



Trinity College Dublin

Coláiste na Tríonóide, Baile Átha Cliath

The University of Dublin

Modelling Electric Fields In Ireland And UK For Space Weather Applications

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[4] Dublin Institute for Advanced Studies (DIAS)



**British
Geological Survey**

NATURAL ENVIRONMENT RESEARCH COUNCIL



DIAS

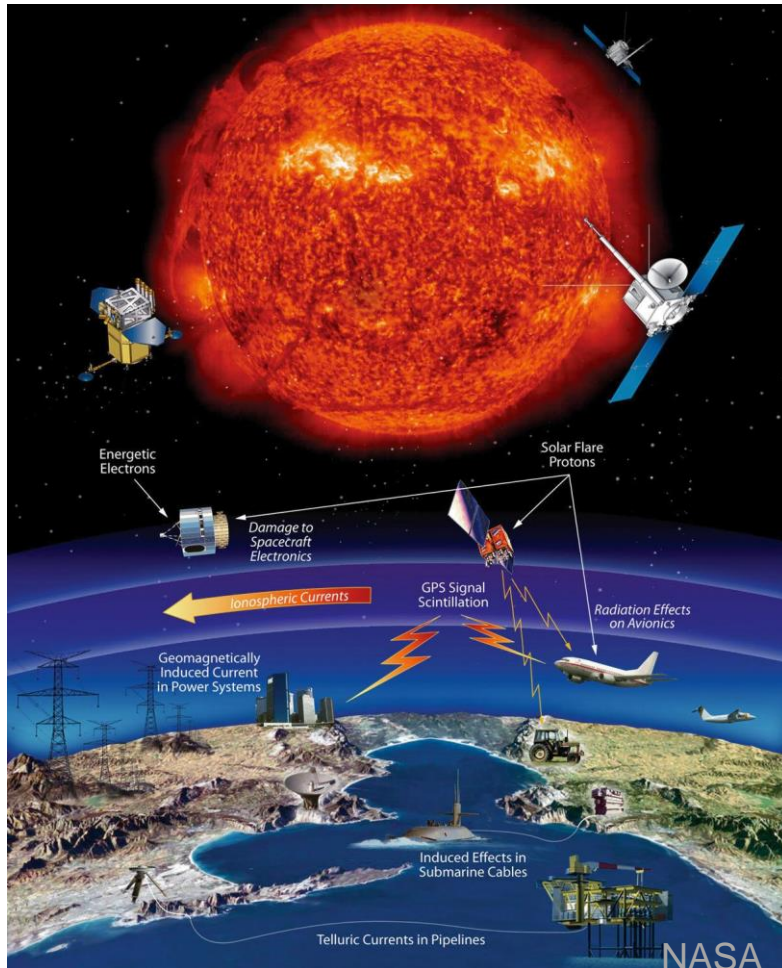
Institiúid Ard-Léinn Bhaile Átha Cliath
Dublin Institute for Advanced Studies



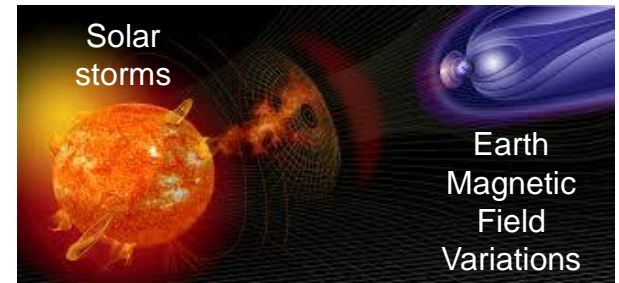
IRISH RESEARCH COUNCIL
An Chomhairle um Thaighde in Éirinn

Why do we want to model the electric fields?

Geomagnetic Induced Currents (GICs)



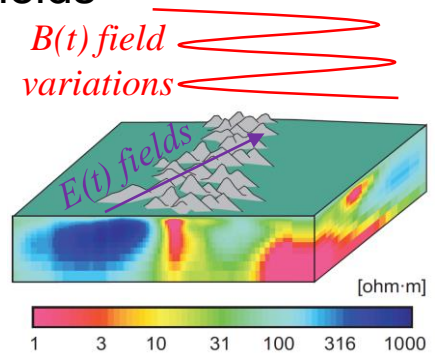
- Solar Activity



- Induced Electric Fields

Faraday's law

$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$$



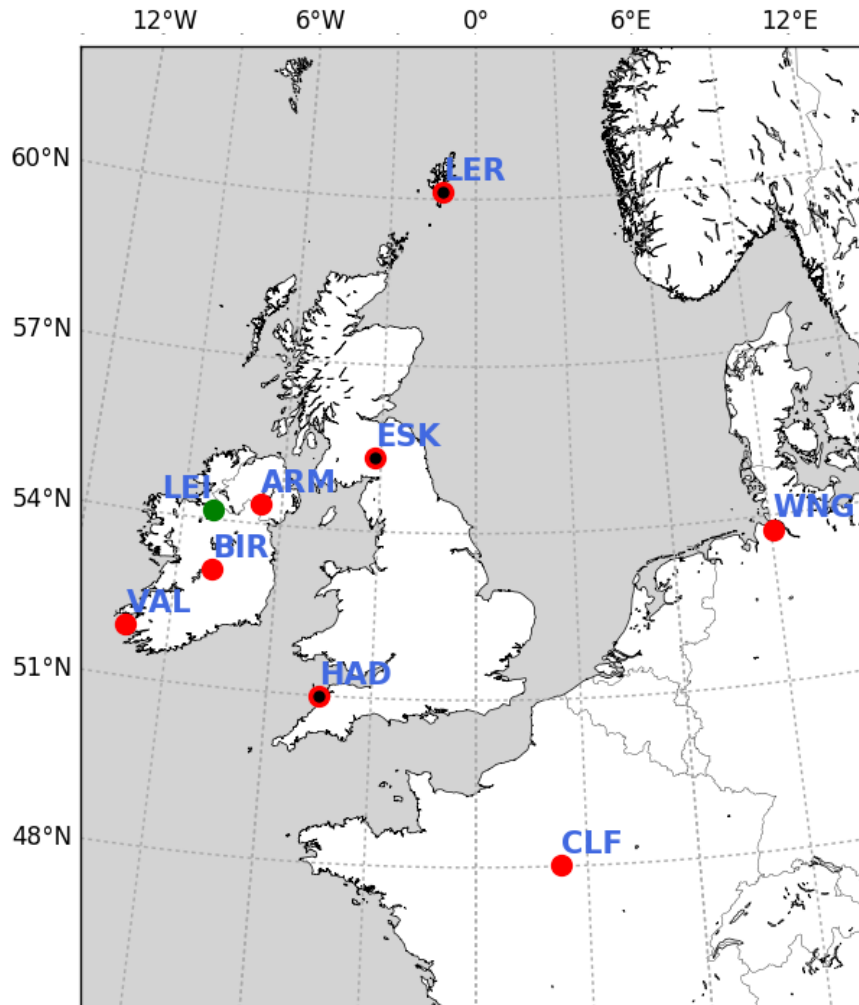
- Power Transmission Network



Induced
Electric
Currents

Area of Interest

Ireland and UK

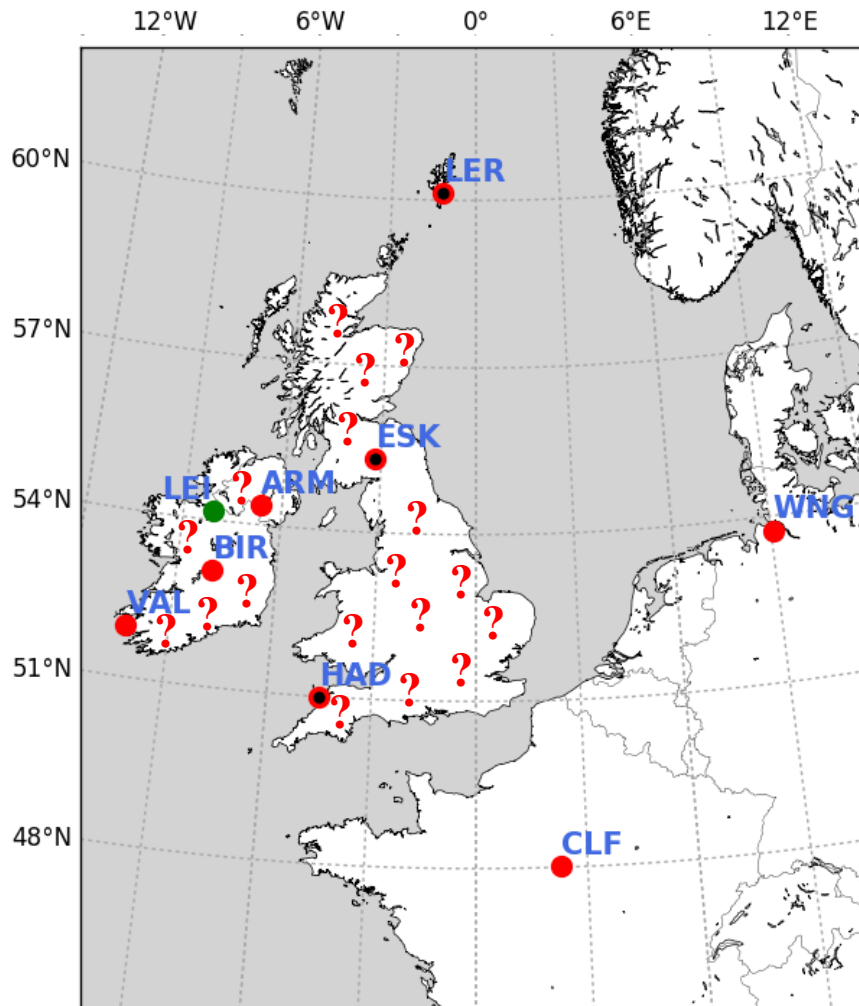


- Permanent Magnetic Observatories
- Permanent Electric Observatories
- Temporary site (electrics and magnetics)

INTERMAGNET & MagIE

Area of Interest

Ireland and UK



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- Permanent Electric Observatories
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How accurate can we model the
electric fields at sites with no
permanent recordings?

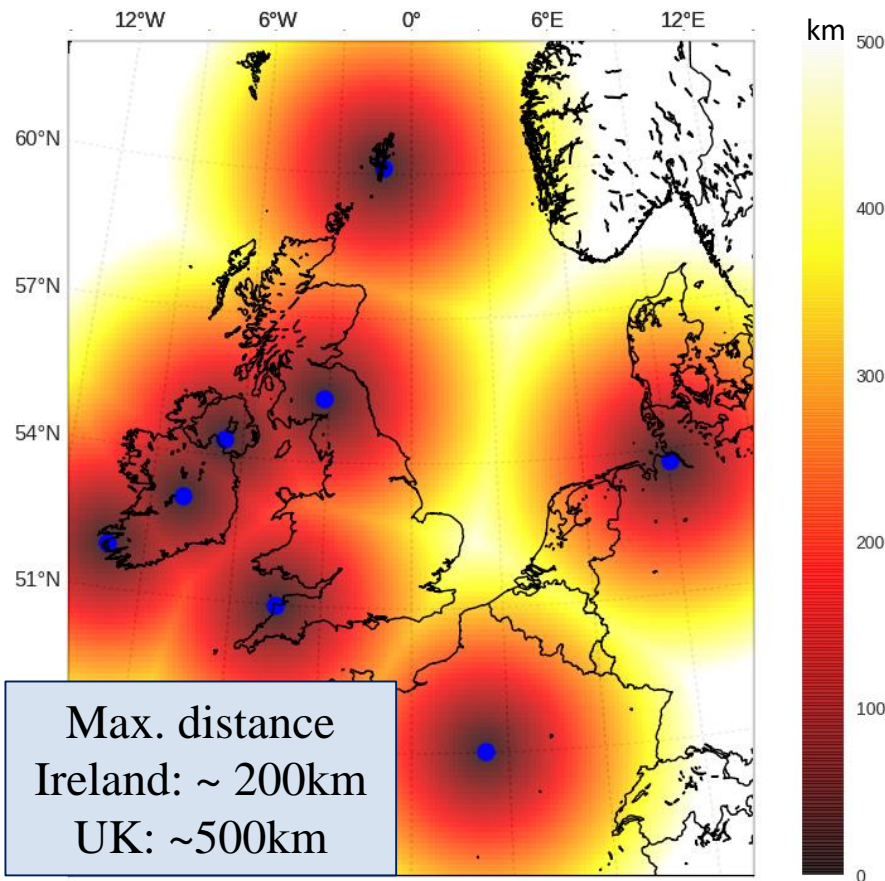
INTERMAGNET & MagIE

Sources of EM fields

Primary Magnetic Field & Influence of the Subsurface Geology

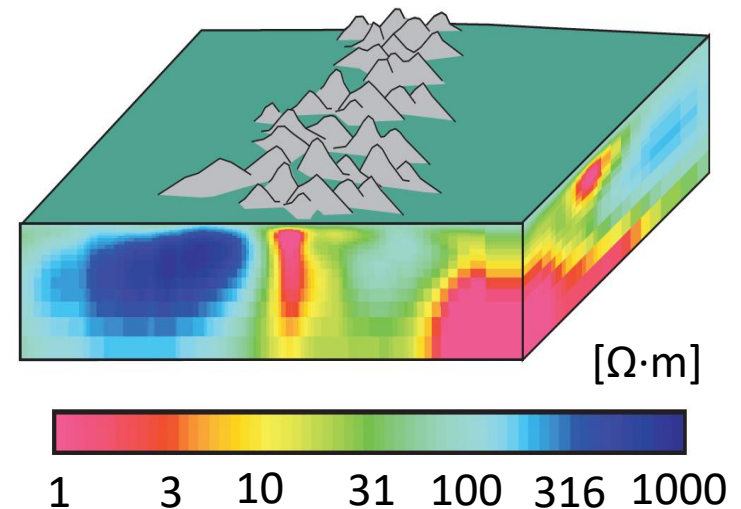
Primary magnetic field

(Interpolate between Magnetic Observatories)



Influence of the geology

(Magnetotelluric geophysical method:
Tensor relationships relating EM fields)

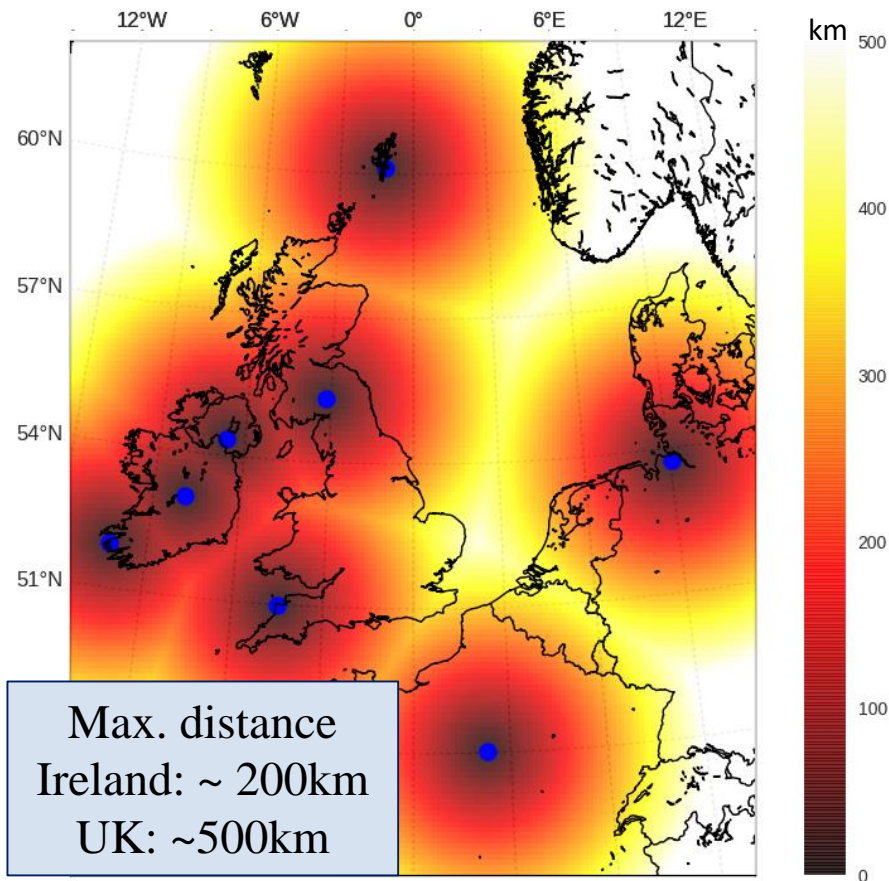


Sources of EM fields

Primary Magnetic Field & Influence of the Subsurface Geology

Primary magnetic field

(Interpolate between Magnetic Observatories)



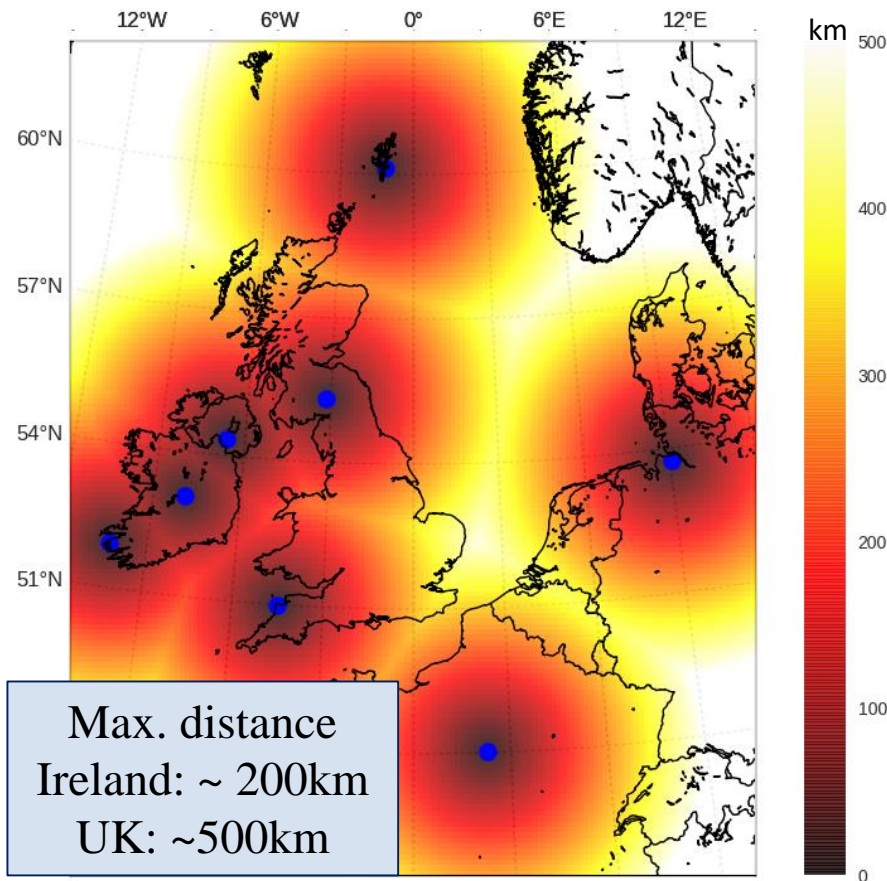
- Spherical elementary current systems (SECS, ionospheric currents)
- Linear interpolation
- Cubic interpolation

Sources of EM fields

Primary Magnetic Field & Influence of the Subsurface Geology

Primary magnetic field

(Interpolate between Magnetic Observatories)



- Spherical elementary current systems (SECS, ionospheric currents)
- ~~Linear interpolation~~
- ~~Cubic interpolation~~

Linear and Cubic interpolation are NOT accurate during storms

Sources of EM fields

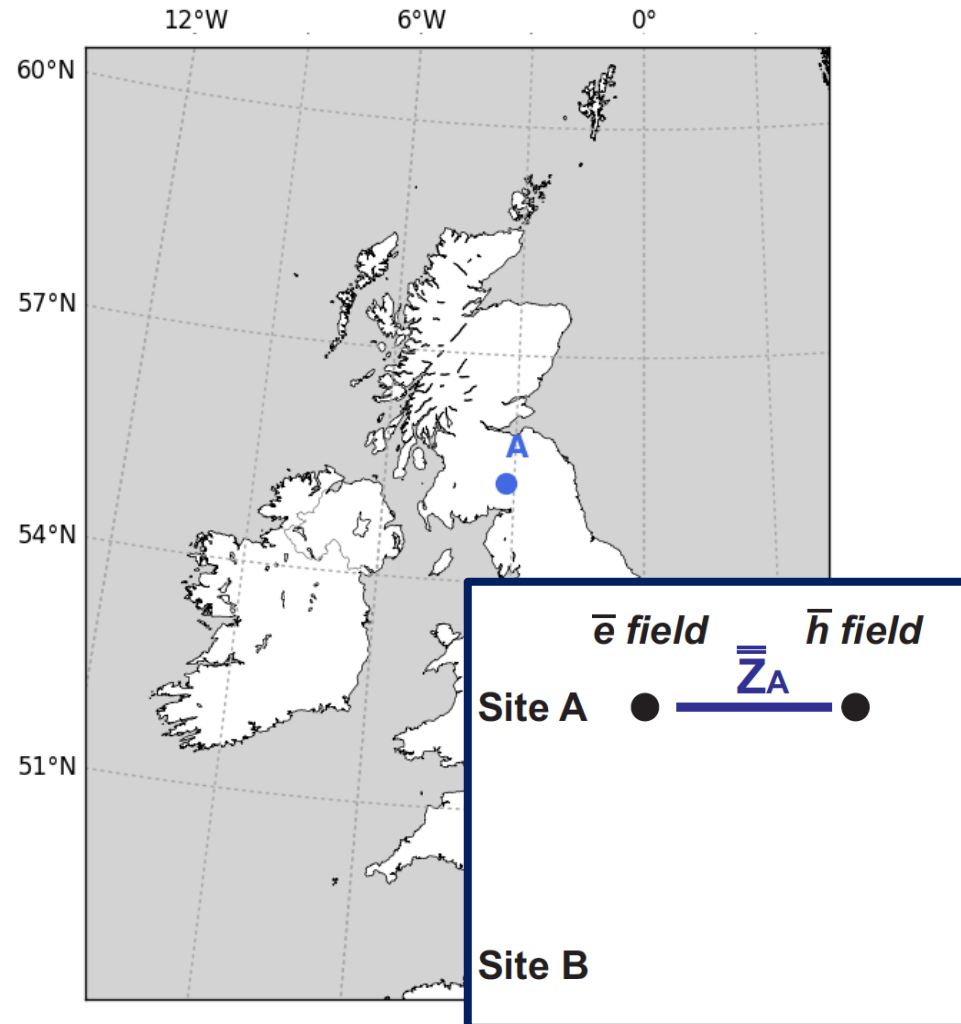
Primary Magnetic Field & Influence of the Subsurface Geology

Tensor relationships

MT Impedance Tensor, \mathbf{Z} (local)

$$\begin{pmatrix} e_x^A(\omega) \\ e_y^A(\omega) \end{pmatrix} = \begin{pmatrix} Z_{xx}(\omega) & Z_{xy}(\omega) \\ Z_{yx}(\omega) & Z_{yy}(\omega) \end{pmatrix} \begin{pmatrix} h_x^A(\omega) \\ h_y^A(\omega) \end{pmatrix}$$

(ω) : Frequency dependence



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Inter-station Impedance Tensor, \mathbf{Z}'

$$\begin{pmatrix} e_x^A(\omega) \\ e_y^A(\omega) \end{pmatrix} = \begin{pmatrix} Z'_{xx}(\omega) & Z'_{xy}(\omega) \\ Z'_{yx}(\omega) & Z'_{yy}(\omega) \end{pmatrix} \begin{pmatrix} h_x^B(\omega) \\ h_y^B(\omega) \end{pmatrix}$$

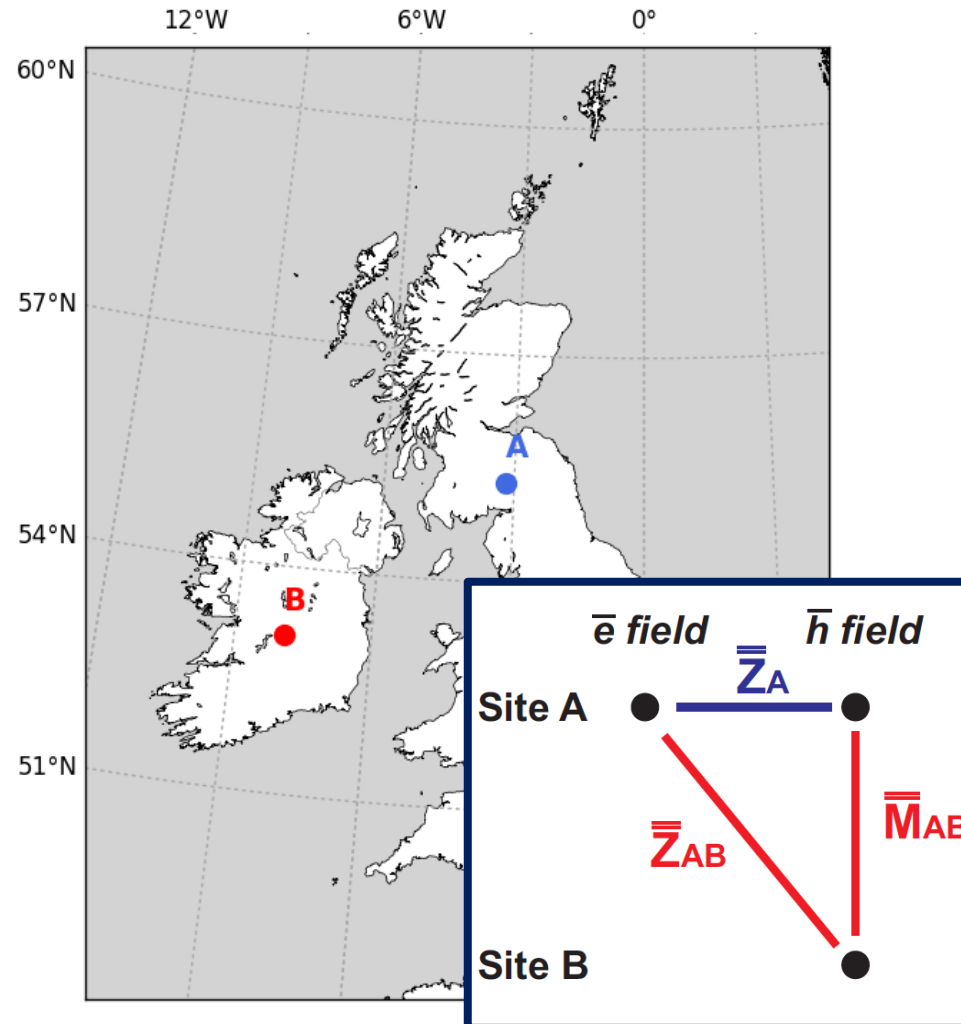
Reference site

Inter-station Horizontal Magnetic, \mathbf{M}'

$$\begin{pmatrix} h_x^A(\omega) \\ h_y^A(\omega) \end{pmatrix} = \begin{pmatrix} M'_{xx}(\omega) & M'_{xy}(\omega) \\ M'_{yx}(\omega) & M'_{yy}(\omega) \end{pmatrix} \begin{pmatrix} h_x^B(\omega) \\ h_y^B(\omega) \end{pmatrix}$$

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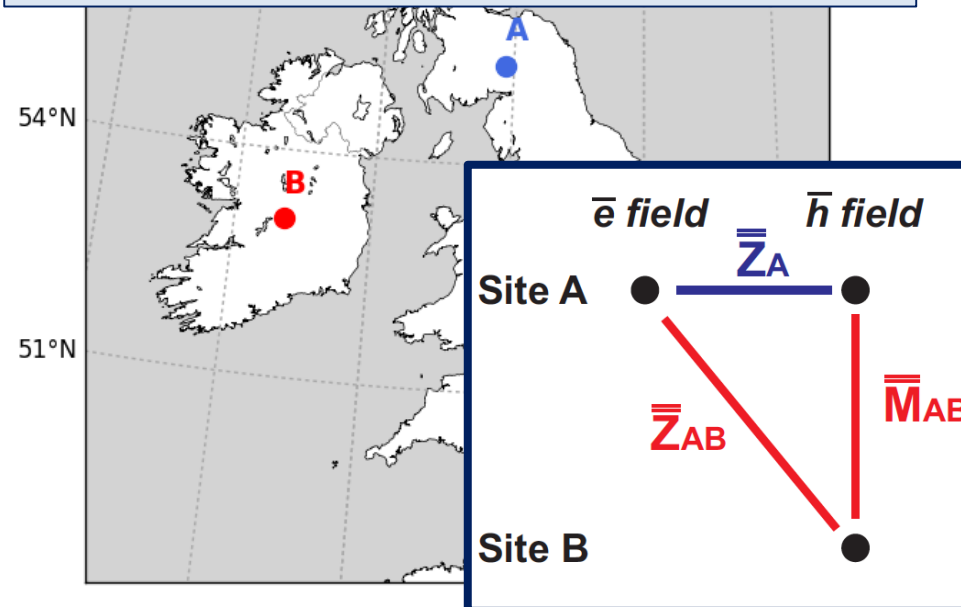
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Reference site

(ω) : Frequency dependence

- Data needs to be measured at least ones at the site of interest to compute the Tensor relationships

- Works under the Plane-Wave approximation: similar primary magnetic field in both sites

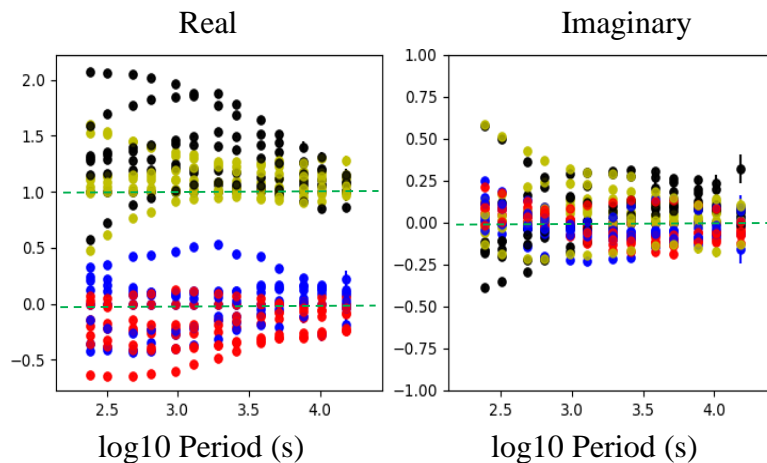


Sources of EM fields

Primary Magnetic Field & Influence of the Subsurface Geology

Influence of the geology on the magnetic field (Secondary/Induced magnetic field)

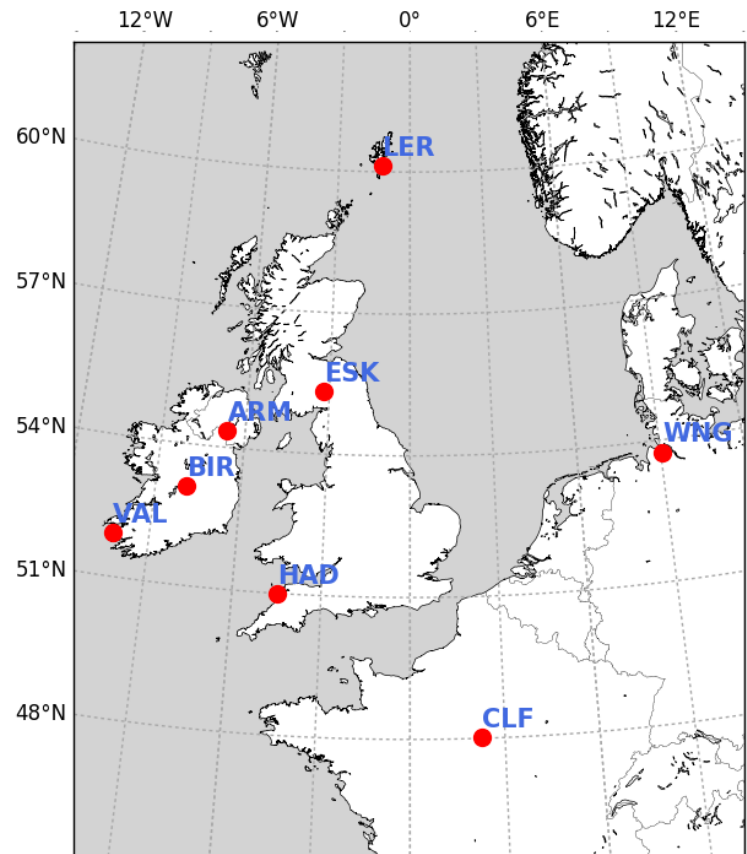
Tensor Relationship between magnetic fields (assuming same magnetic source for all the sites)



$$\begin{pmatrix} h_x^A(\omega) \\ h_y^A(\omega) \end{pmatrix} = \begin{pmatrix} \underline{M'_{xx}(\omega)} & \underline{M'_{xy}(\omega)} \\ \underline{M'_{yx}(\omega)} & \underline{M'_{yy}(\omega)} \end{pmatrix} \begin{pmatrix} h_x^B(\omega) \\ h_y^B(\omega) \end{pmatrix}$$

Site A: ESK

Site B: HAD, ESK, LER, VAL, BIR, ARM



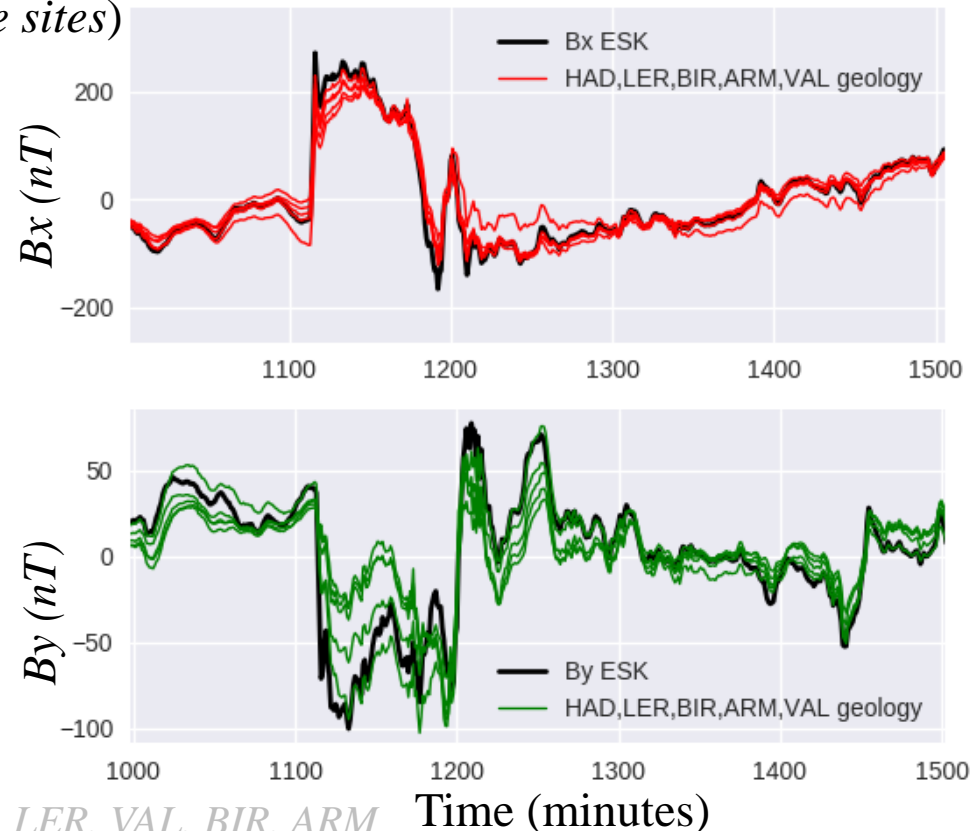
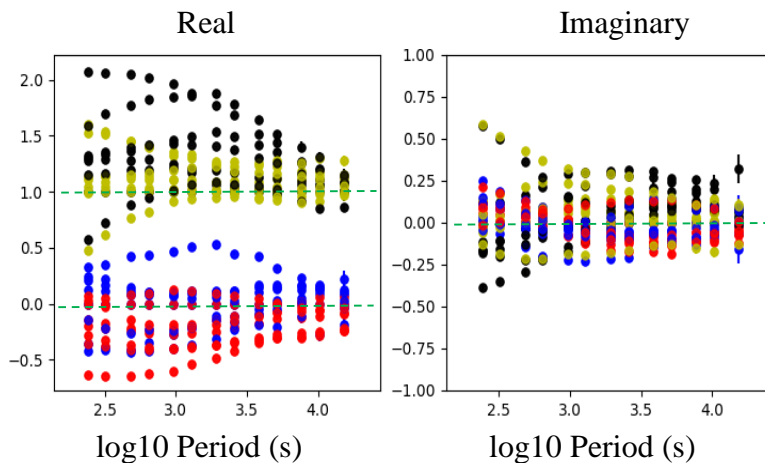
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22-23 June 2015 storm



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Site A: ESK

Site B: HAD, ESK, LER, VAL, BIR, ARM

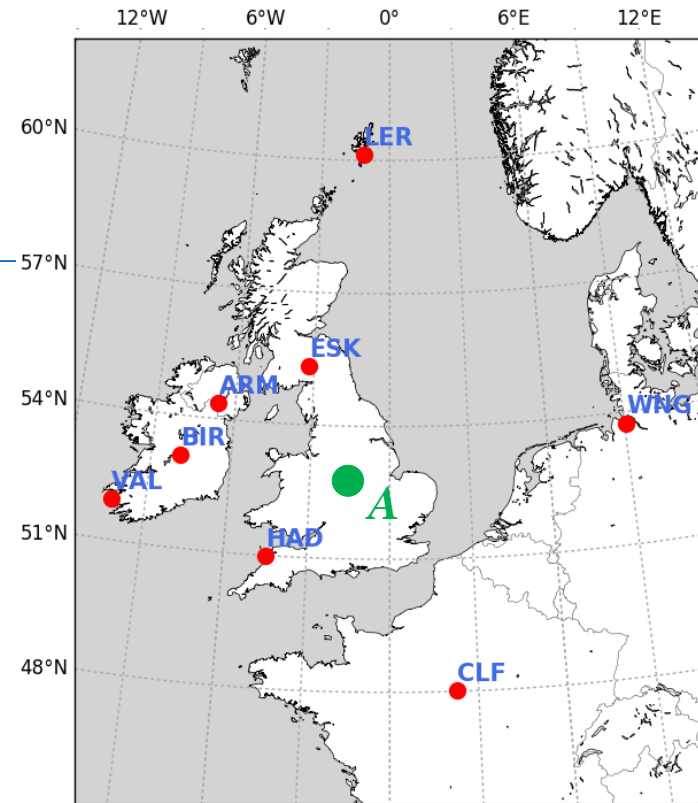
Modelling E fields

Testing different approaches

Method 1

$$E_T^A = Z^A B^A$$

B^A as a result of SECS interpolation
using measured magnetic fields as inputs



Modelling E fields

Testing different approaches

Method 1

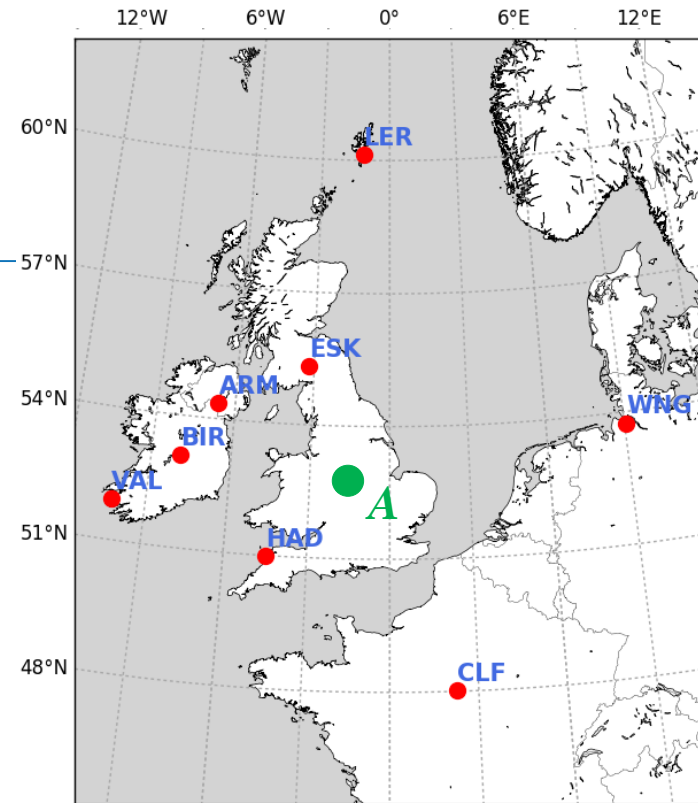
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Method 2

“Total” = “regional” + “local”

$$E_T^A = E_{reg}^A + E_{loc}^A$$



Modelling E fields

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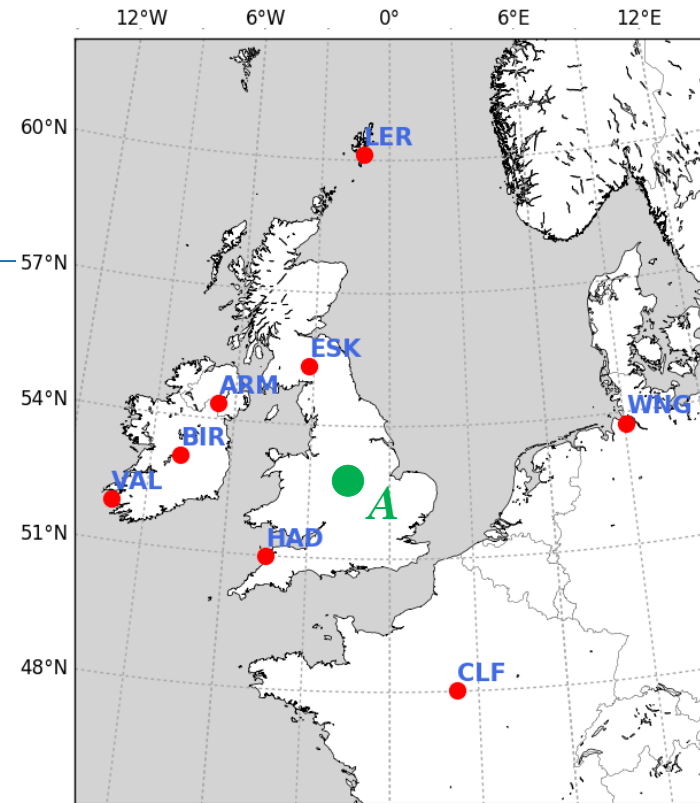
$$E_T^A = E_{reg}^A + E_{loc}^A$$

“regional”

$$E_{reg}^A = Z^{AMr} B^{Mr}$$

Not account for different magnetic
sources (plane wave approx.)

*Mr: Magnetic Reference site, such as CLF
(less affected by local storms)*



Modelling E fields

Testing different approaches

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B^A as a result of SECS interpolation
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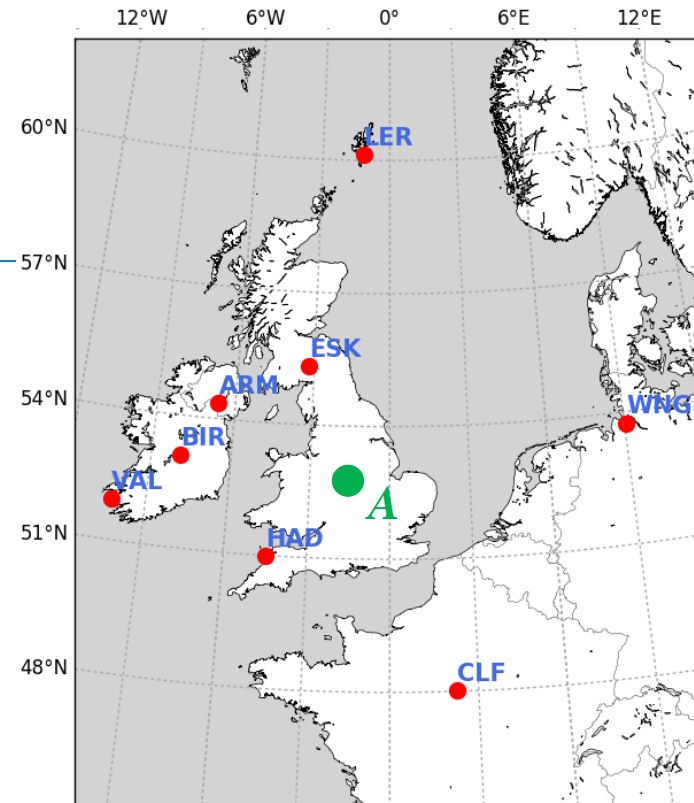
“local”

$$E_{loc}^A = Z^A B_{loc}^A$$

Correction for local storms

B_{loc}^A as a result SECS interpolation using
local magnetic storms as input (B_{loc}^i for $i =$
VAL, BIR, ARM, LER, ESK, HAD ...).

$$B_{loc}^i = B^i - M^{iMr} B^{Mr}$$



Modelling E fields

Testing different approaches

Method 1

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B^A as a result of SECS interpolation
using measured magnetic fields as inputs

Method 2

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“regional”

“local”

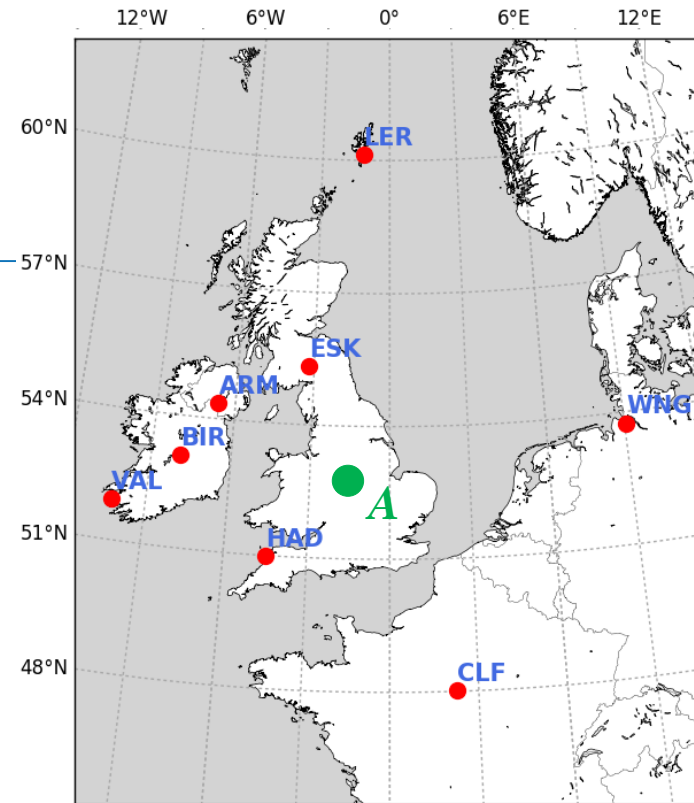
$$E_{reg}^A = Z^{AMr} B^{Mr}$$

$$E_{loc}^A = Z^A B_{loc}^A$$

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Correction for local storms

We aim to reduce the influence of the
interpolation methods



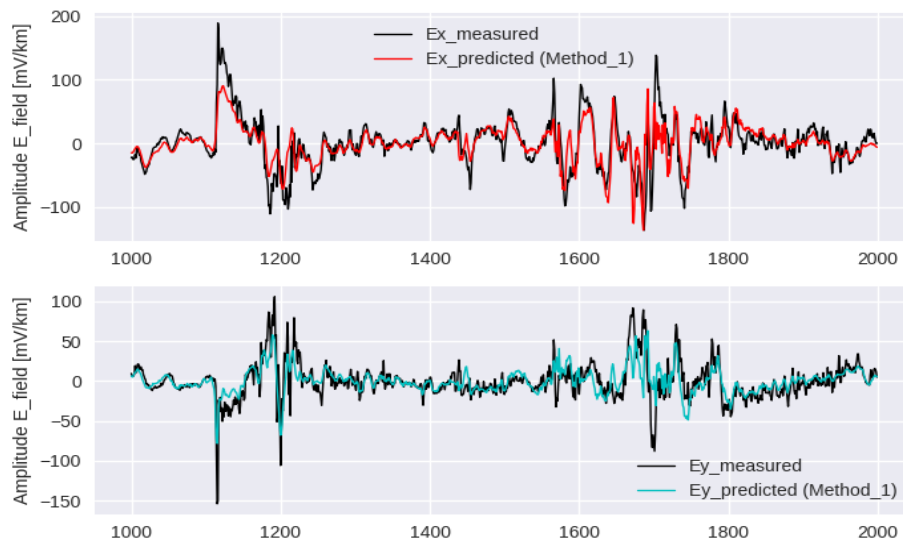
using
for $i =$

Mr: Magnetic Field
(less affected by local storms)

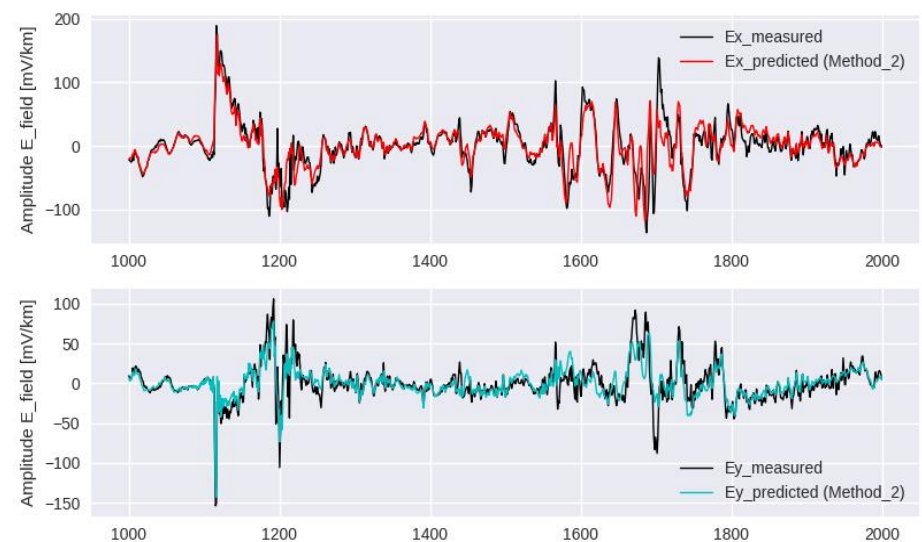
Modelling E fields

22-23 June 2015 Storm, ESK Observatory

Method 1



Method 2



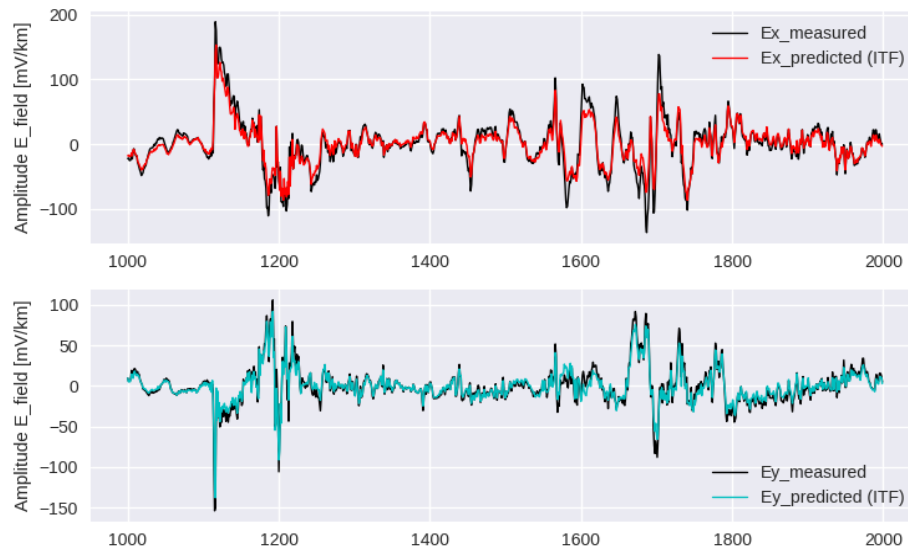
	Ex	Ey
Coherence	0.81	0.76
RMS	12.65	7.29
Pp	0.40	0.34

	Ex	Ey
Coherence	0.86	0.80
RMS	10.32	6.31
Pp	0.47	0.39

Modelling E fields

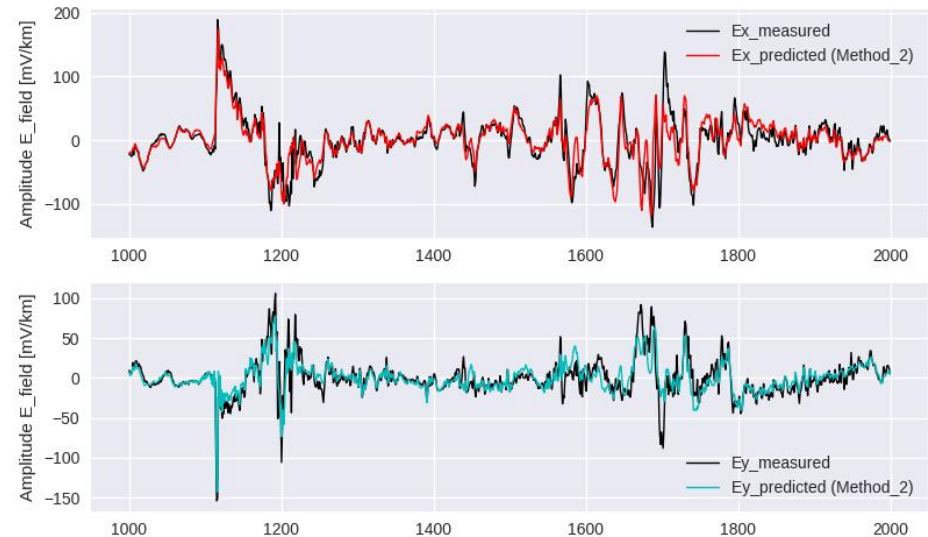
22-23 June 2015 Storm, ESK Observatory

MT with B_{ESK}



	Ex	Ey
Coherence	0.97	0.98
RMS	7.22	2.99
Pp	0.68	0.76

Method 2



	Ex	Ey
Coherence	0.86	0.80
RMS	10.32	6.31
Pp	0.47	0.39

Modelling E fields

ESK and LEI sites for two different storms

17-18 March, 2015

	Method_1			Method_2			Local B			Dist. Obs.
	Coh	RMS	Pp	Coh	RMS	Pp	Coh	RMS	Pp	[km]
ESK	0.64	7.12	0.24	0.72	6.60	0.30	0.98	3.35	0.73	400
LEI	0.86	2.61	0.37	0.87	1.86	0.43	0.98	0.98	0.69	125

*ARM Observatory stop recording

22-23 June, 2015

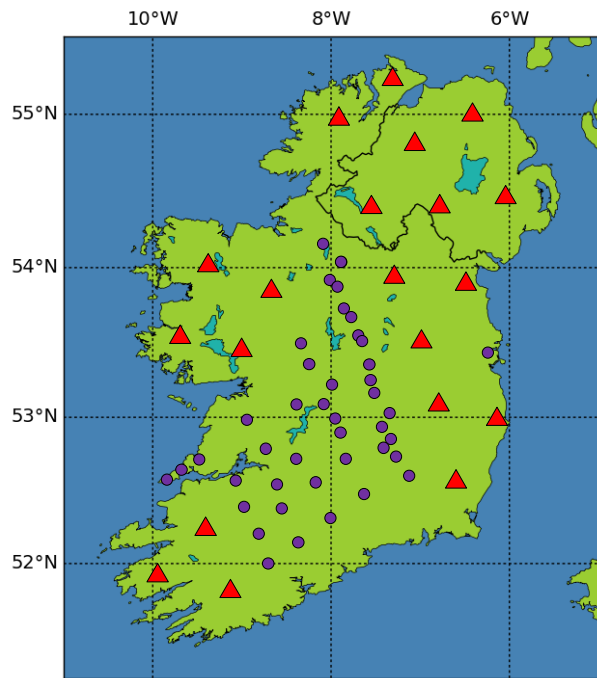
	Method_1			Method_2			Local B			Dist. Obs.
	Coh	RMS	Pp	Coh	RMS	Pp	Coh	RMS	Pp	[km]
ESK	0.79	9.92	0.37	0.83	8.21	0.44	0.97	4.67	0.72	250
LEI	0.93	1.42	0.56	0.93	1.21	0.60	0.96	1.11	0.64	95

$1 \geq |\text{Coherence (Coh)}| \geq 0$

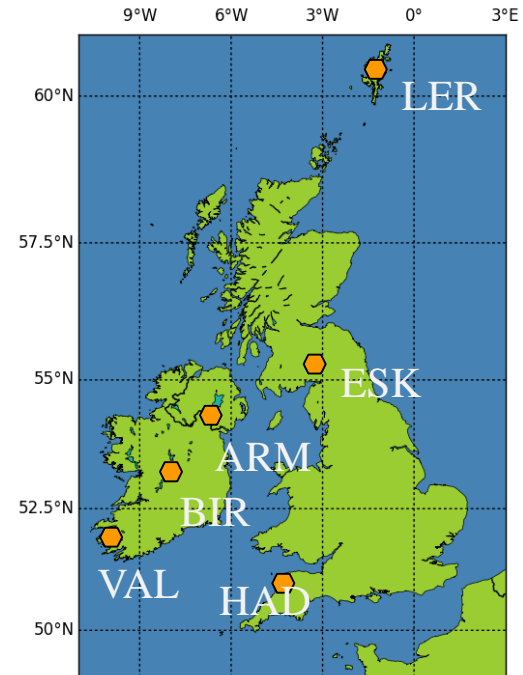
$1 \geq \text{Performance Parameter (Pp)} \geq 0$

New EM data

Ireland and UK



▲ New EM Sites ● Sites already acquired



● Permanent magnetic observatories



Conclusions

Modelling electric fields in Ireland and UK

- **New approach for modelling E fields (*Method 2*)**
 - Higher accuracy
 - Differentiate between local and regional signal

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- **Constrained levels of accuracy (approx.):**
 - Ireland: $\text{Coh} \geq 0.8$; $\text{Pp} \geq 0.4$
 - UK: $\text{Coh} \geq 0.65$; $\text{Pp} \geq 0.3$
 - RMS depends on the storm; larger storms larger RMS

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- **New EM data in Ireland and UK**
 - Modelling EM fields at country scale.

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 - RMS depends on the storm; larger storms larger RMS
- **New EM data in Ireland and UK**
 - Modelling EM fields at country scale.
- **Computational costs**
 - Over 7 min with standard PC, mostly to calculate SECS, which is not ideal for monitoring (Machine learning?)

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