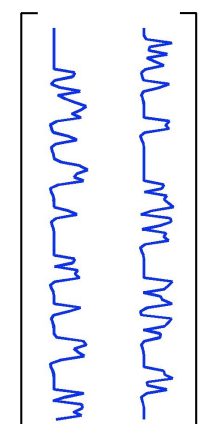


t-contrasts



Contrast weight vector: $\begin{bmatrix} 1 & 0 \end{bmatrix}$

$$\text{COPE} = 1 \times 1.04 + 0 \times -0.10 = 1.04$$

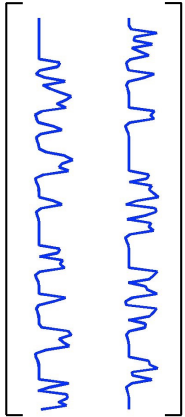
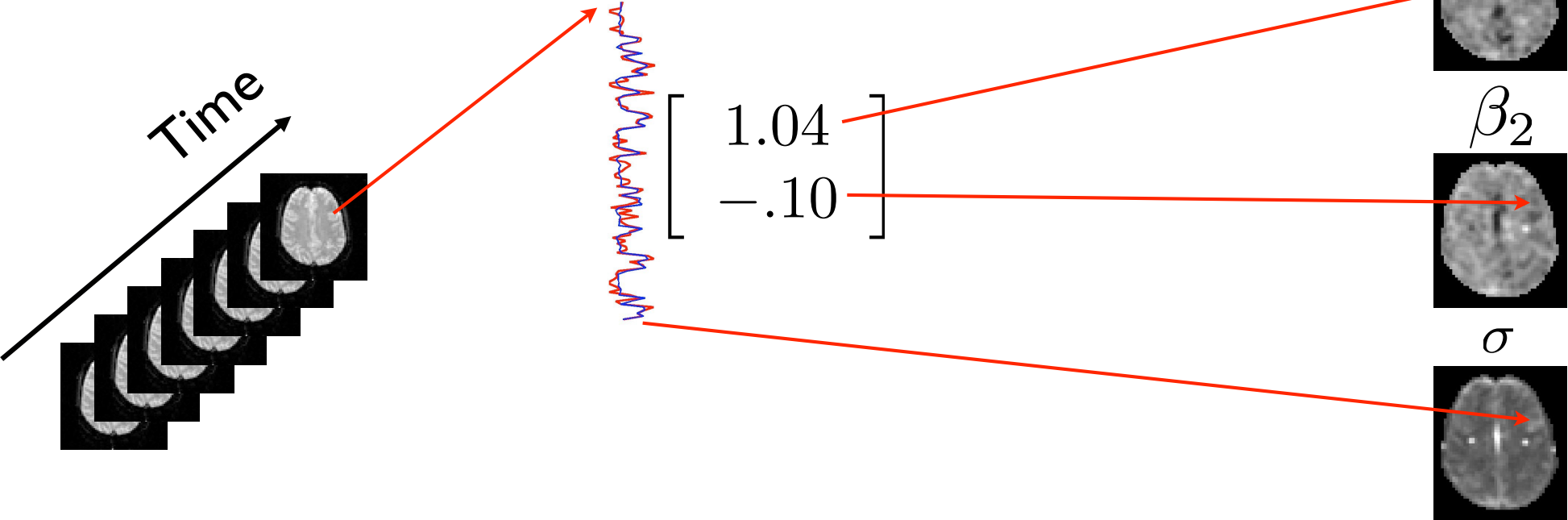


Model

$$\text{COPE} = \text{[Brain Slice]} = \beta_1$$



t-contrasts



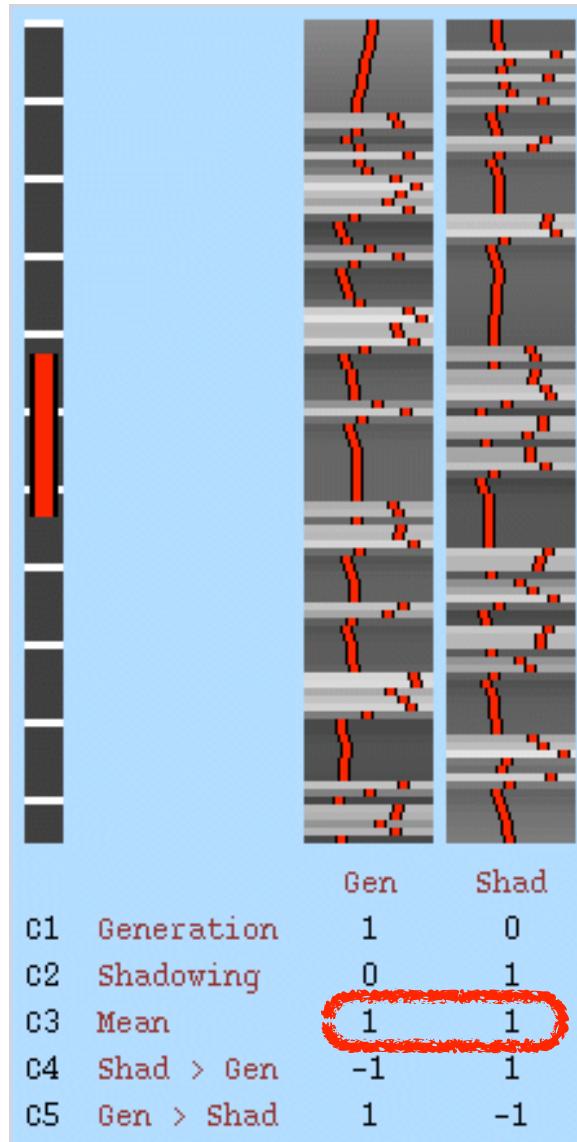
Model

$$t = \frac{\text{COPE}}{\text{std}(\text{COPE})} = \frac{\text{Brain Slice } \beta_1}{\text{Brain Slice } \sigma} = \text{Brain Slice } t$$



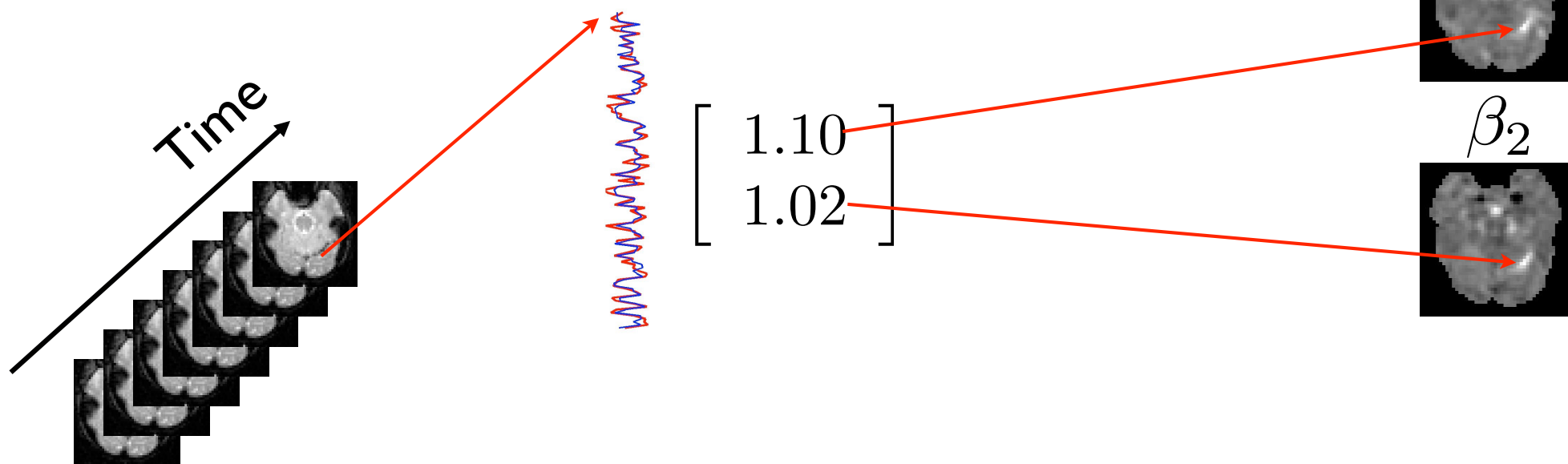
t-contrasts

- $[1 \ 0]$: EV1 only (i.e. Generation vs rest)
- $[0 \ 1]$: EV2 only (i.e. Shadowing vs rest)
- $[1 \ 1]$: EV1 + EV2 (Mean activation)



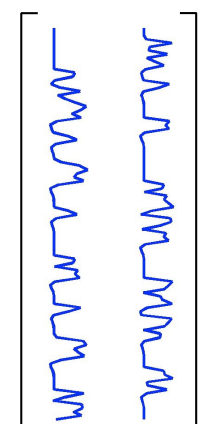


t-contrasts



Contrast weight vector: $\begin{bmatrix} 1 & 1 \end{bmatrix}$

$$\text{COPE} = 1 \times 1.10 + 1 \times 1.02 = 2.12$$

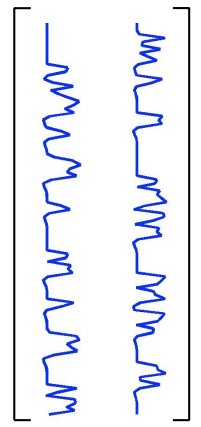
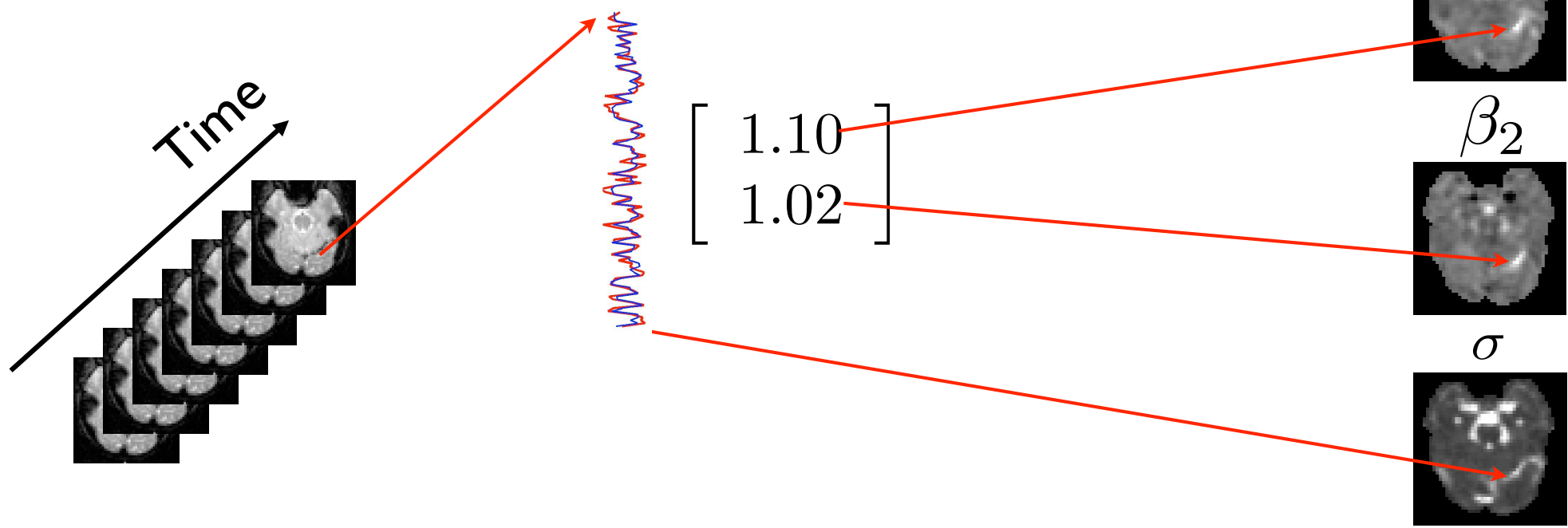


Model

$$\text{COPE} = \text{Brain Slice} = \beta_1 + \beta_2$$



t-contrasts



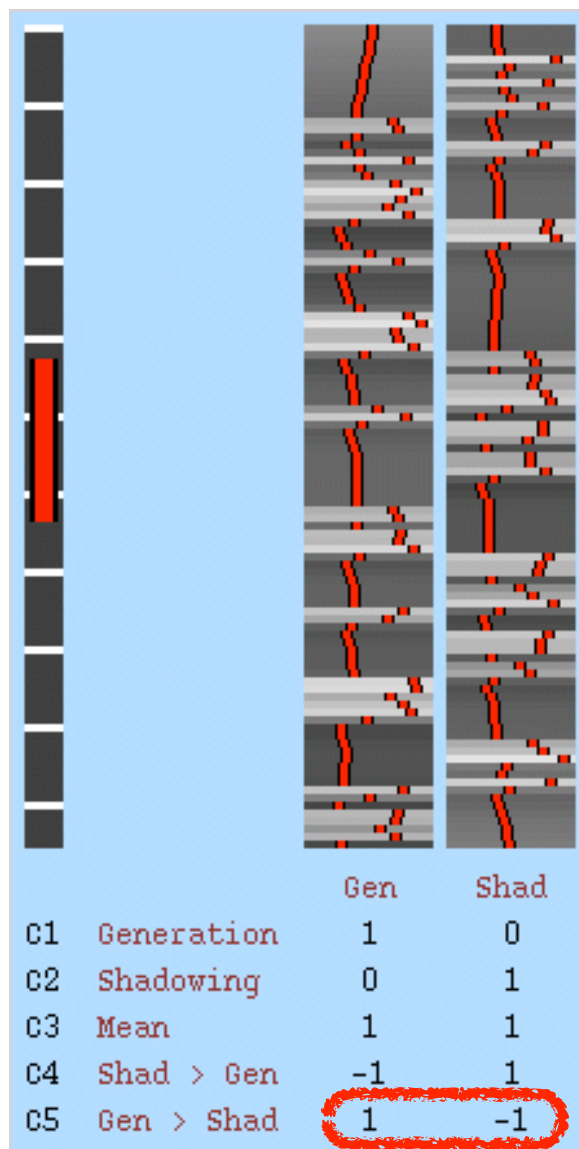
Model

$$t = \frac{\text{COPE}}{\text{std}(\text{COPE})} = \frac{\text{[Brain Slice]}}{\text{[Brain Slice]}} = \text{[Brain Slice]}$$



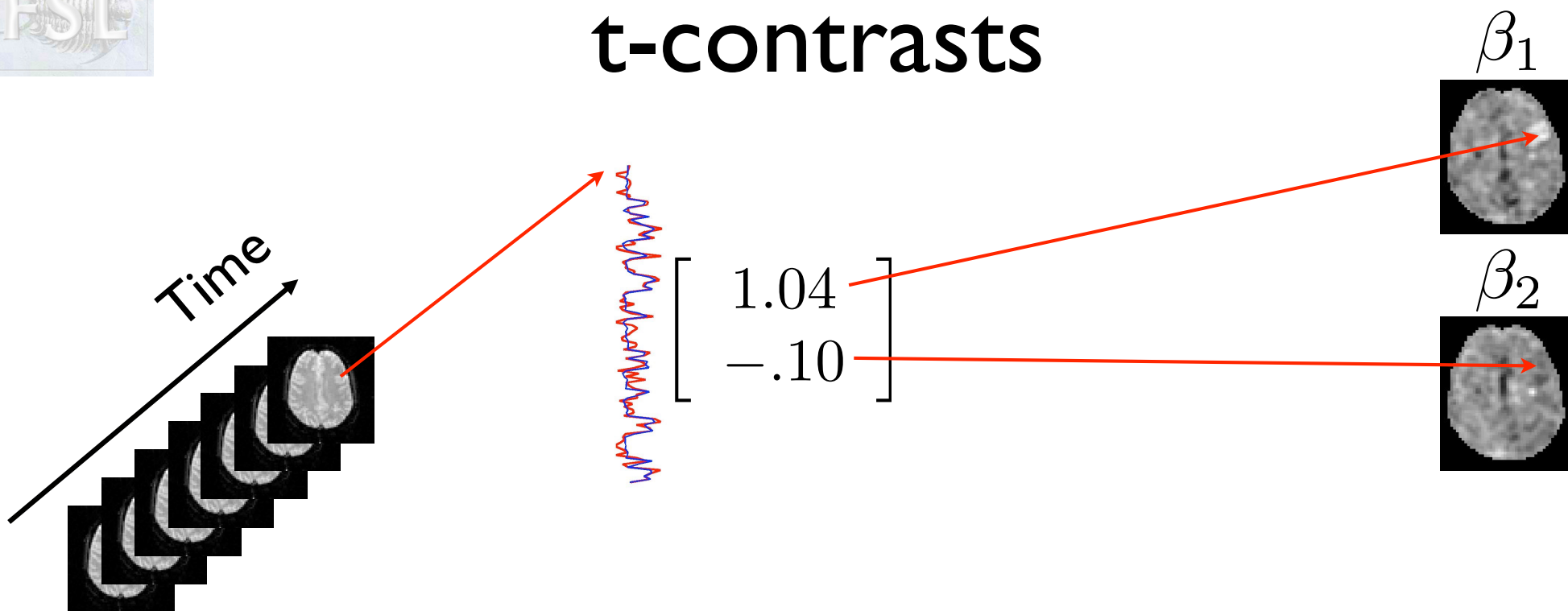
t-contrasts

- $[1\ 0]$: EV1 only (i.e. Generation vs rest)
- $[0\ 1]$: EV2 only (i.e. Shadowing vs rest)
- $[1\ 1]$: EV1 + EV2 (Mean activation)
- $[-1\ 1]$: EV2 - EV1 (More activated by Shadowing than Generation)
- $[1\ -1]$: EV1 - EV2 (More activated by Generation than Shadowing (*t*-tests are directional))



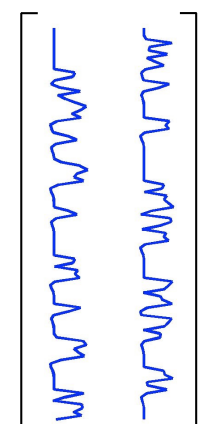


t-contrasts



Contrast weight vector: $\begin{bmatrix} 1 & -1 \end{bmatrix}$

$$\text{COPE} = 1 \times 1.04 - 1 \times -0.10 = 1.14$$



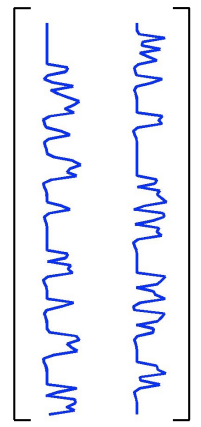
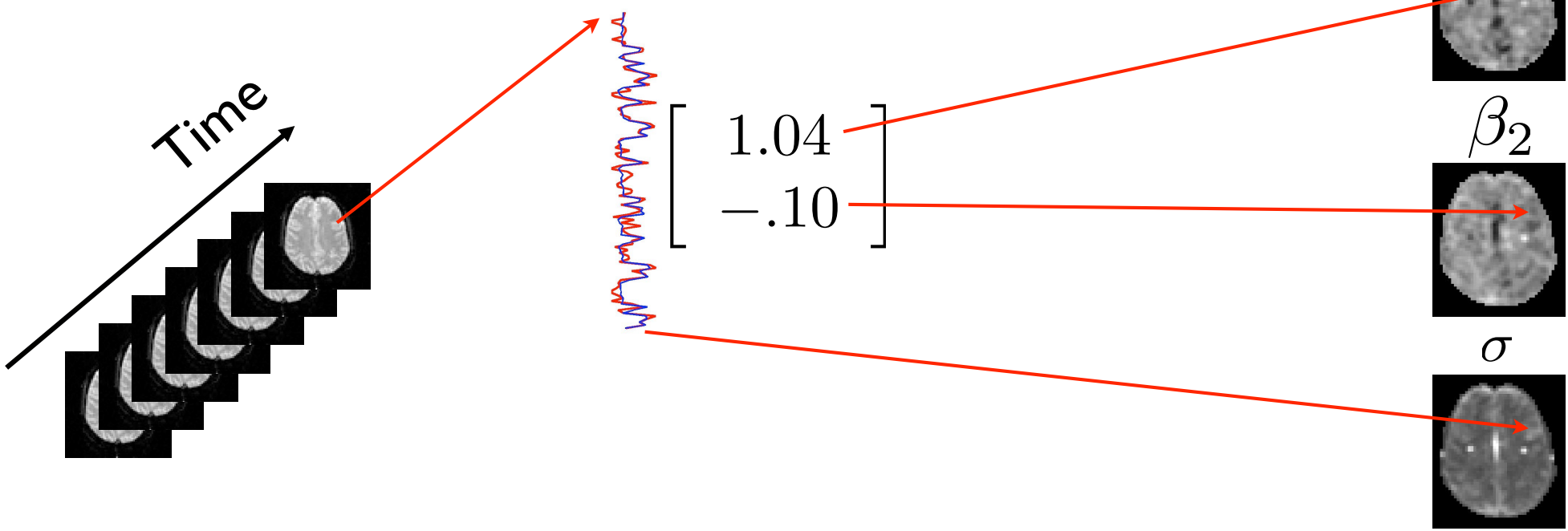
Model

$$\text{COPE} = \text{Image} = \beta_1 - \beta_2$$

The equation shows the Contrast of Parameters (COPE) as the difference between two brain slices, β_1 and β_2 . The first slice is the result of the contrast operation, and the second slice is the difference between the two input slices.



t-contrasts

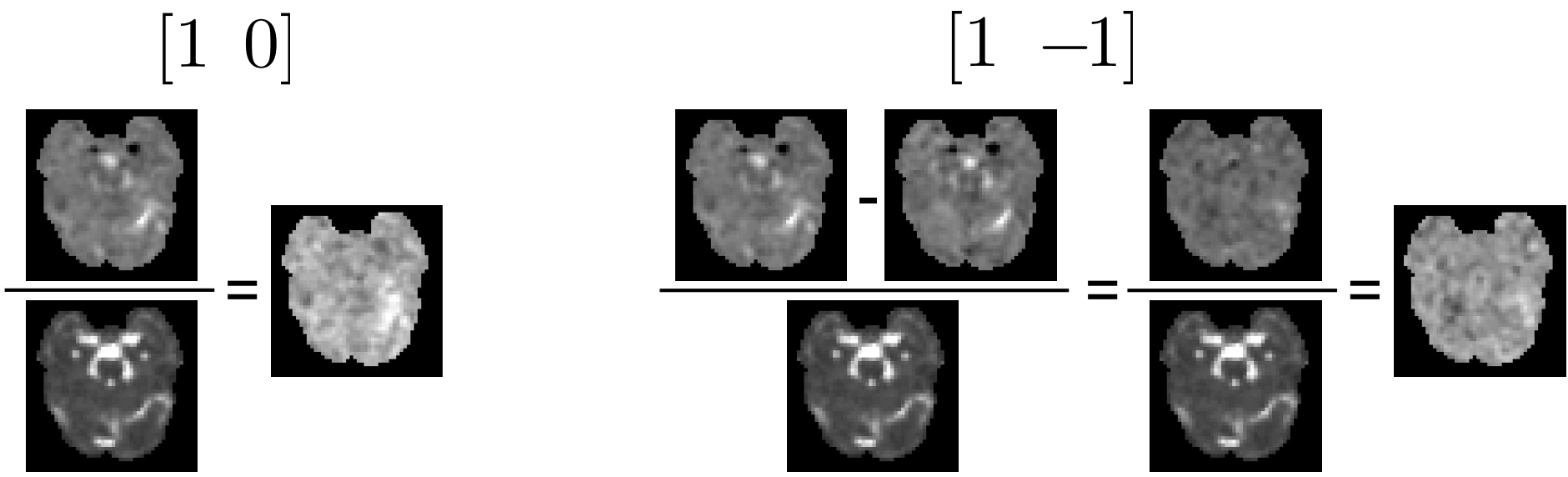
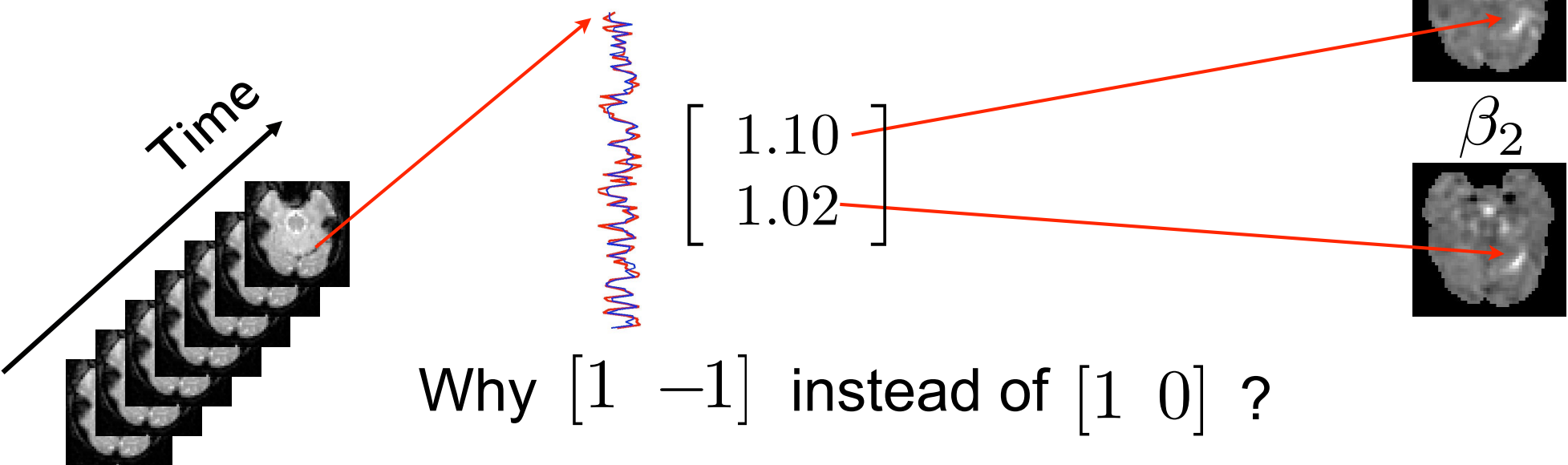


Model

$$t = \frac{\text{COPE}}{\text{std}(\text{COPE})} = \frac{\text{[Brain Slice } \beta_1 \text{]}}{\text{[Brain Slice } \sigma \text{]}} = \text{[Brain Slice } t \text{]}$$



t-contrasts

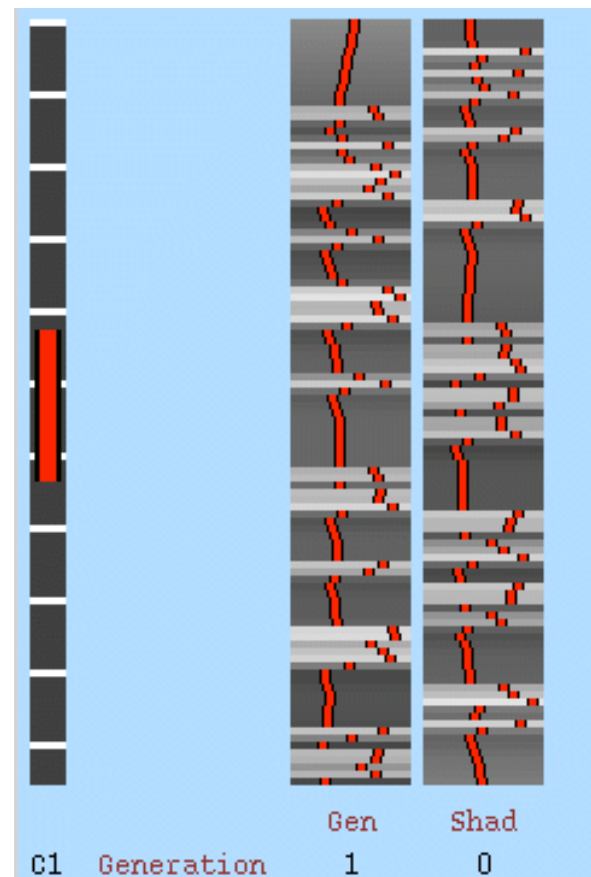




F-contrasts

We have two conditions:
Word Generation and Shadowing

We want to know:
Is there an activation to any condition?



First we ask: Is there activation to Generation?

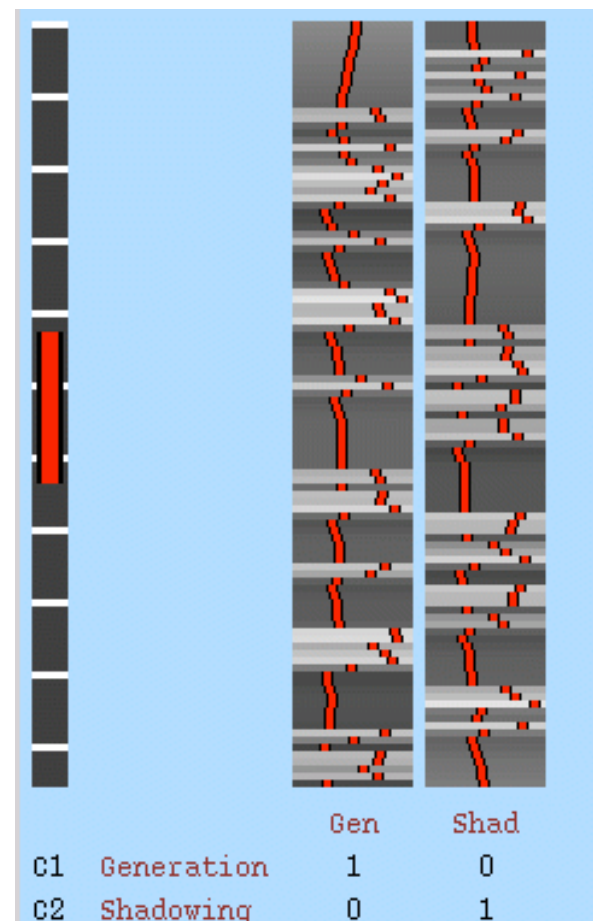
$$\begin{bmatrix} 1 & 0 \end{bmatrix}$$



F-contrasts

We have two conditions:
Word Generation and Shadowing

We want to know:
Is there an activation to any condition?



Then we ask: Is there activation to Shadowing?

$$\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$



F-contrasts

We have two conditions:
Word Generation and Shadowing

We want to know:
Is there an activation to any condition?

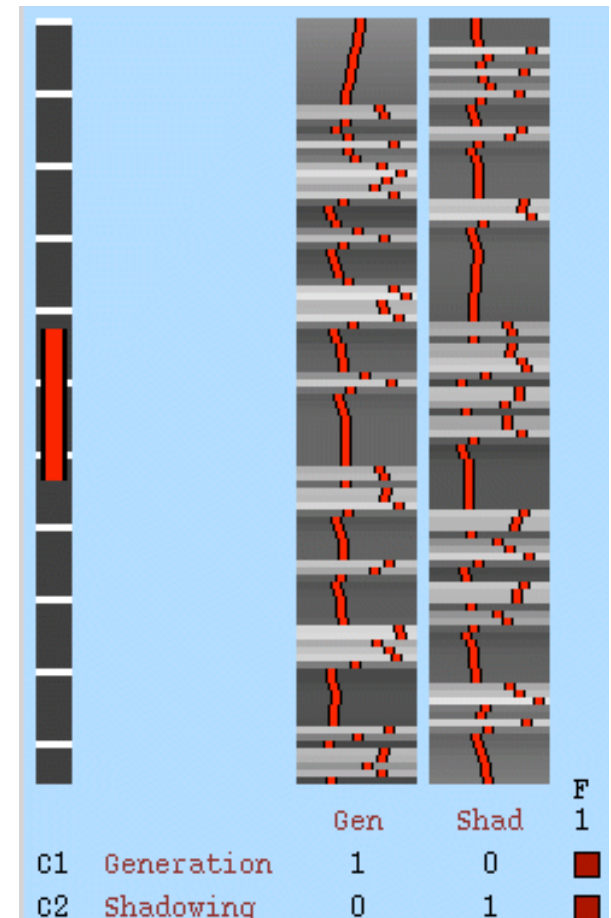
EVs Contrasts & F-tests

Setup contrasts & F-tests for Original EVs

Contrasts 2 F-tests 1

Paste

		Title	EV1	EV2	F1
OC1	<input checked="" type="checkbox"/>	Generation	1	0	<input checked="" type="checkbox"/>
OC2	<input checked="" type="checkbox"/>	Shadowing	0	2	<input checked="" type="checkbox"/>



Then we add the OR

$$\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$



F-contrasts

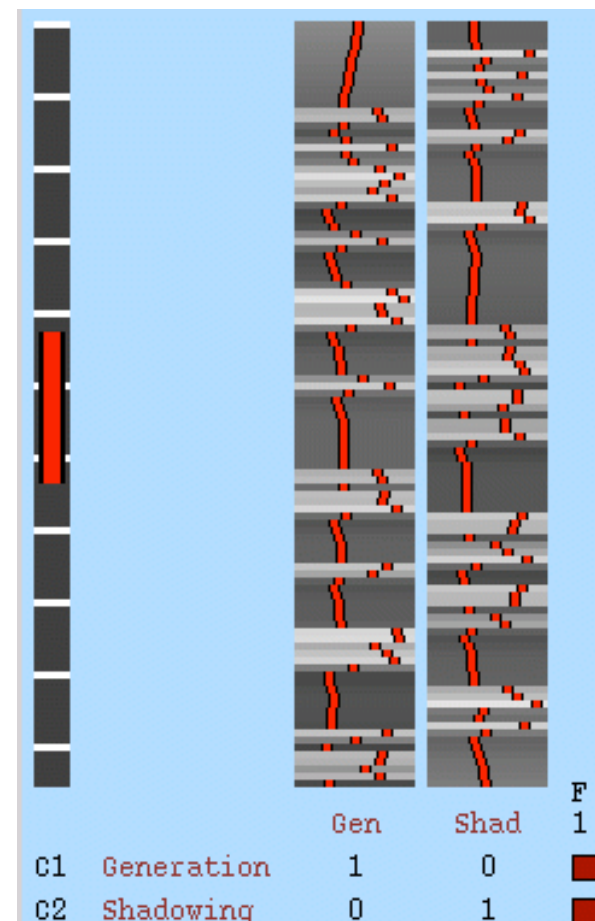
We have two conditions:
Word Generation and Shadowing

We want to know:
Is there an activation to any condition?

Is there an activation to any condition?

Is equivalent to:

Does any regressor explain the
variance in the data?

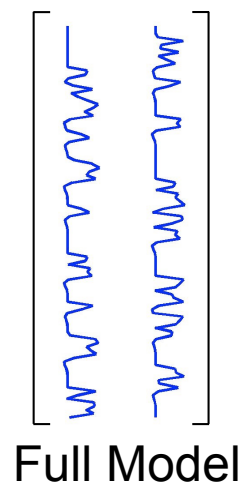


Then we add the OR

$$\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$



F-contrasts

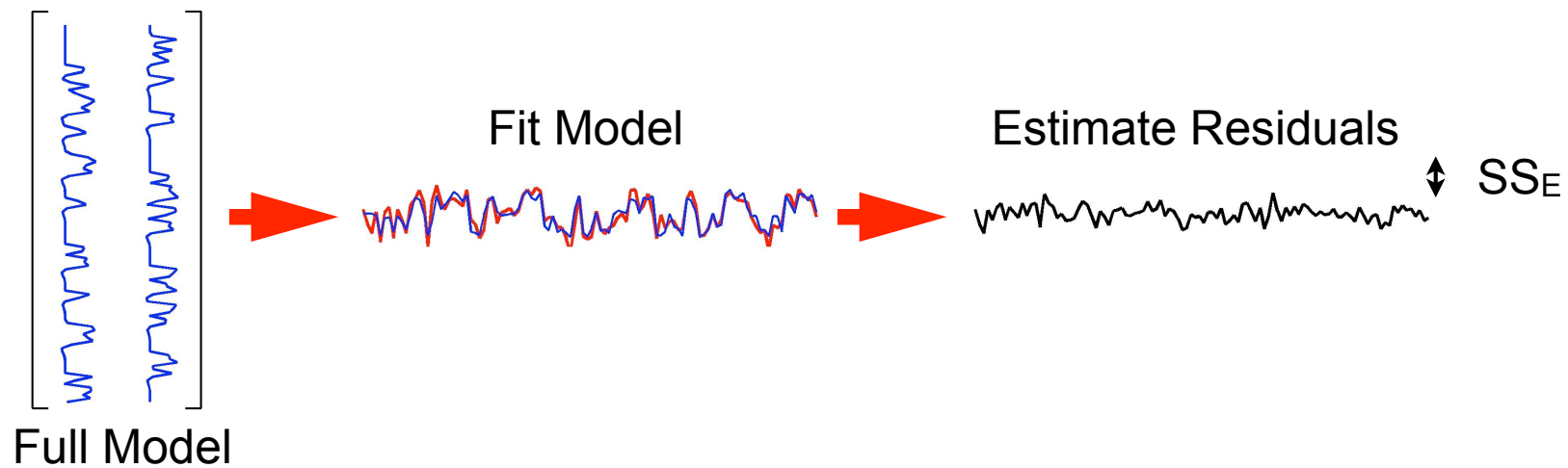


&



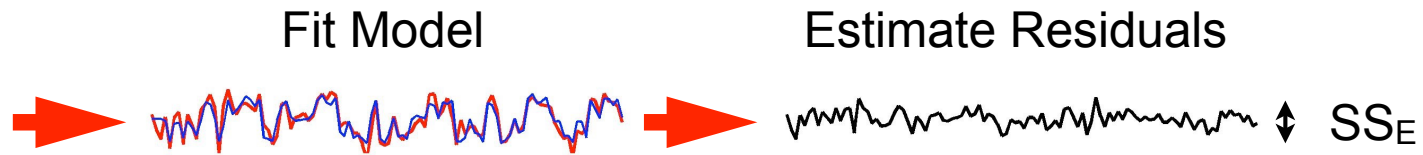
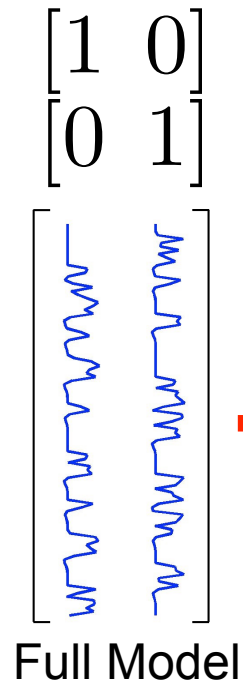


F-contrasts

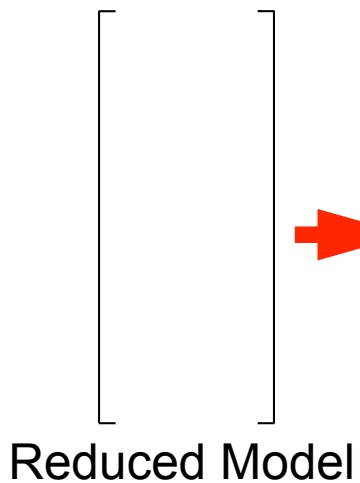




F-contrasts

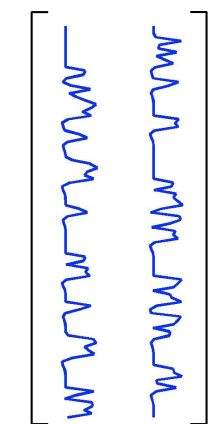


$$F = \frac{SS_R - SS_E}{SS_E} = \frac{\updownarrow - \updownarrow}{\updownarrow}$$

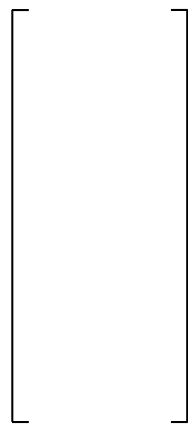




F-contrasts



Full Model



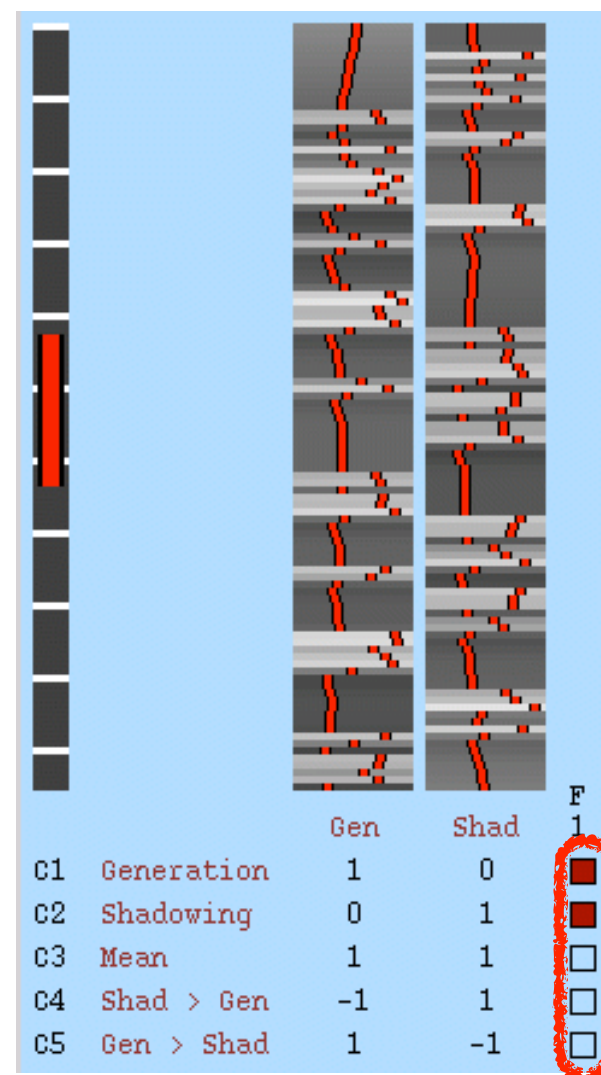
Reduced Model

$$F = \frac{SS_R - SS_E}{SS_E} = \frac{\text{Brain Image} - \text{Brain Image}}{\text{Brain Image}} = \frac{\text{Residual Image}}{\text{Brain Image}} = \text{F-contrast Image}$$



F-contrasts

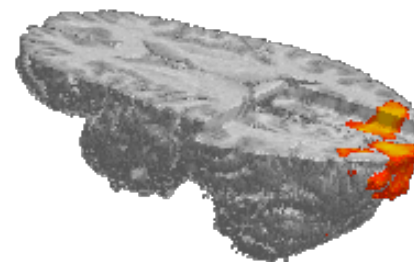
- Two conditions: A, B
- Is any condition significant?
- Set of COPEs form an F-contrast
- Or: “Is there a significant amount of power in the data explained by the combination of the COPEs in the F-contrast?”
- F-contrast is F-distributed





FMRI Modelling and Statistics

- An example experiment
- Multiple regression (GLM)
- T and F Contrasts
- **Null hypothesis testing**
- The residuals
- Thresholding: multiple comparison correction



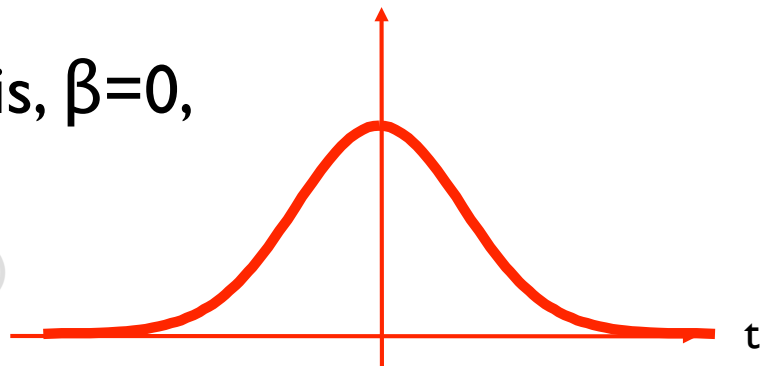


Null Hypothesis Testing

t-statistic: $t = \frac{\hat{\beta}}{\widehat{std}(\beta)}$

Under null hypothesis, $\beta=0$,
t is t-distributed

(what are the chances of that?)

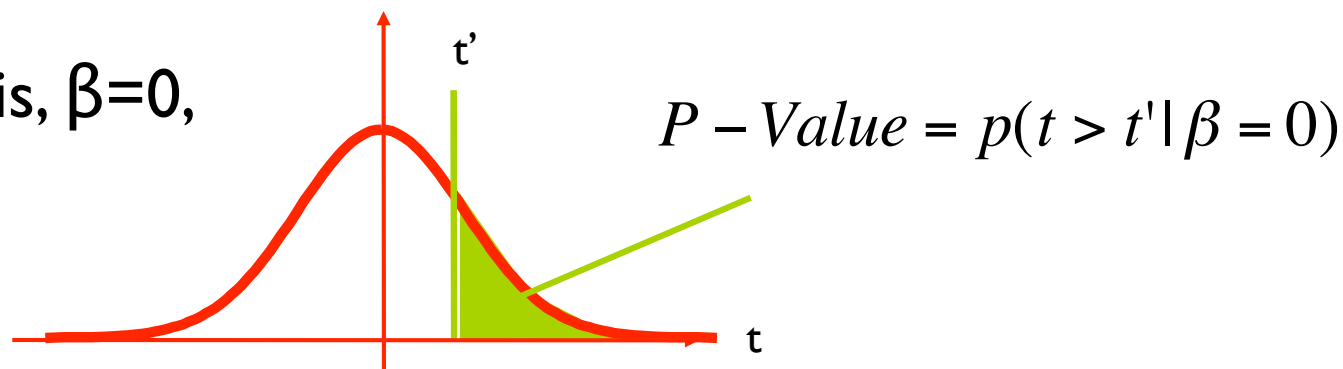




Null Hypothesis Testing

t-statistic: $t = \frac{\hat{\beta}}{\widehat{std}(\beta)}$

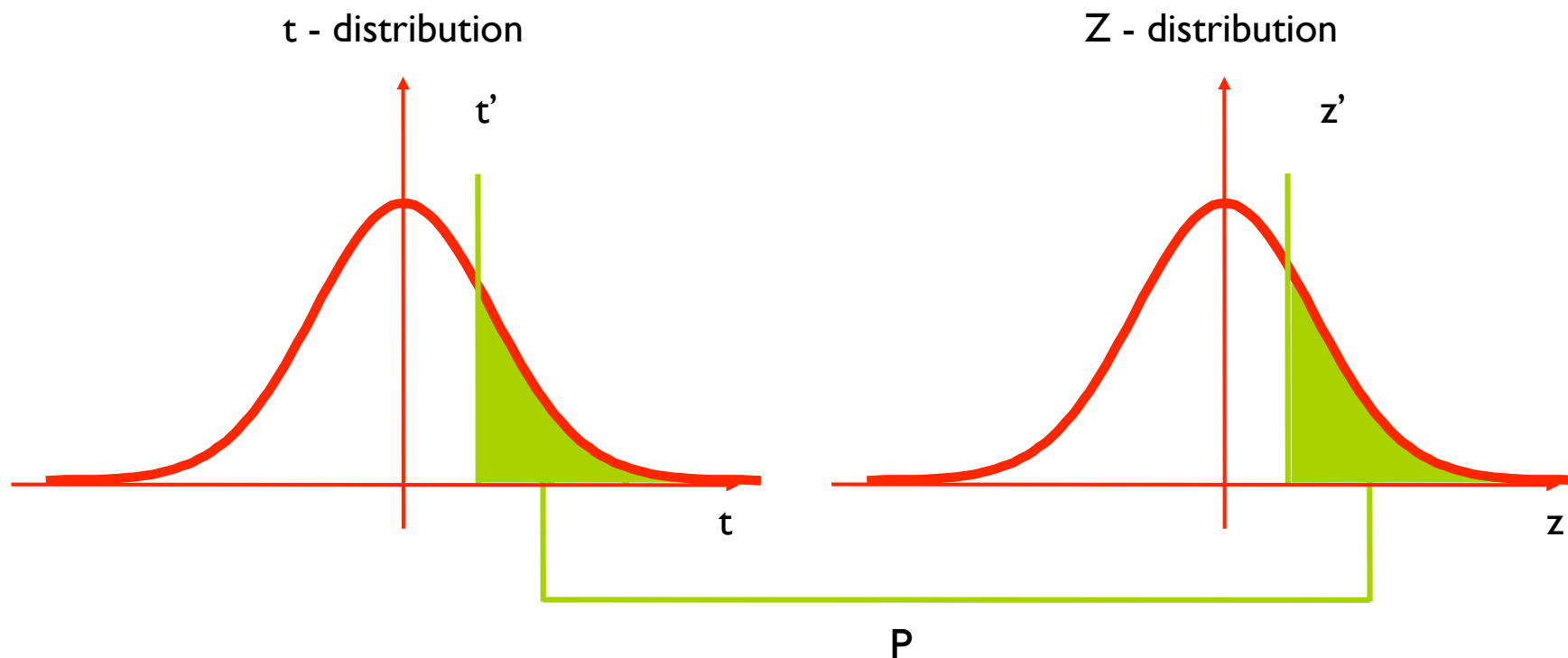
Under null hypothesis, $\beta=0$,
 t is t-distributed



Small P-Value = null hypothesis unlikely
If P-Value < P-threshold then voxel is “active”
P-threshold corresponds to False Positive Rate (FPR)



T to P to Z



- FEAT performs spatial inference on z statistic maps
- Therefore, we convert t statistics to z statistics by equating probabilities under the tails of the distributions ($t' \rightarrow p \rightarrow z'$)

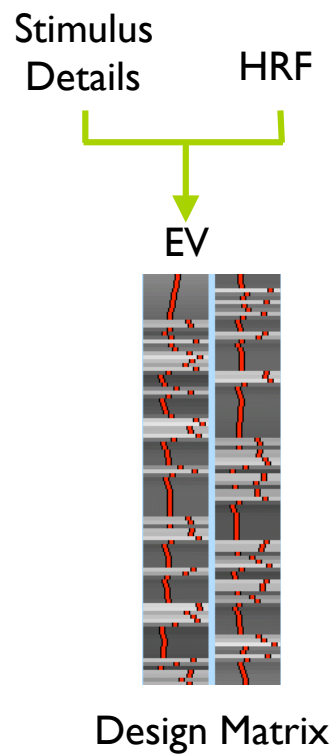


Summary of what we learned so far

- Once you have fitted your model and estimated your parameters you can ask directed questions of your data using contrasts.
- A contrast can be a t -contrast, which asks relatively specific question, or an F -contrast, which can ask more general questions.
- A t - or F -value specifies the “degree of surprise” of the data (given that the null-hypothesis is true).
- A t - or F -value can be transformed to a z -score with the same p -value (degree of surprise).

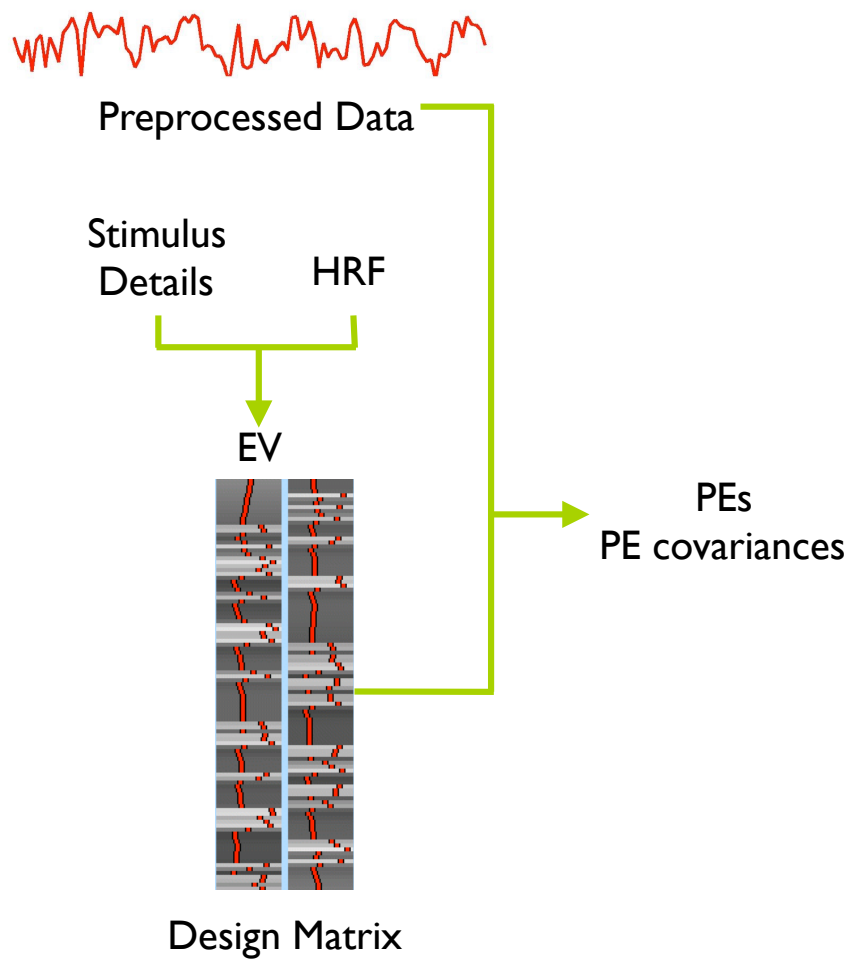


FEAT Schematic



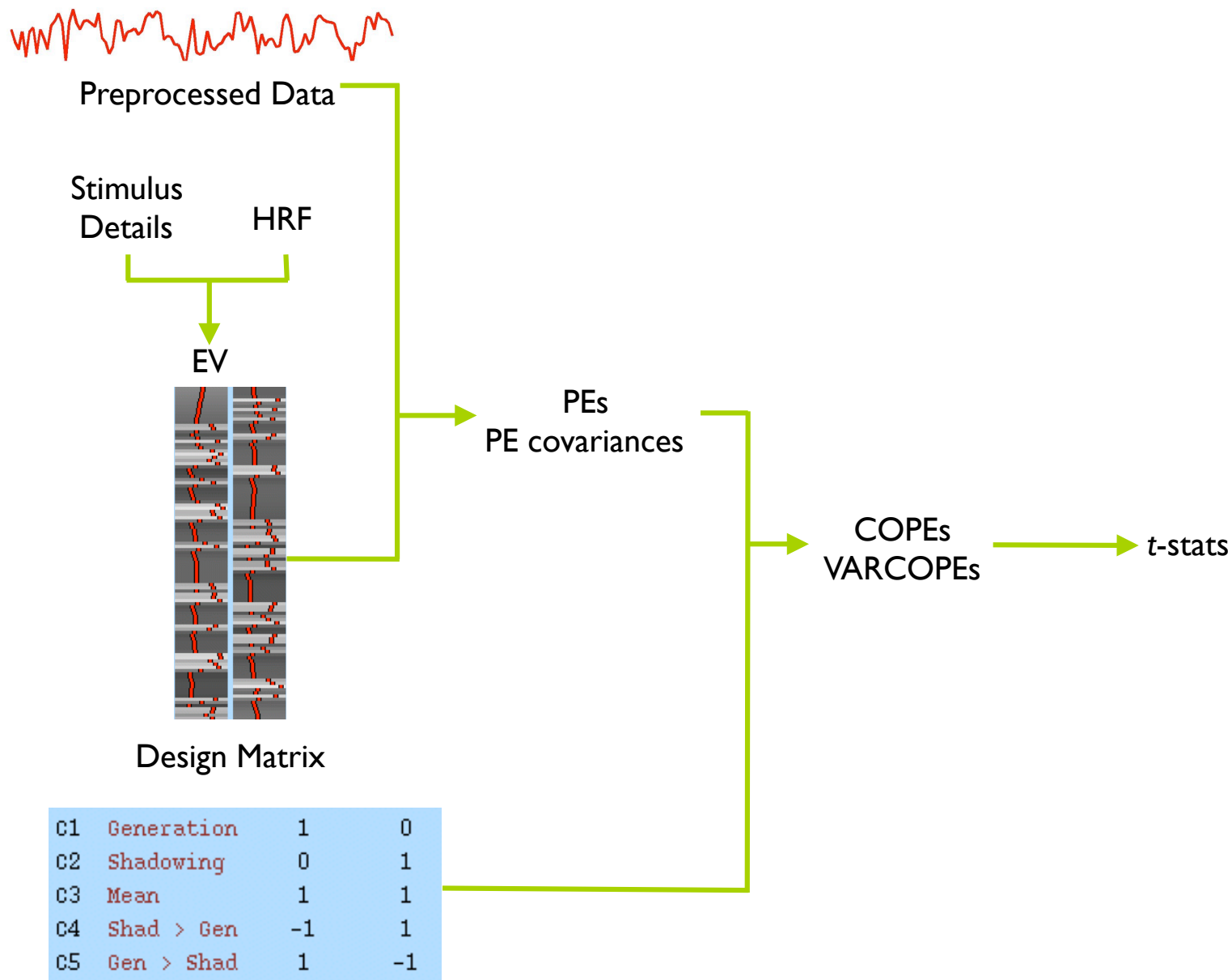


FEAT Schematic



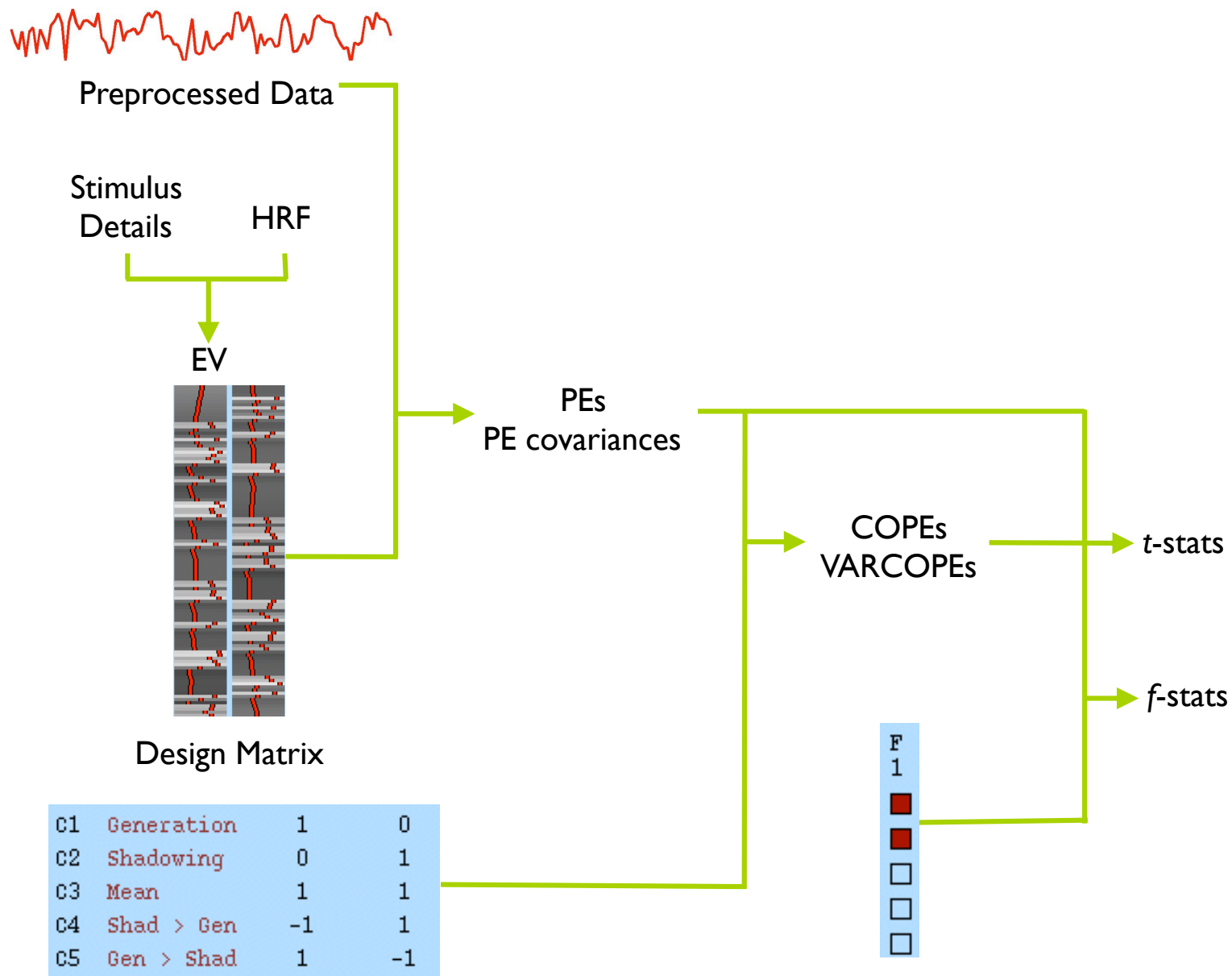


FEAT Schematic



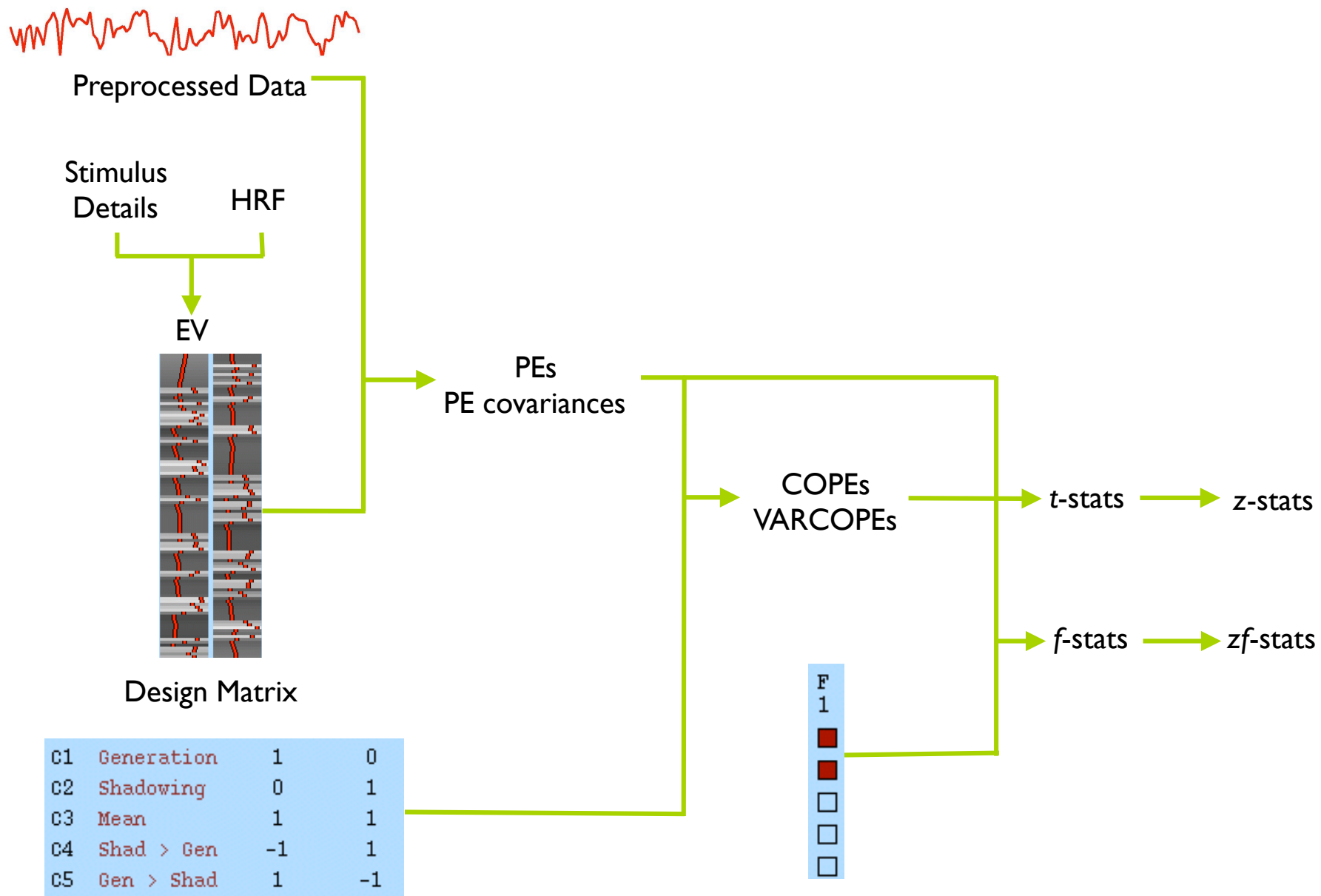


FEAT Schematic





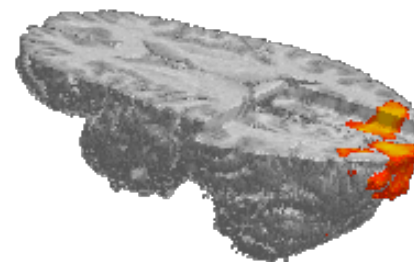
FEAT Schematic





FMRI Modelling and Statistics

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- **The residuals**
- Thresholding: multiple comparison correction





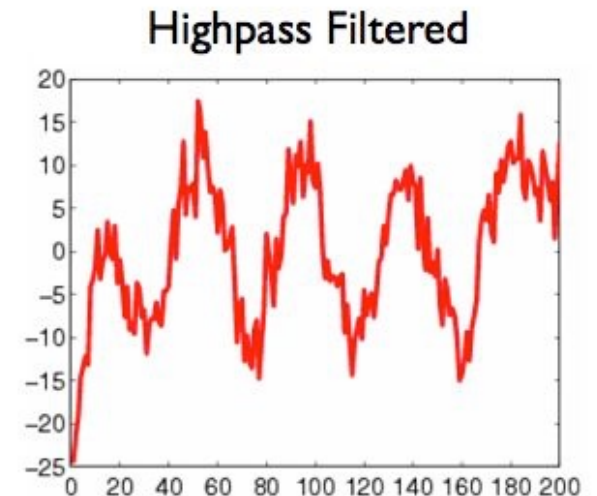
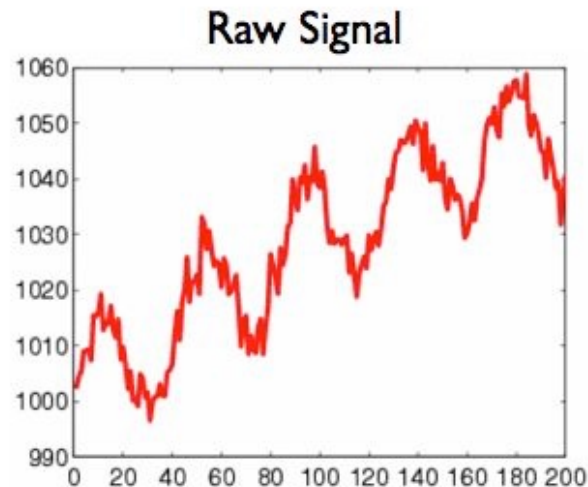
Choosing High-Pass Filter Cut-off

- Can use the tool *cutoffcalc* to determine a good cut-off value

Remember that
MJ mentioned
highpass filtering?



Temporal Filtering: Highpass



- Removes low frequency signals, including linear trend
- Must choose cutoff frequency carefully (lower than frequencies of interest = longer period)

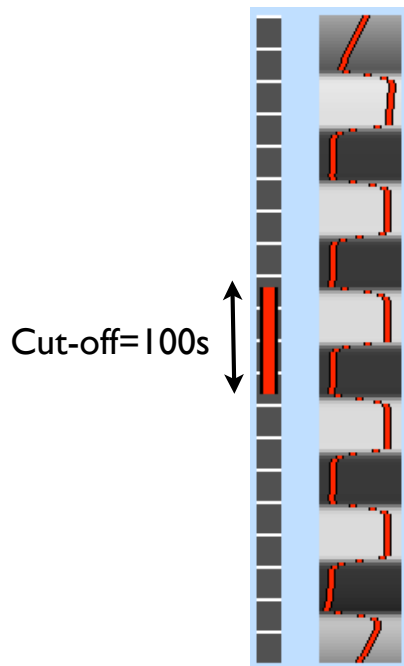


Choosing High-Pass Filter Cut-off

- Can use the tool *cutoffcalc* to determine a good cut-off value
- OR
- Set by hand, but make sure model is not badly affected

Example: Boxcar EV with period

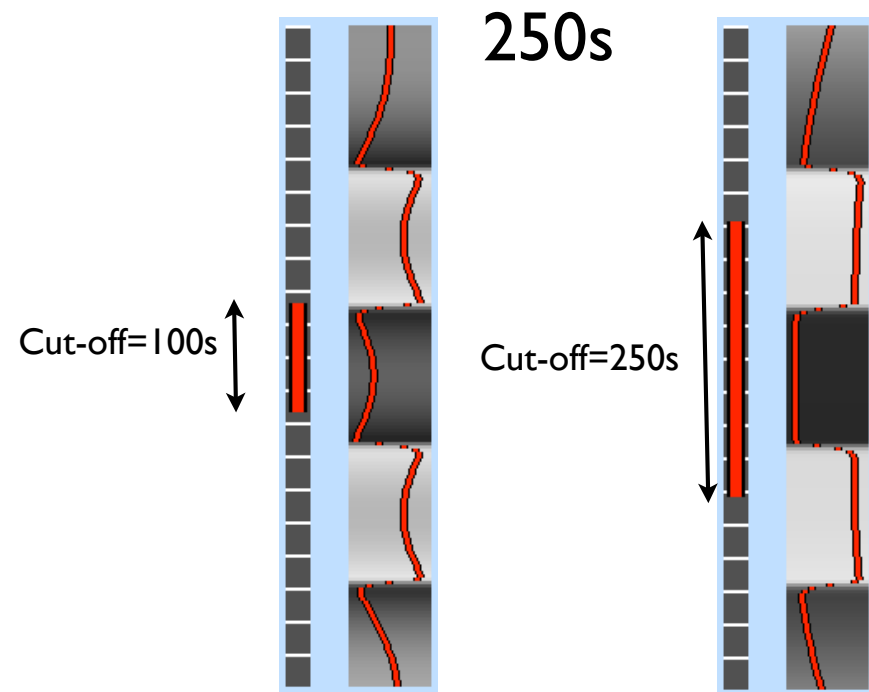
100s



Negligible effect on EV, so use cut-off of 100s

Example: Boxcar with period

250s

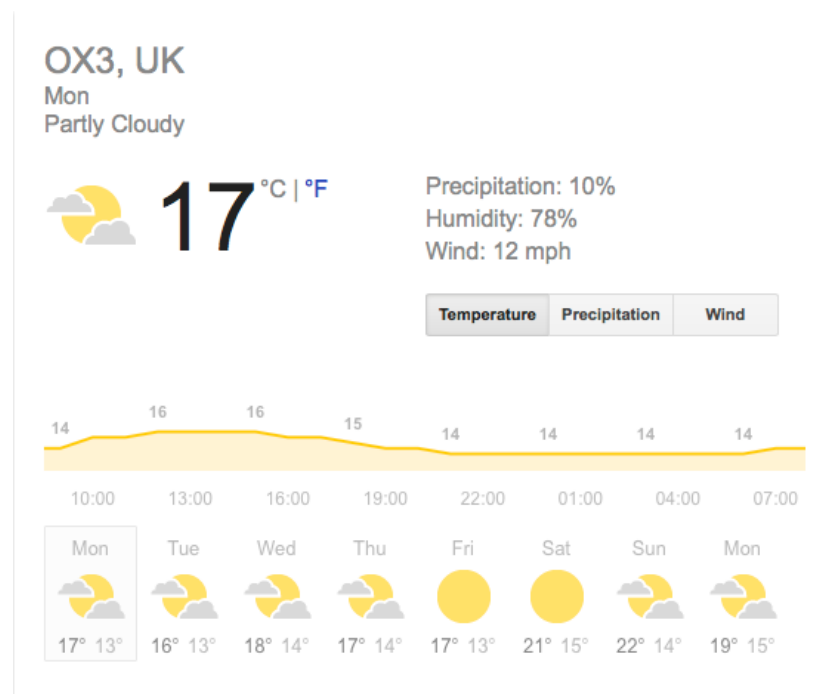


Substantial effect on EV, so need longer cut-off

Negligible effect on EV, so use cut-off of 250s



Non-independent/Autocorrelation/ Coloured FMRI noise



Uncorrected, this causes:

- biased stats (increased false positives)
- decreased sensitivity

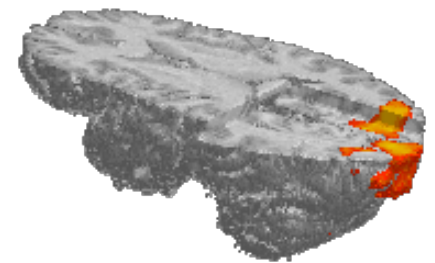
FSL fixes it for you in FEAT!

Cannot use randomise (see later) because of autocorrelation



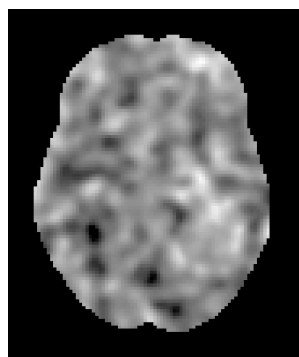
FMRI Modelling and Statistics

- An example experiment
- Multiple regression (GLM)
- T and F Contrasts
- Null hypothesis testing
- The residuals
- **Thresholding: multiple comparison correction**

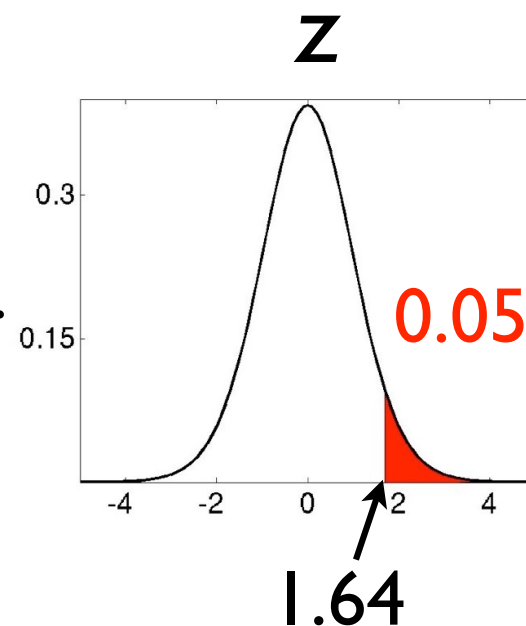




What happens when we apply “standard” statistical testing to imaging data?



z-map where each voxel $\sim N$.
Null-hypothesis true everywhere, i.e.
NO ACTIVATIONS



z-map
thresholded at
1.64



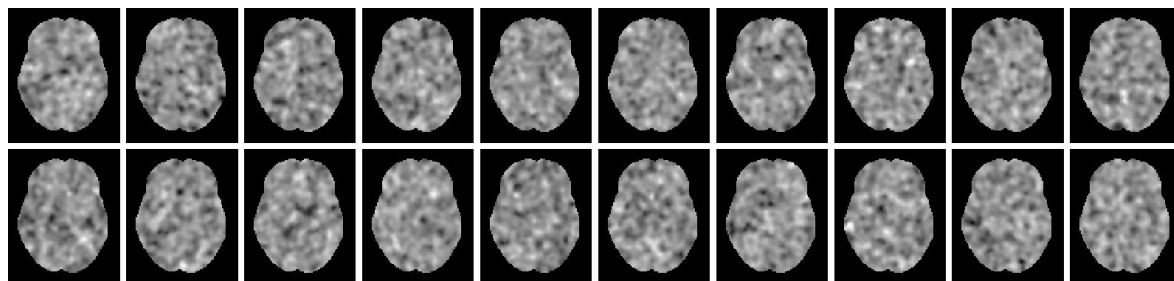
16 clusters
288 voxels
~5.5% of the voxels

That's a LOT of false positives



What we really want

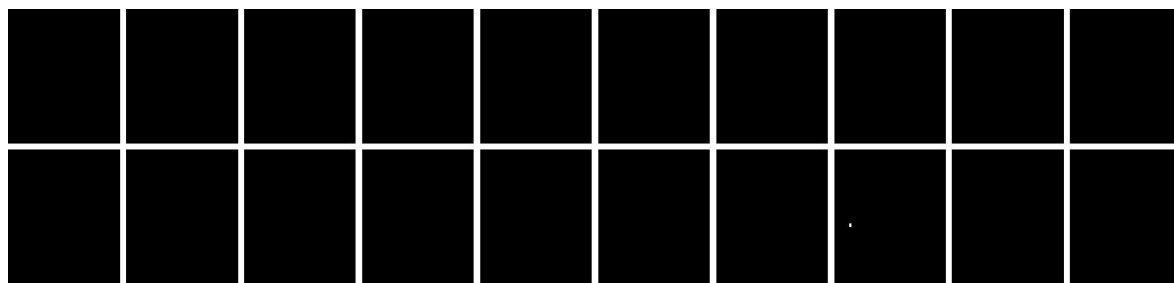
Let's say we perform a series of identical studies



Each z-map is the end result of a study

Let us further say that the null-hypothesis is true

We want to threshold the data so that only once in 20 studies do we find a voxel above this threshold



There will be a whole talk on how to find such a threshold



Summary

- The GLM is used to summarise data in a few parameters that are pertinent to the experiment.
- GLM predicts how BOLD activity might change as a result of the experiment.
- We can test for significant effects by using t or f contrasts on the GLM parameters
- When thresholding the number of false positives needs to be controlled across the entire brain

That's all folks

